



# Noise Models and Correction for fMRI

## - *an Introduction to the PhysIO Toolbox*

Lars Kasper

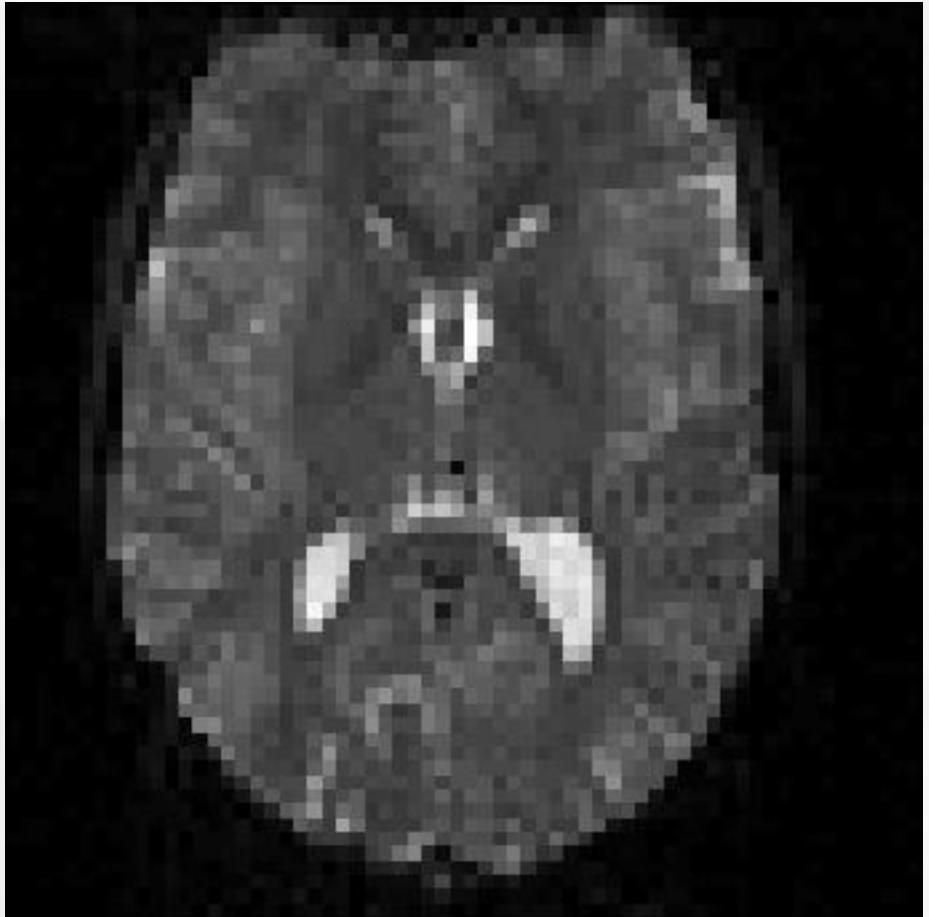
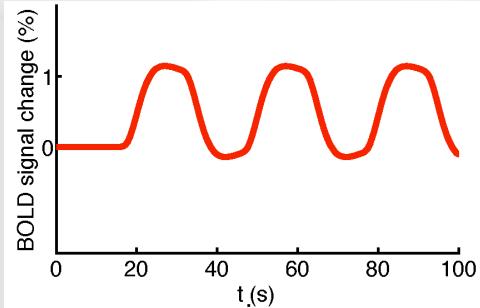
Jan 9<sup>th</sup>, 2017

MR-Technology Group & Translational Neuromodeling Unit

Institute for Biomedical Engineering  
University of Zurich and ETH Zurich



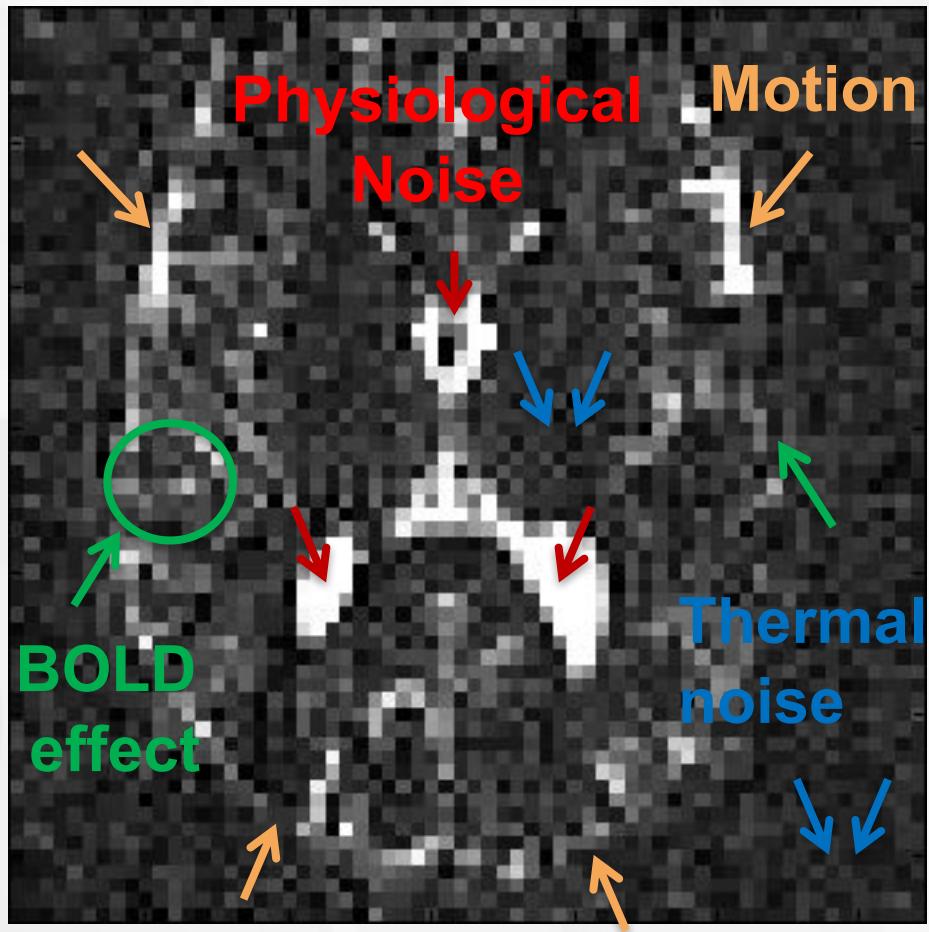
# fMRI Data is noisy...



# fMRI Data is noisy...



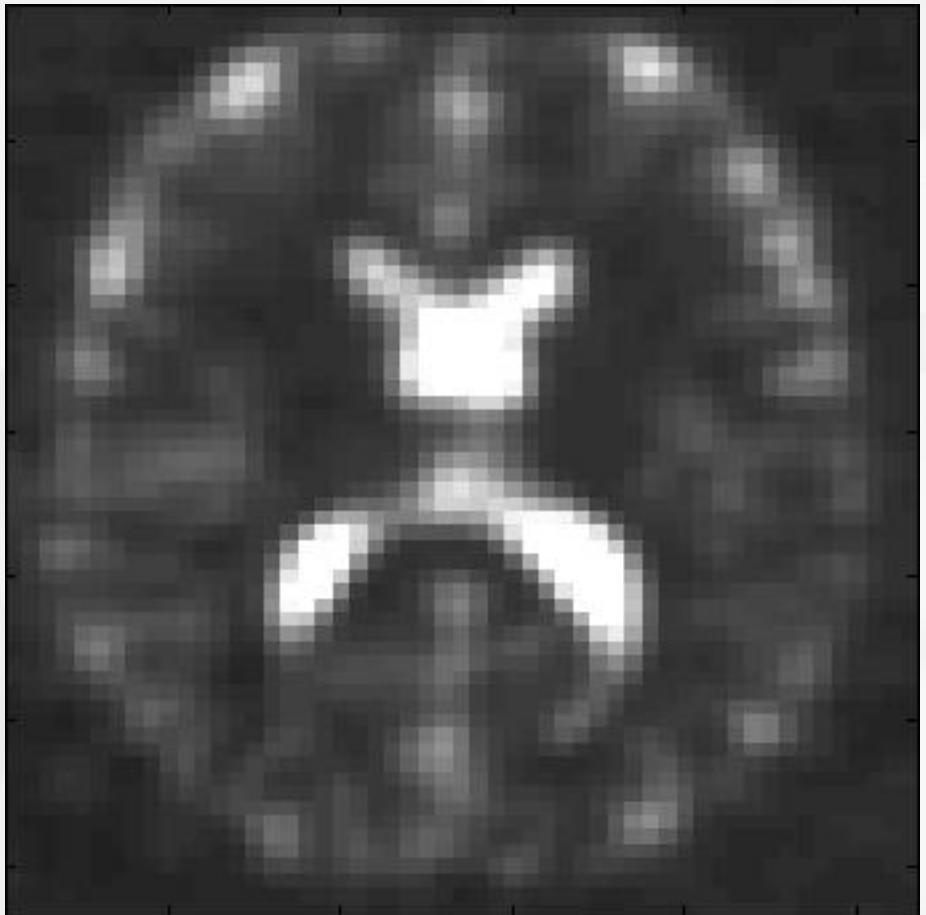
- Interest in fluctuations only: Subtract the mean



# fMRI Data is (still) noisy



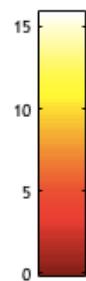
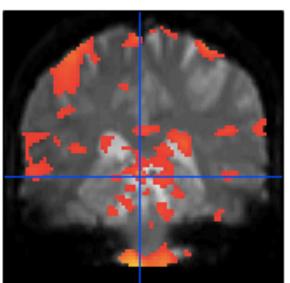
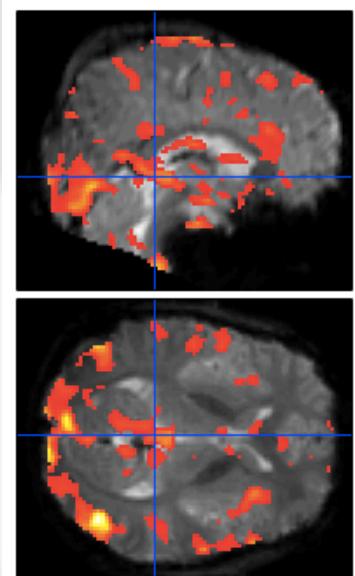
- After preprocessing...
- Much better, but still:  
some fluctuation



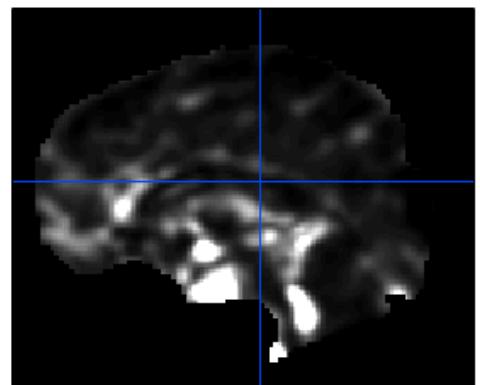
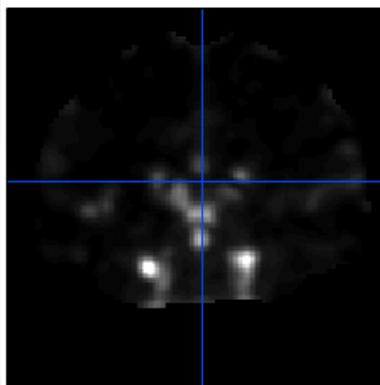
# Noise and Statistics



- GLM folder: ResMS image
- Indicates where model incomplete...
- limits sensitivity...



F contrast  
All effects

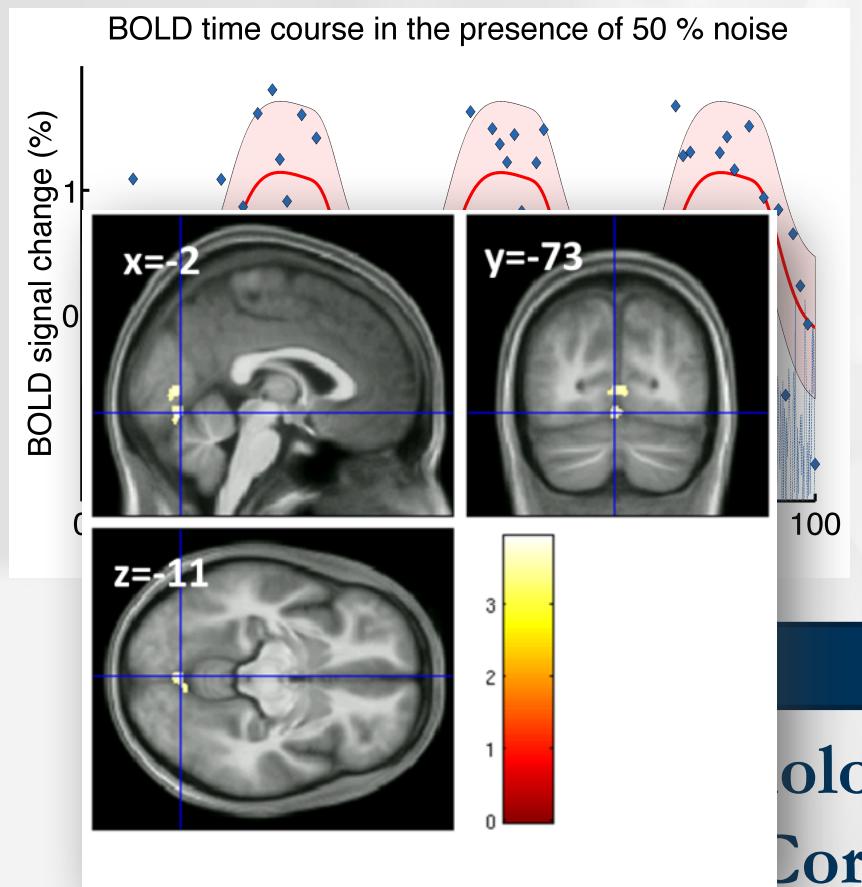


$$\widehat{\sigma^2} = \frac{(Y - X\beta)^2}{N - p}$$

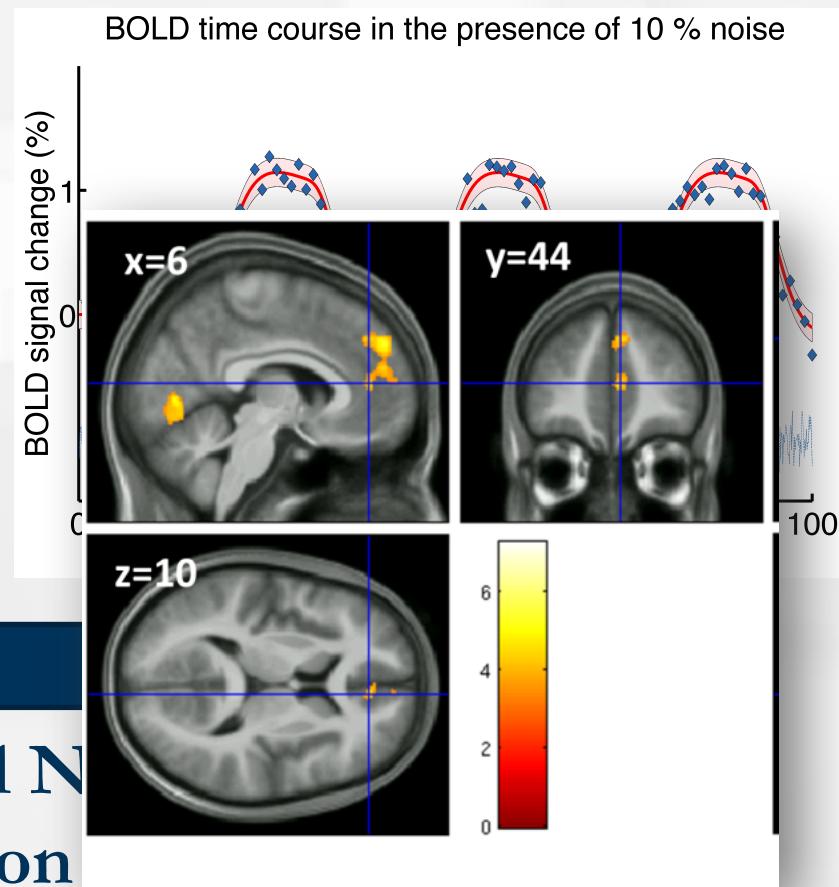
# The Goal of Noise Correction



Before



After



# The PhysIO Toolbox



- Toolbox for model-based physiological noise correction in fMRI
- Developed at the Translational Neuromodeling Unit (TNU)
  - Lead programmer: Lars Kasper (TNU, University of Zurich & ETH Zurich)
  - Contributors: Jakob Heinzle (TNU), Steffen Bollmann (KiSpi Zurich)
- Part of the TNU «TAPAS» software suite
- Used at the TNU, in Zurich and beyond by ~50 researchers
  - Iglesias 2013, Neuron; Kasper 2014, NeuroImage; Sulzer 2013, NeuroImage; Hauser 2014, NeuroImage; Grueschow 2015, Neuron; Diaconescu 2017, SCAN
- Download & Example Data:
  - <https://translationalneuromodeling.org/tapas>
  - <https://www.tnu.ethz.ch/en/software/tapas/data.html>

# Outline – Noise Correction



- MRI Time Series Recap and Noise Sources
  - Why de-noising? Structured Noise; Noise Pathways
- Noise Correction Approaches
  - Method: Modeling VS Preprocessing
  - Target: Motion, Cardiac/Breathing Cycle
  - Input: fMRI Data VS Peripheral Measures
- Prospects for Improving Group Statistics
- Limitations
  - Degrees of Freedom; Task-related “noise”; Interoception

# Outline – Noise Correction



- **MRI Time Series Recap and Noise Sources**
  - Why de-noising? Structured Noise; Noise Pathways
- Noise Correction Approaches
  - Method: Modeling VS Preprocessing
  - Target: Motion, Cardiac/Breathing Cycle
  - Input: fMRI Data VS Peripheral Measures
- Prospects for Improving Group Statistics
- Limitations
  - Degrees of Freedom; Task-related “noise”; Interoception

# fMRI = Acquiring Movies

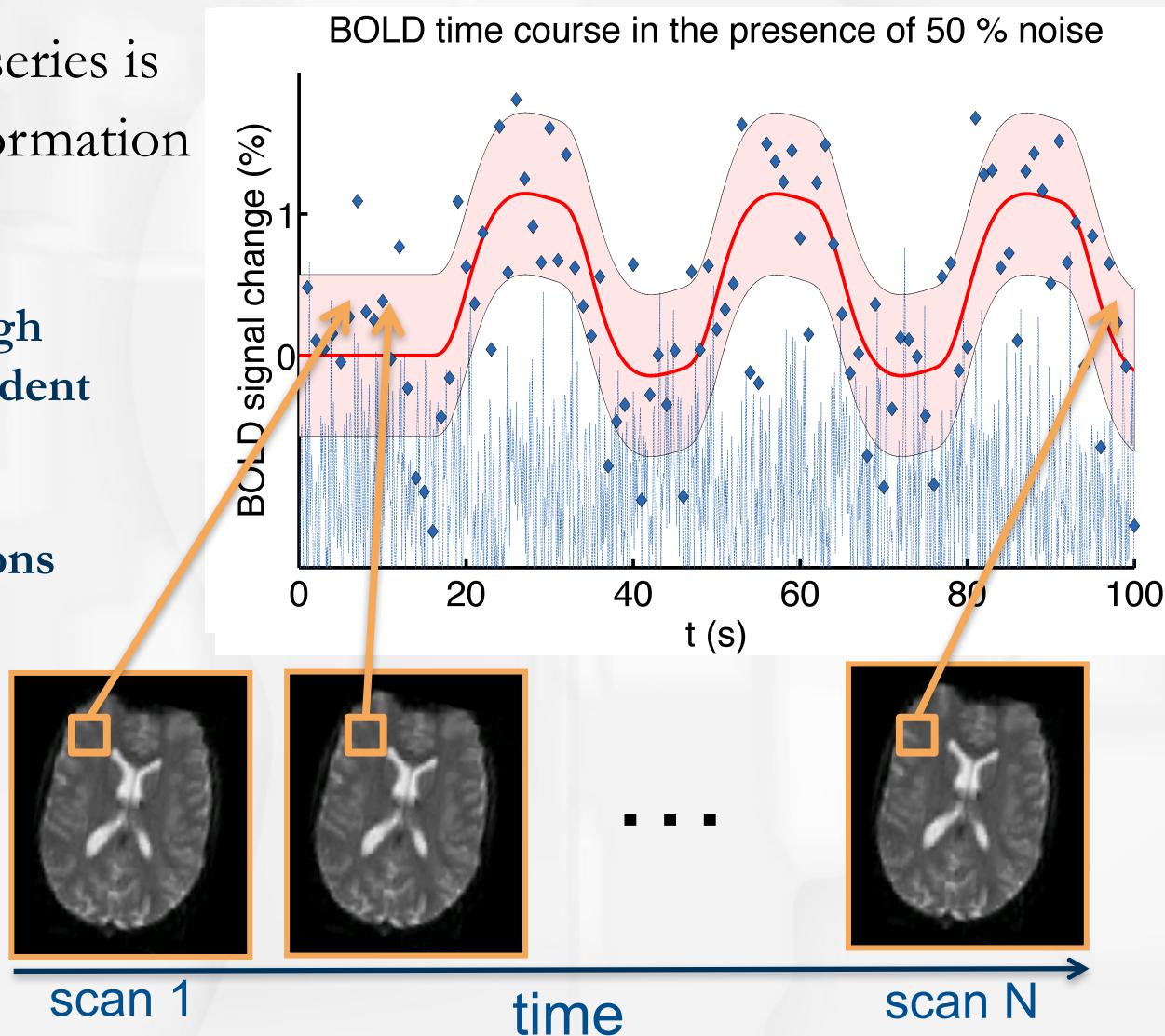


- The Localized Time-series is the Fundamental Information Unit of fMRI

**Signal:** Fluctuation through Blood oxygen level dependent (**BOLD**) contrast

**Noise:** All other fluctuations

- Run/Session:  
Time Series of Images



# Noise Categories & Reduction



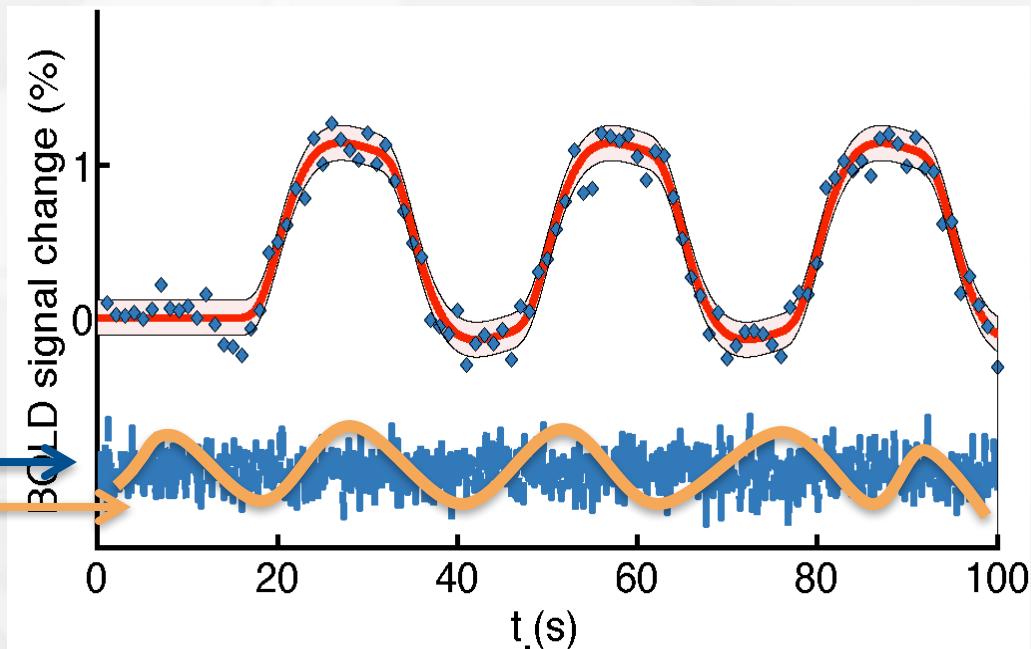
## Thermal Noise

- temporally uncorrelated
- reduced SNR → risk of false negatives
- Remedy: Spatial Smoothing

## Noise: All other fluctuations

## “Structured” Noise

- temporally correlated
- reduced SNR → risk of false negatives
- correlated with task → risk of false positives
- Remedy: Noise modeling (e.g. GLM)



Inference = Signal-To-Noise

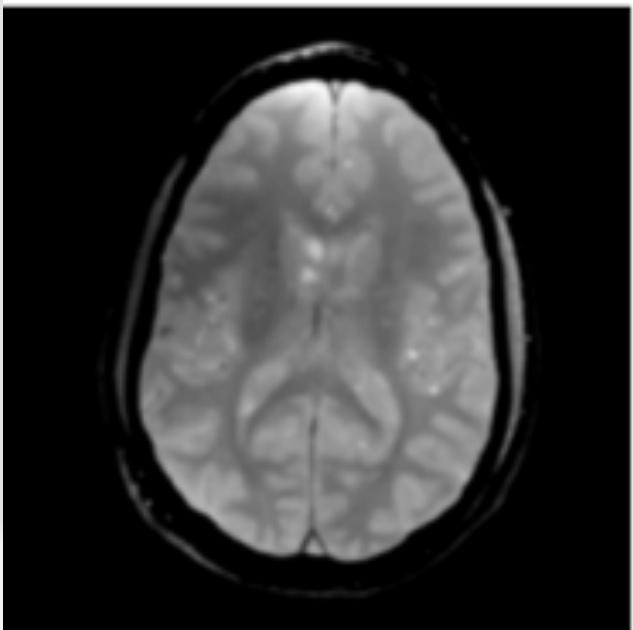
$$t = \frac{\beta}{\sqrt{\sigma_{\varepsilon}^2(X^T X)^{-1}}} = \frac{\beta \|x\|}{\hat{\sigma}_{\varepsilon}}$$

$$F = \frac{N - M}{M_1} \cdot \frac{(\sigma_S^2 + \sigma_N^2) - \sigma_N^2}{\sigma_N^2}$$

# Recap: MR Image Encoding



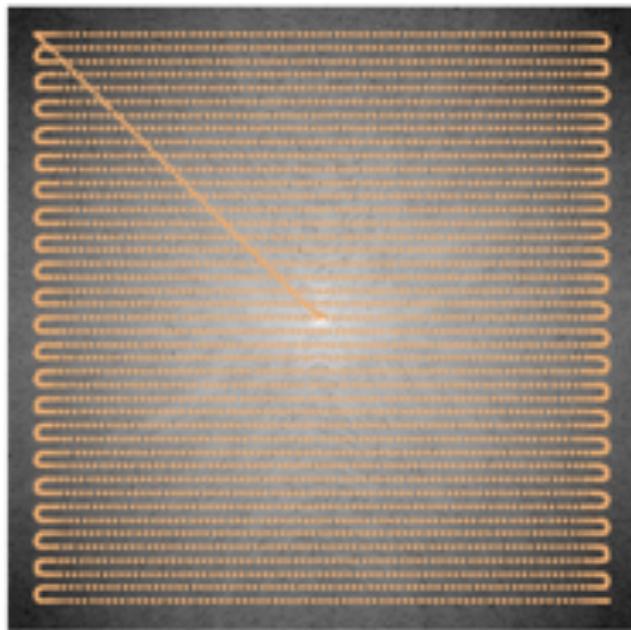
Image Space ( $m$ )



$y$   
↑  
 $x$

Fourier  
Transform  
(FT)  
In general:  
Image  
Encoding  
 $E$

k-Space ( $s$ )



$k_y$   
↑  
 $k_x$

# Image Reconstruction & Noise



$$s = E \cdot m + \eta$$

Coil Signal

Encoding      Object      Thermal

Matrix      Magnetization      Noise

- Image reconstruction is also (often) a GLM, though a huge one,  $\sim 100.000$  rows
- Any changes between encodings (images) in encoding matrix (field), object magnetization and thermally induces image noise

$$\hat{m} = (E^H E)^{-1} E^H s$$

$$\begin{aligned} s_1 \\ s_2 = E_2 \cdot m_2 + \eta_2 \\ \vdots \\ s_N = E_N \cdot m_N + \eta_N \end{aligned}$$

Time Series

# What fluctuates?



Noise Sources

Imaged Object

MR System

Entry Points  
of Noise

Encoding  
Magnetic Fields

Magnetization

Receiver Channels  
(Thermal Noise)

Forward Model:  
MR Image  
Encoding

$$\mathbf{s} = \mathbf{E} \cdot \mathbf{m} + \boldsymbol{\eta}$$

Encoding

Matrix

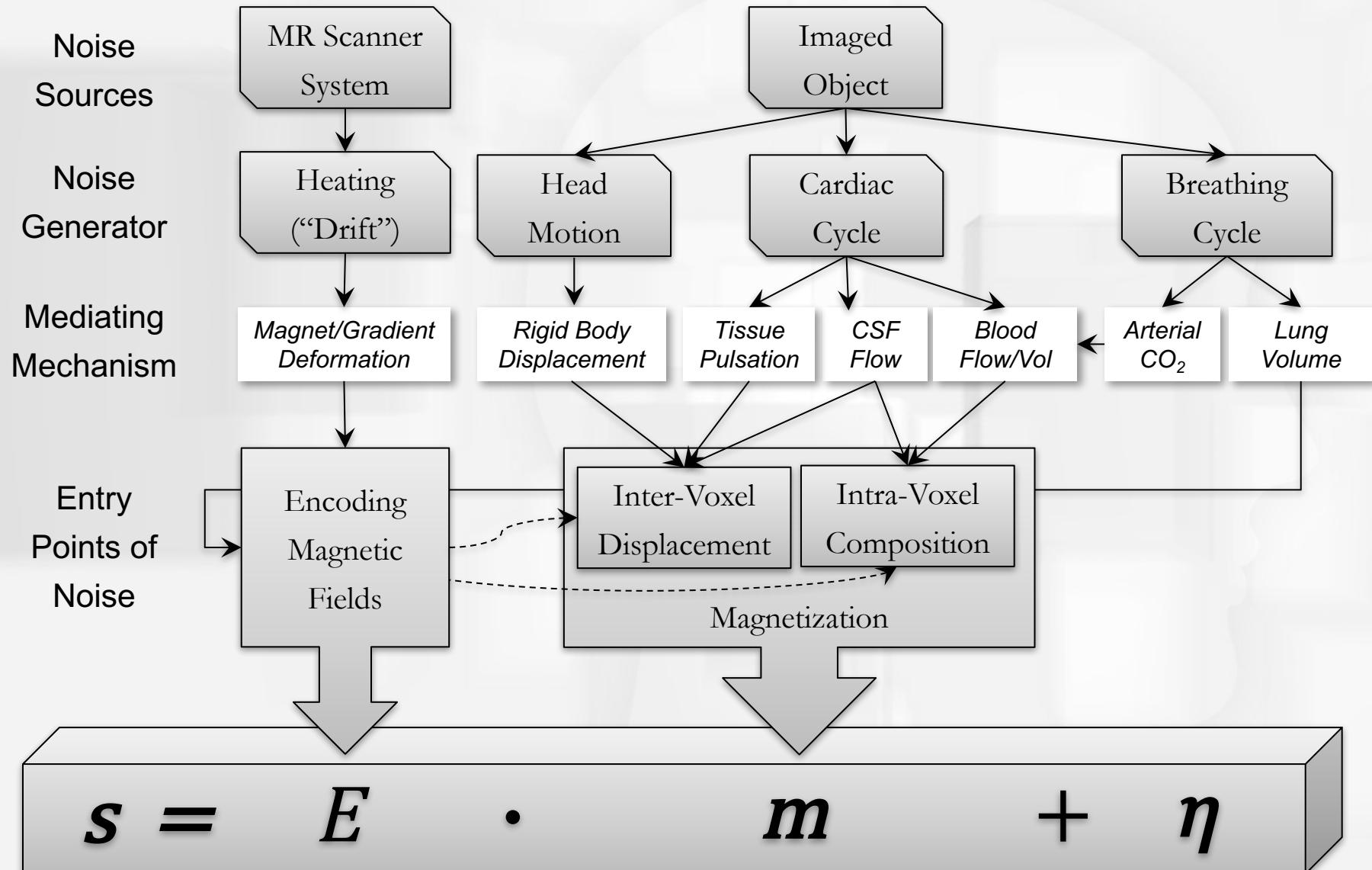
Object

Magnetization

Thermal

Noise

# Structured Noise in MRI



# The Problem: Physiological Noise



- Cardiac effects
- Respiratory effects

# The Problem: Physiological Noise



## Cardiac effects

- Systole:
  - Blood pumped into brain, vessel volume increases: pulsatile vessels
  - CSF pushed down: pulsatile CSF
- Diastole:
  - Vessel volume decreases
  - CSF flows back into “void” brain volume

## A Cardiac Cycle in the Brain

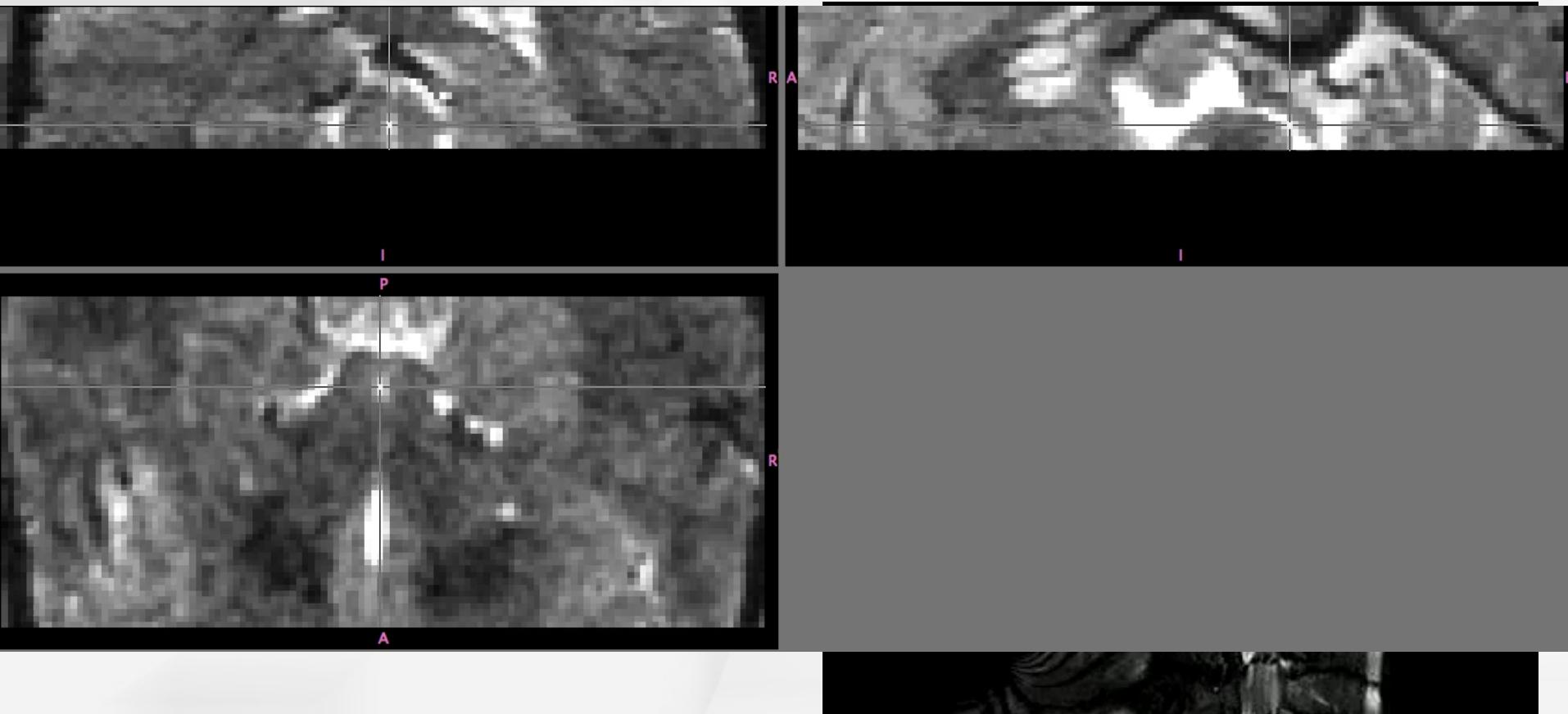


# The Problem: Physiological Noise



Triggered High-Resolution fMRI

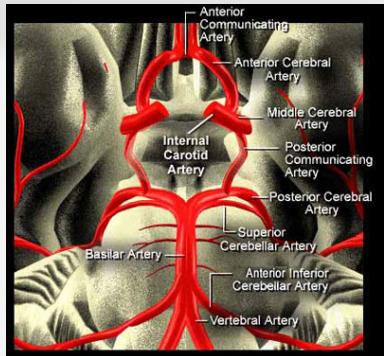
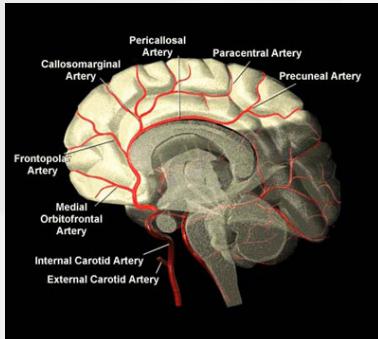
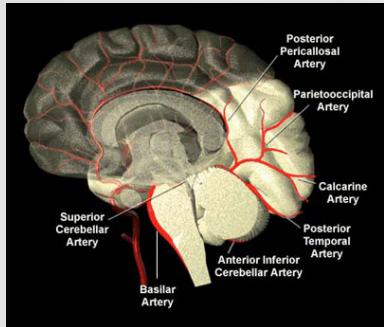
A Cardiac Cycle in the Brain



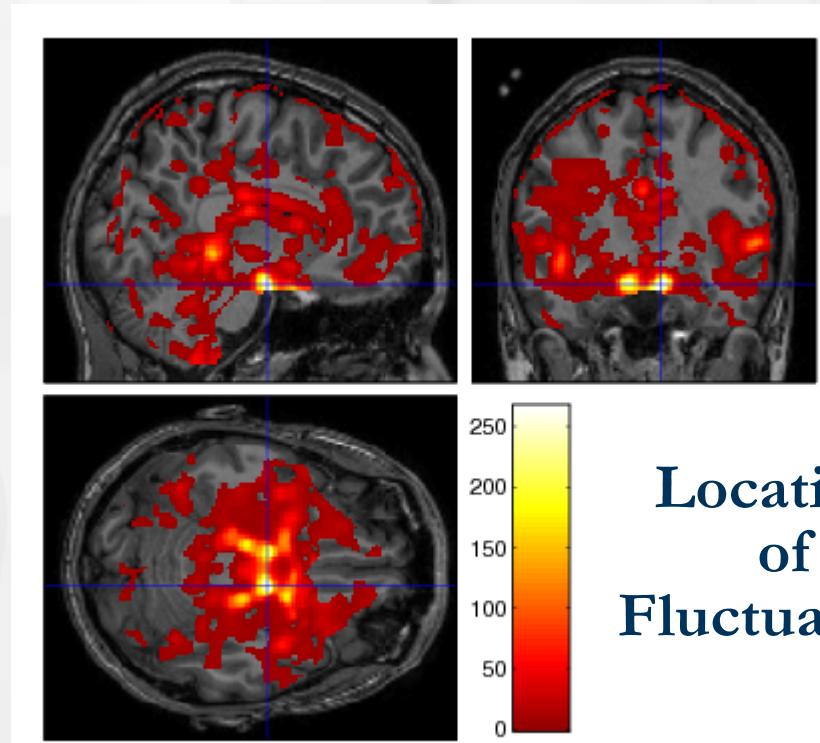
# The Problem: Physiological Noise



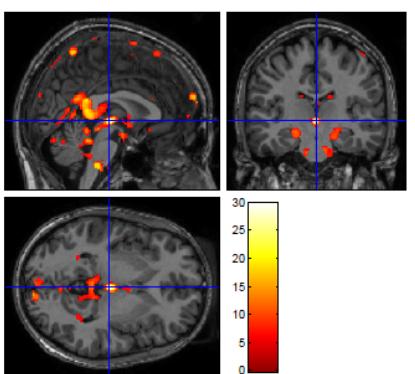
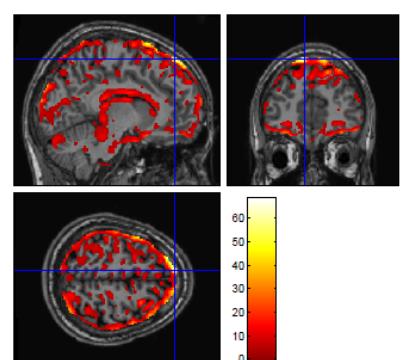
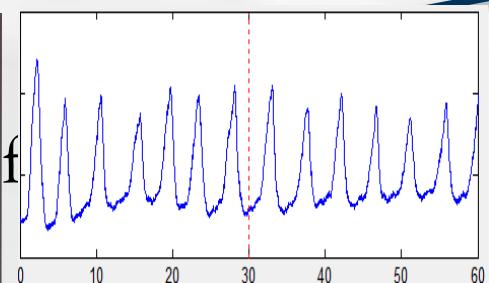
- Cardiac effects



Vessel  
Anatomy



# The Problem: Physiological Noise



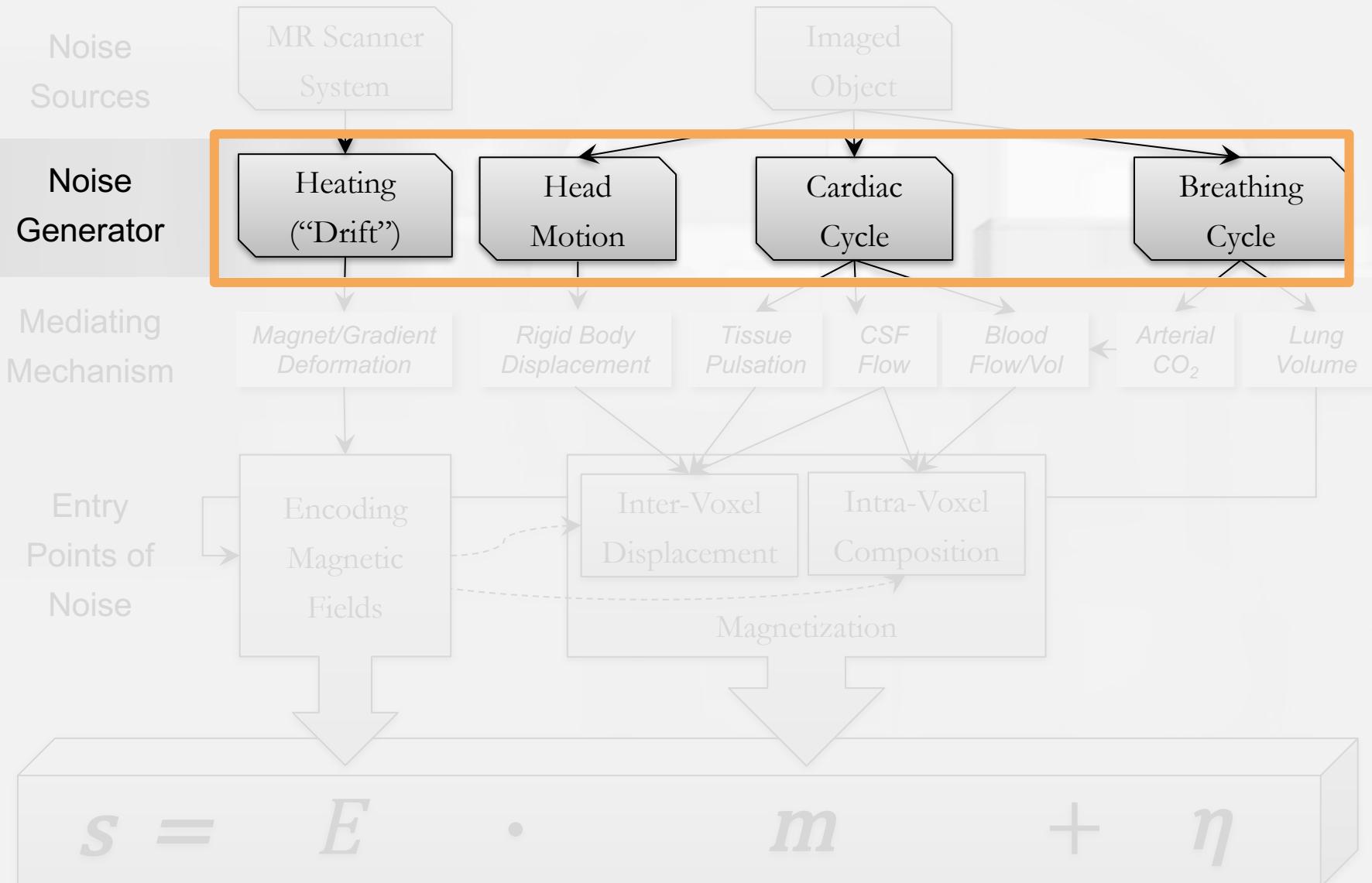
- Respiratory effects
  - Chest (&head) moves with respiratory cycle
  - Changes in lung volume change encoding magnetic field for MR
    - Geometric distortion/scaling
  - Respiratory-sinus arrhythmia
    - Heart beats faster during inhalation

# Outline – Noise Correction



- MRI Time Series Recap and Noise Sources
  - Why de-noising? Structured Noise; Noise Pathways
- **Noise Correction Approaches**
  - Method: Modeling VS Preprocessing
  - Target: Motion, Cardiac/Breathing Cycle
  - Input: fMRI Data VS Peripheral Measures
- Prospects for Improving Group Statistics
- Limitations
  - Degrees of Freedom; Task-related “noise”; Interoception

# Noise Correction Targets



# Preprocessing and Limits



- Acquisition Timing

Temporal Preproc

- Subject Motion

Spatial Preproc

- Anatomical Identity

Spatial Preproc

- Inter-subject variability

Spatial Preproc

- Thermal Noise

Spatial Preproc

- Physiological Noise

Noise Modeling

- Slice-Timing

- Realignment

- Co-registration

- Segmentation

- Smoothing

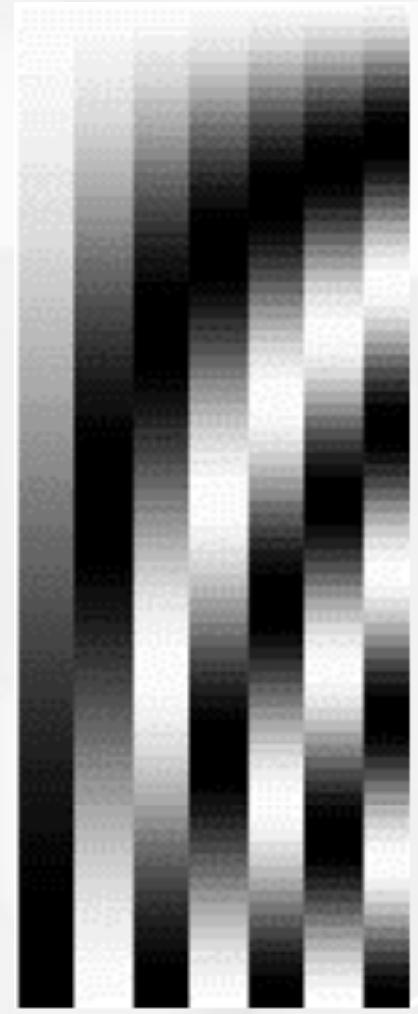
- PhysIO Toolbox

# Drift Example: Modeling/Preproc



- Discrete Cosine Model (last lecture) of slow oscillations (cycle  $\geq 128$  s)
- Was: Extra, non-task related columns in design matrix: **nuisance regressors**
- Now: Part of “hidden” preprocessing (high pass filtering)
  - Residual forming Matrix
$$K = \mathbf{1} - \mathbf{X}_0(\mathbf{X}_0^T \mathbf{X}_0)^{-1} \mathbf{X}_0^T$$
  - With  $\mathbf{X}_0$  being the design matrix modeling the confounds
  - In fact, GLM in SPM estimates

$$K \cdot \mathbf{y} = K \cdot \mathbf{X} \cdot \boldsymbol{\beta} + K \cdot \boldsymbol{\varepsilon}$$



# Modeling VS Preprocessing



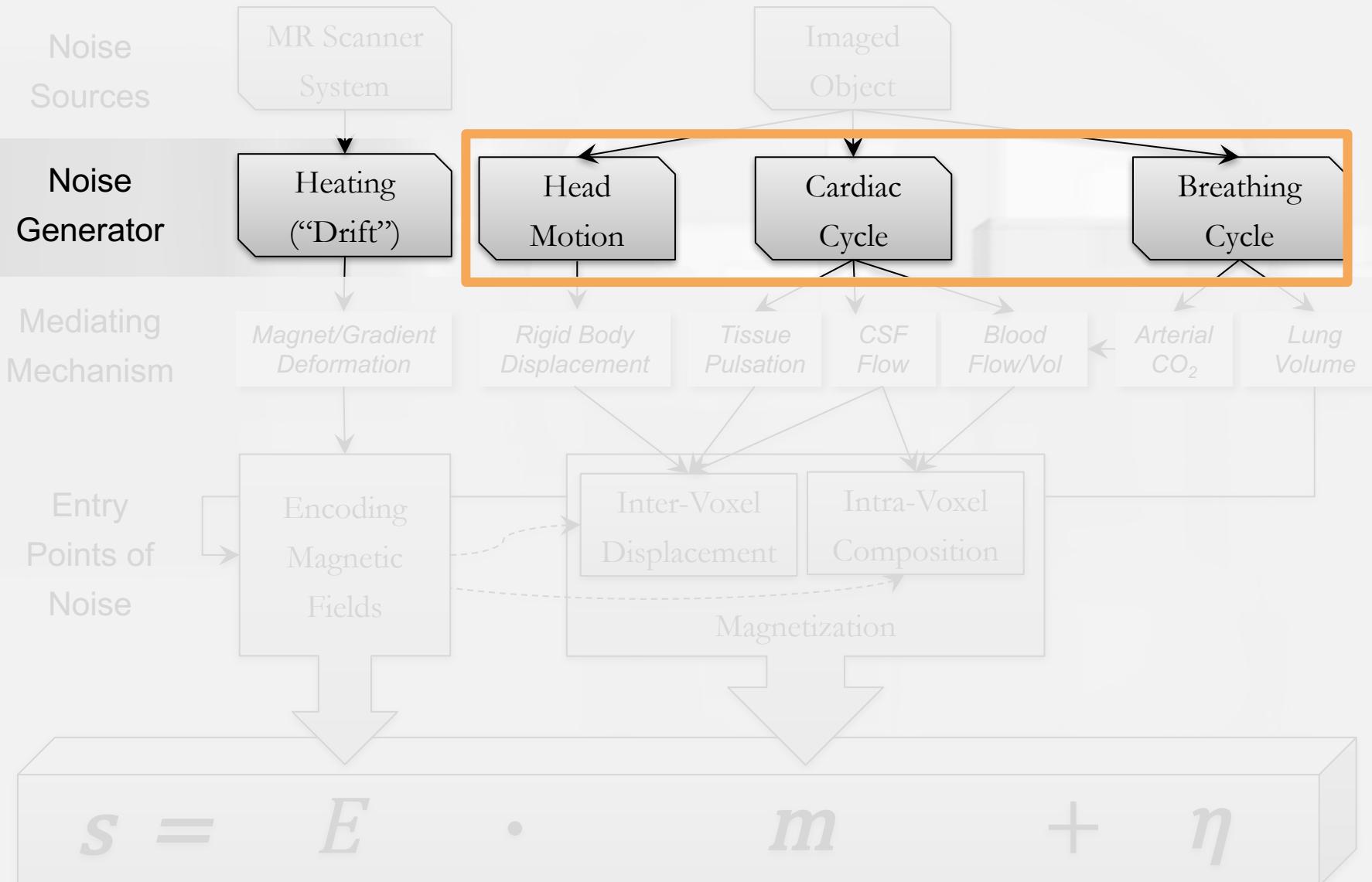
- Modeling:
  - Filters, projections (e.g. to independent components) etc. are all linear operations
  - Combination in one design matrix, together with task
  - Simple test of correction efficacy: F-test on nuisance regressors
- Preprocessing:
  - The data  $y$  entering the GLM is altered  $\Rightarrow y' = X\beta + \varepsilon$
  - For non-linear changes of  $y$  or inter-voxel dependencies, alteration outside GLM necessary

# The Problem with Preprocessing



- Problem: No inherent measure of efficacy (F-test in GLM), correlation with task regressors undetected
- “Advantage”: No loss of degrees of freedom (sensitivity of F-test)
  - But it is only a hidden loss, statistics for inference is biased, if performed modeling is not incorporated
- Modeling via GLM recommended, if possible
  - Drifts, Motion Regressors
  - RETROICOR, HRV, RVT
  - aCompCor, (ICA)

# Noise Correction Targets



# Motion: Preprocess & Modeling



- Correction for motion artifacts is actually a combination of Preprocessing and modeling
- Preprocessing cannot correct spin-history effects, intra-volume movements (non-rigid!), small partial volume effects
- Preprocessing:
  - Realignment
  - Motion “Scrubbing”
- Modeling (from estimated realignment parameters)
  - Retrospective Modeling: Motion Regressors
  - Motion Censoring

# Retrospective Motion Correction



- Best: Avoid subject motion in the first place
- Better: Use Prospective Motion Correction
- Standard: Perform rigid-body realignment, use parameters as nuisance regressors
  - 6 parameters: translation+rotation
  - 12 parameters: include derivatives (for temporal shifts)
  - 24 parameters: include squared regressors
- 24-parameter model known as Volterra expansion

*Friston, MRM, 1996*

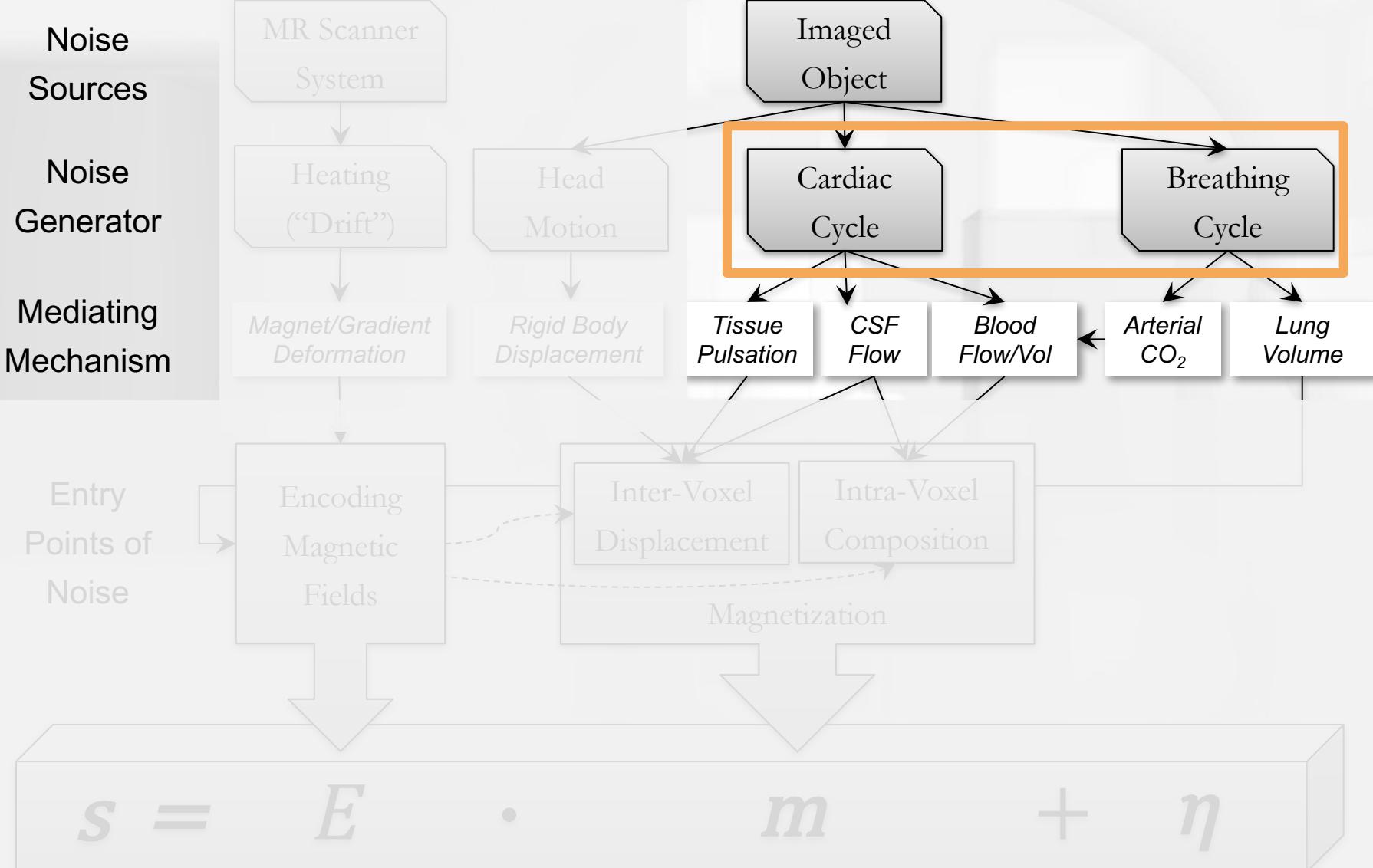
# Motion Censoring = “Scrubbing”



- Detect outlier volumes (strong movement, but also spikes, RF flip angle fluctuations)
- Inform the GLM of these bad volumes via stick regressors (zero everywhere else, 1 at volume)
  - Will absorb all variance of that volume
- Problem: Temporal filtering before GLM might create Gibbs ringing of outliers into neighbors
- Alternative: censoring during preprocessing
  - interpolate faulty volume by neighbors

*Power, NeuroImage, 2012*

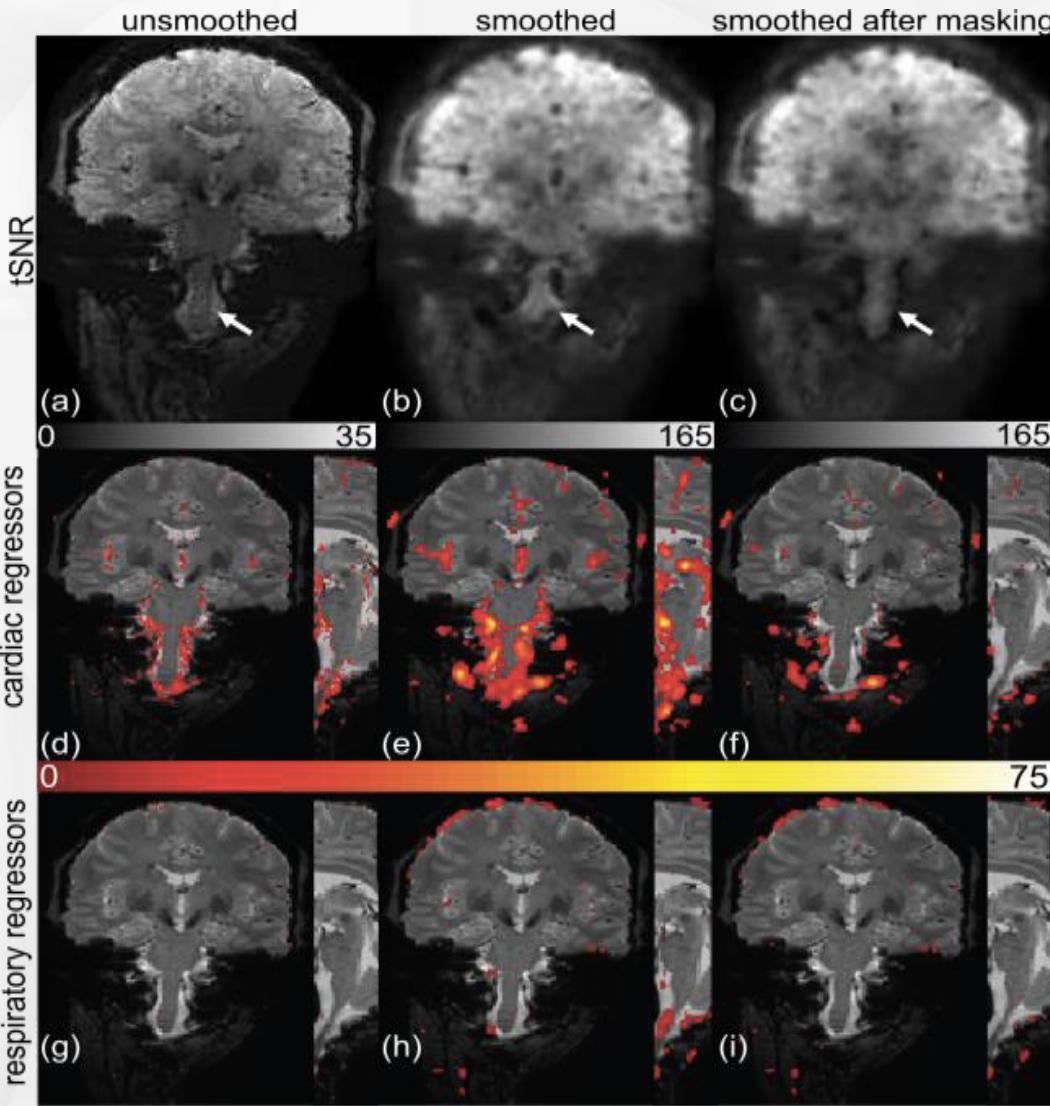
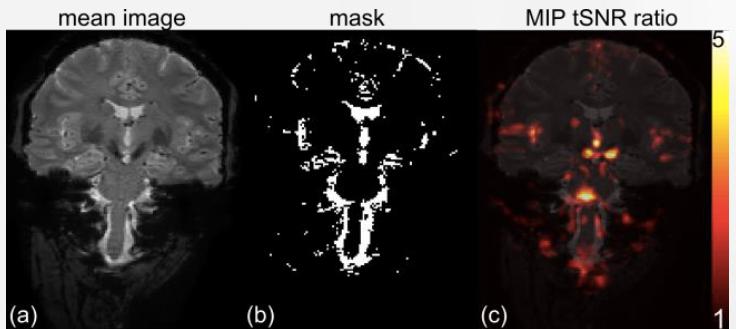
# Noise Correction Targets



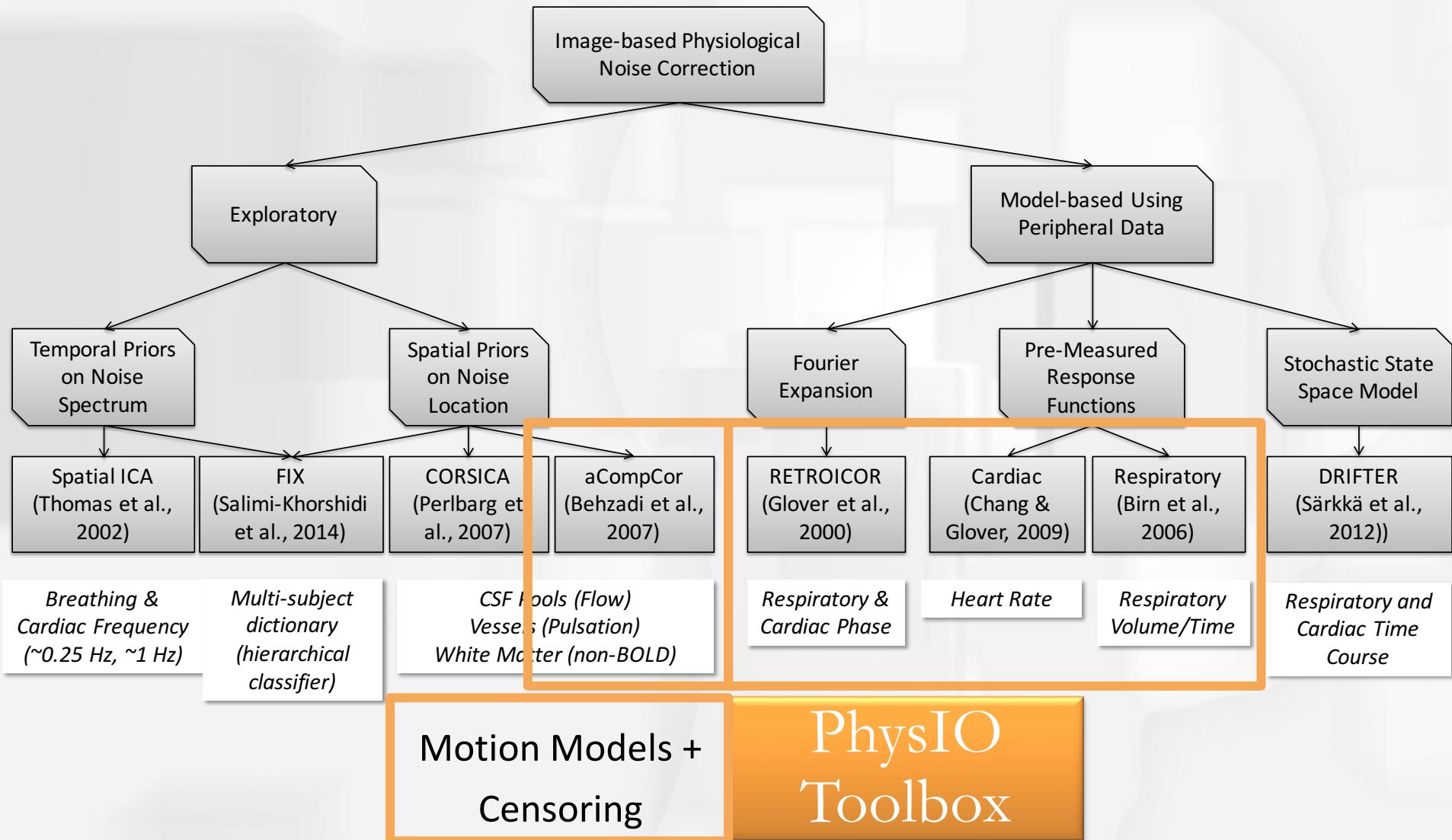
# Solution I: Mask it out!



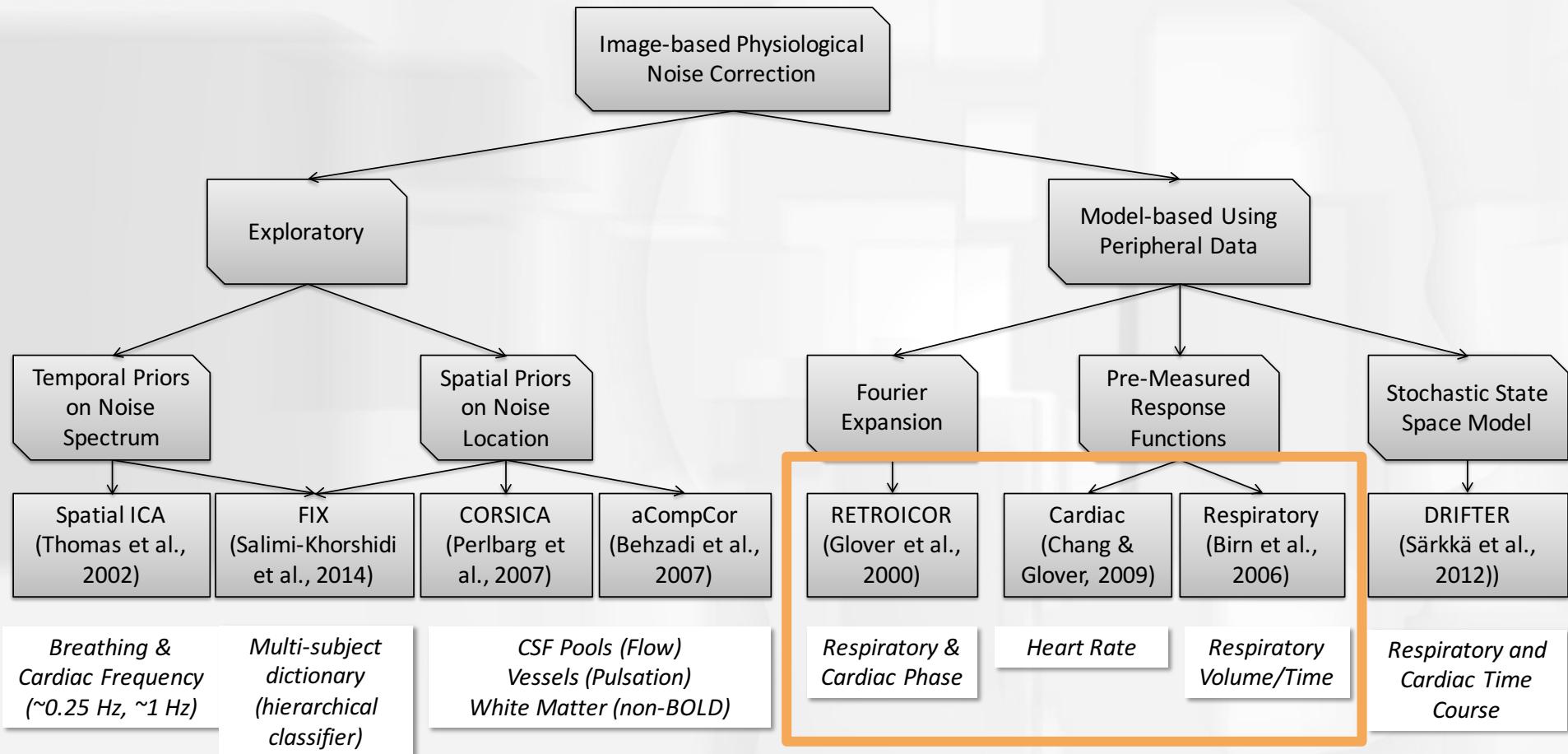
- Physiological noise origins close to, but not *in* gray matter
- High resolution data (1.25mm): mask CSF & vessels, then smooth!
  - *Vionnet 2015, ISMRM*



# Solution II: Image-based Correction



# Model-based Phys Noise Correction





# Noise Modeling

RETROSpective  
Image CORrection

Cardiac Response  
Function

Respiratory  
Response Function

- Cardiac/respiratory phase  $\varphi_c \quad \varphi_r$
- Fourier expansion (cosine/sine)
- evaluated at 1 time point (slice) per volume = regressor
- Heart Rate
- convolved with CRF
- Resp. Volume per Time
- convolved with RRF

# Noise Modeling

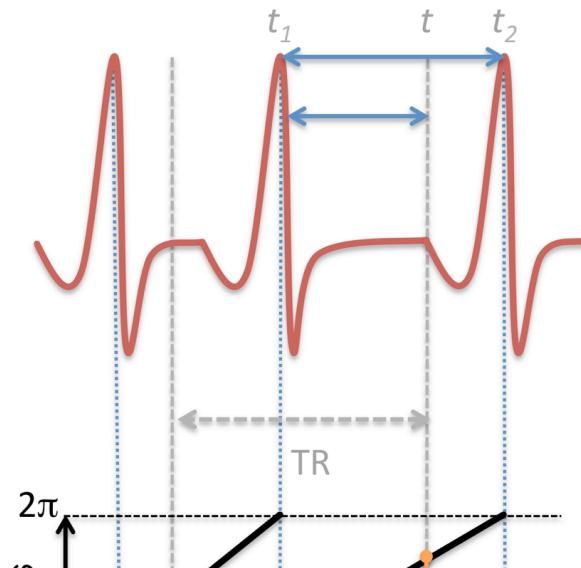


RETROSpective  
Image CORrection

Cardiac/Respiratory phase  
Function  $\varphi_c$       Respiratory  
Response Function  $\varphi_r$

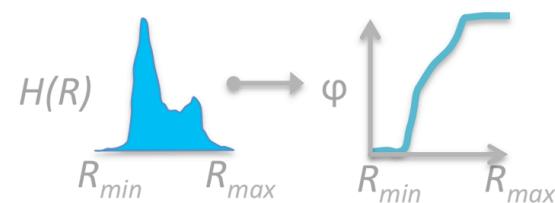
A

Cardiac



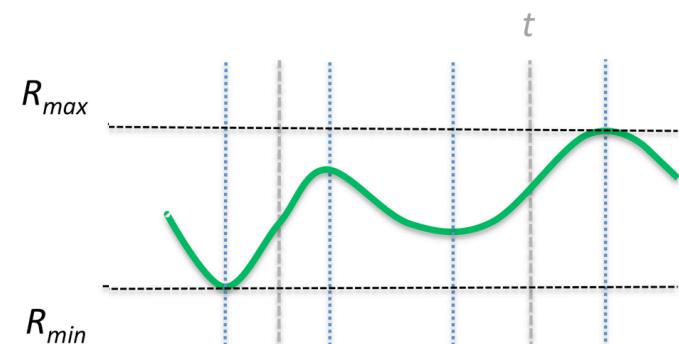
C

Histogram-equalized  
Transfer Function



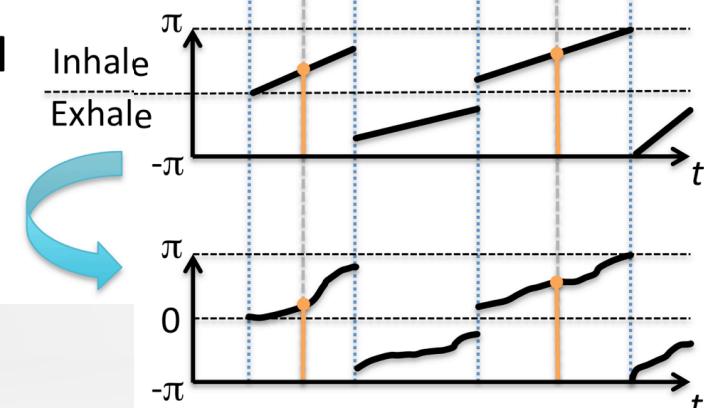
B

Respiratory



Peripheral  
Signal

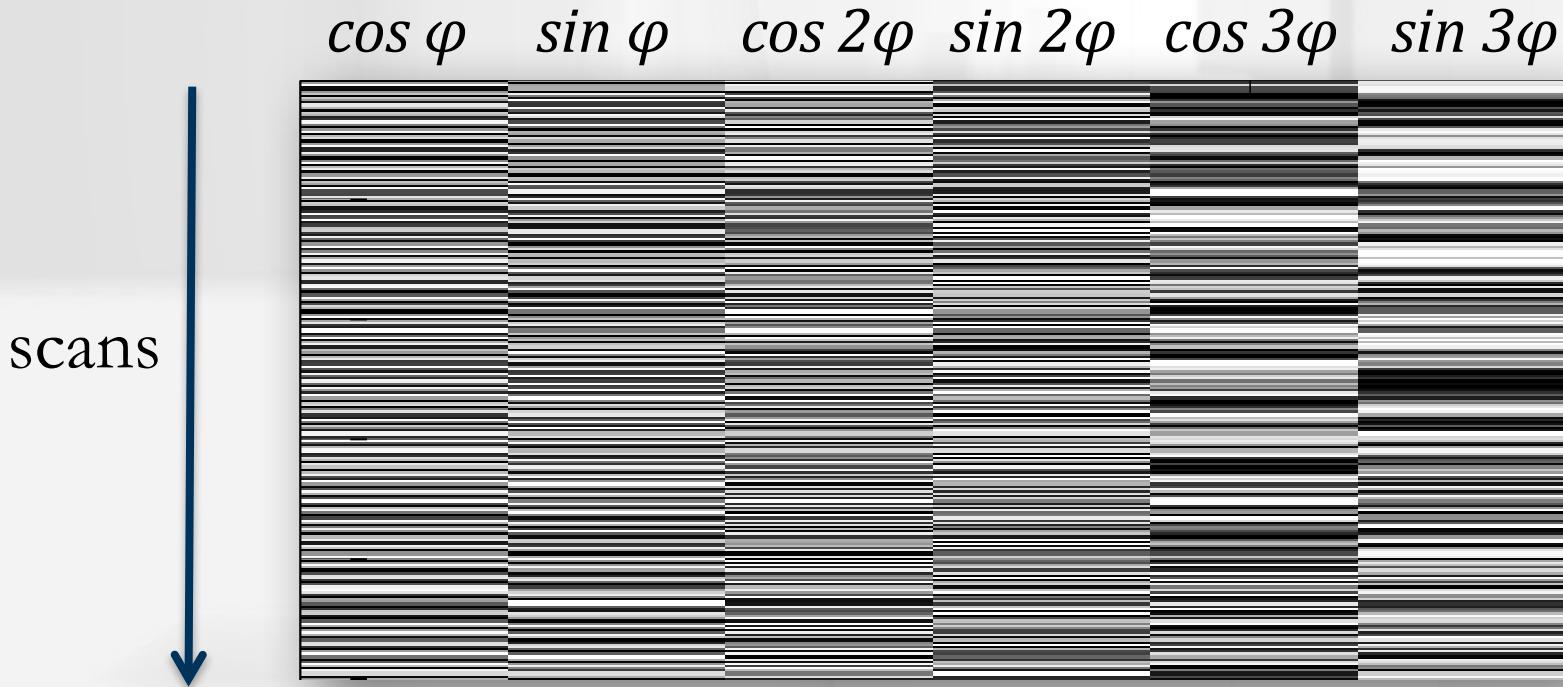
Estimated  
Phase



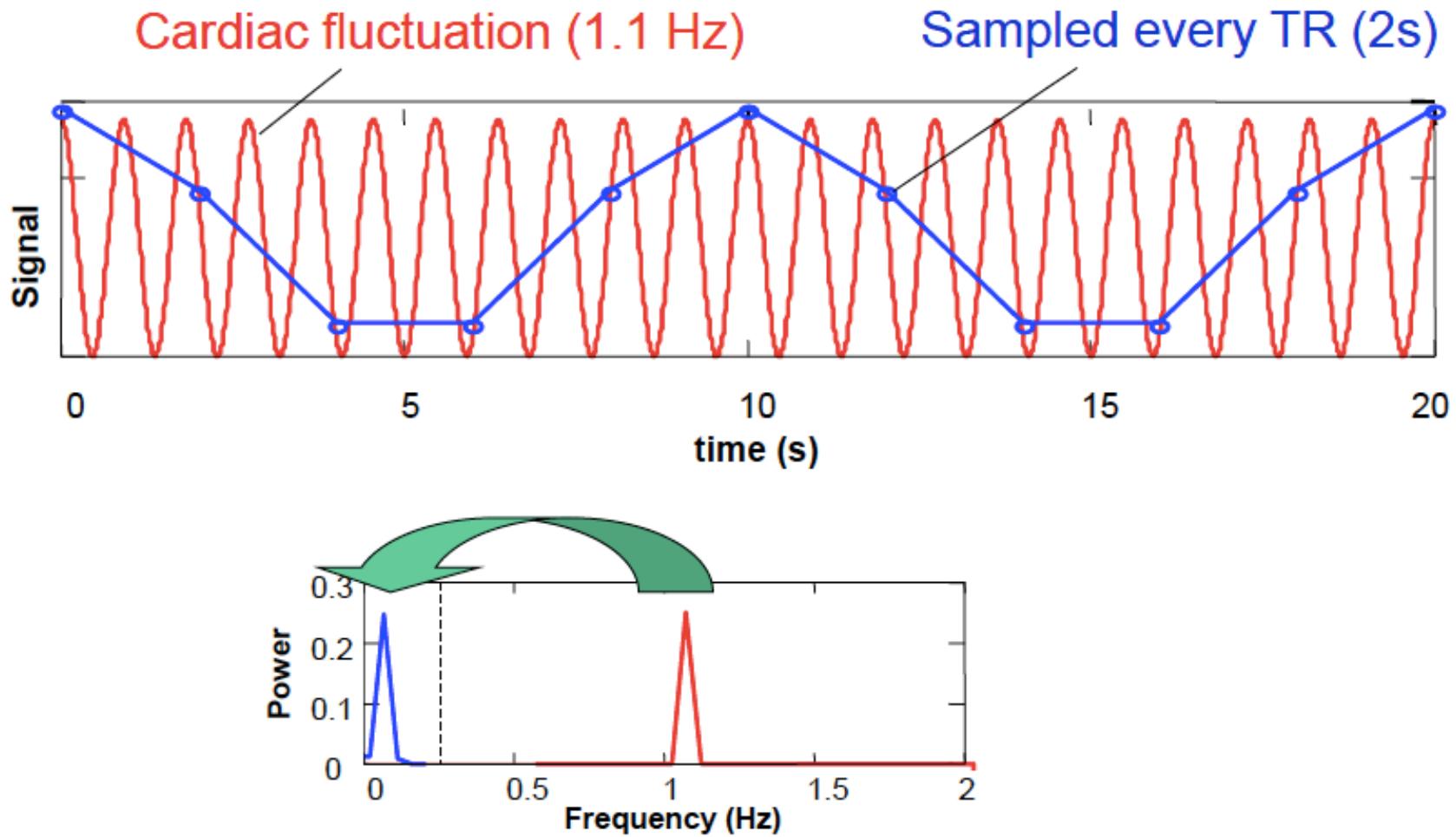
# Model: Fourier Phase Expansion



- Cosine and sine to allow for constant phase shifts per voxel
- Higher model orders to account for under-sampling of physiological frequencies with typical TR in fMRI



# Aliasing of Physiology



Courtesy: R. Birn, HBM 2015

# Noise Modeling



RETROspective  
Image CORrection

Cardiac Response  
Function

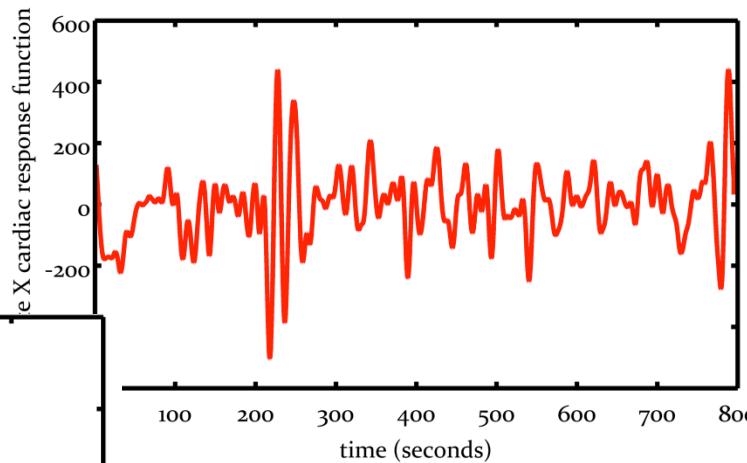
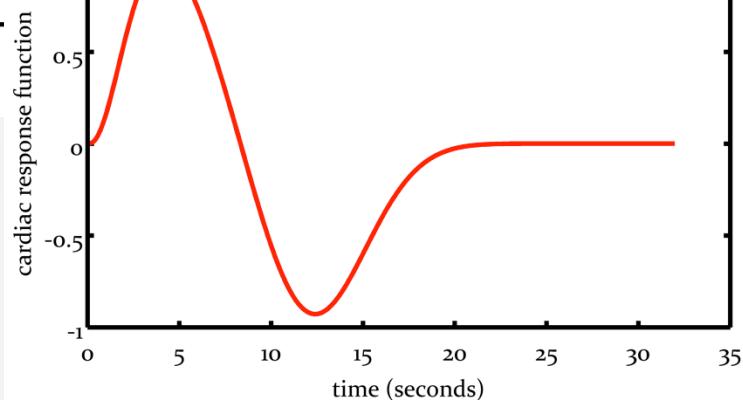
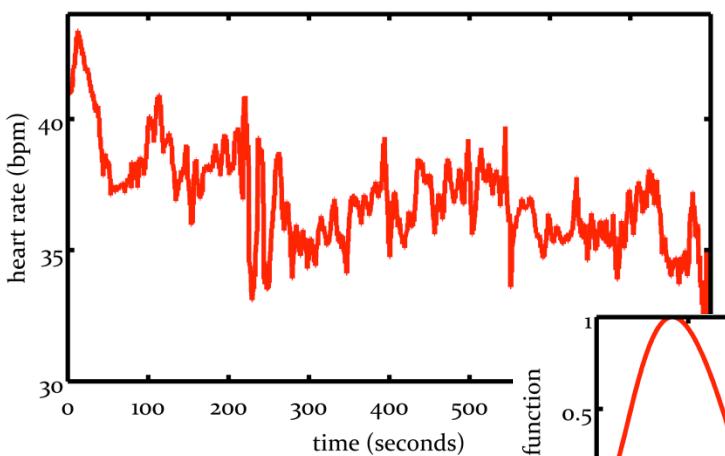
Respiratory  
Response Function

- Heart Rate

- convolved with

CRF

- Heart Rate Variability  
Response Regressor



# Noise Modeling

## RETROspective Image CORrection

## Cardiac Response Function

## Respiratory Response Function

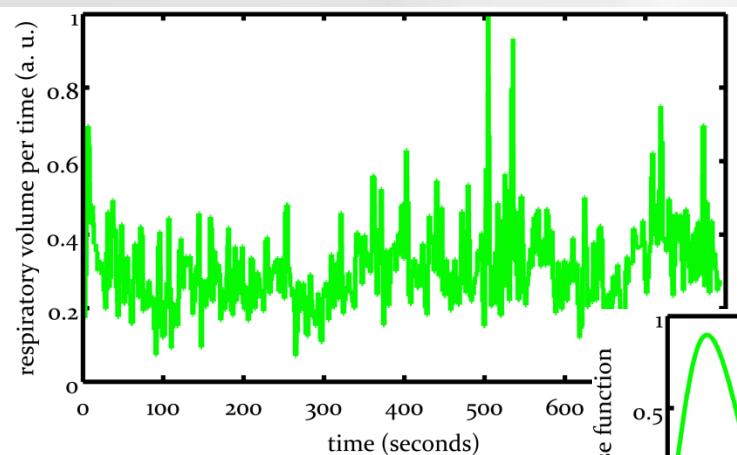
- Respiratory

Volume per Time

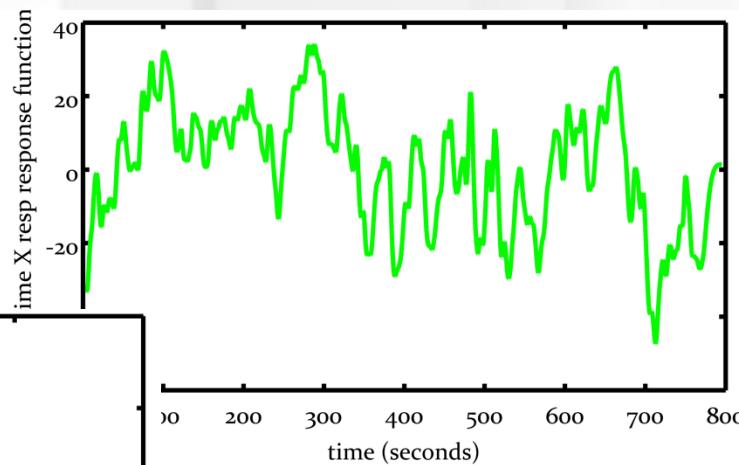
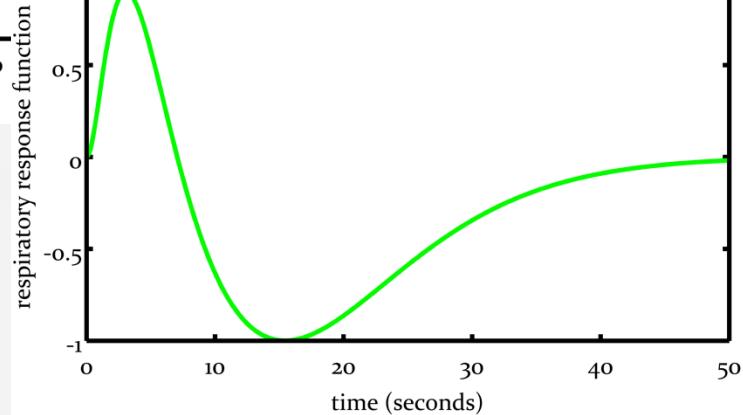
- convolved with

RRF

- Respiratory Volume  
per Time Regressor



respiratory response function



# Estimating the CRF/RRF

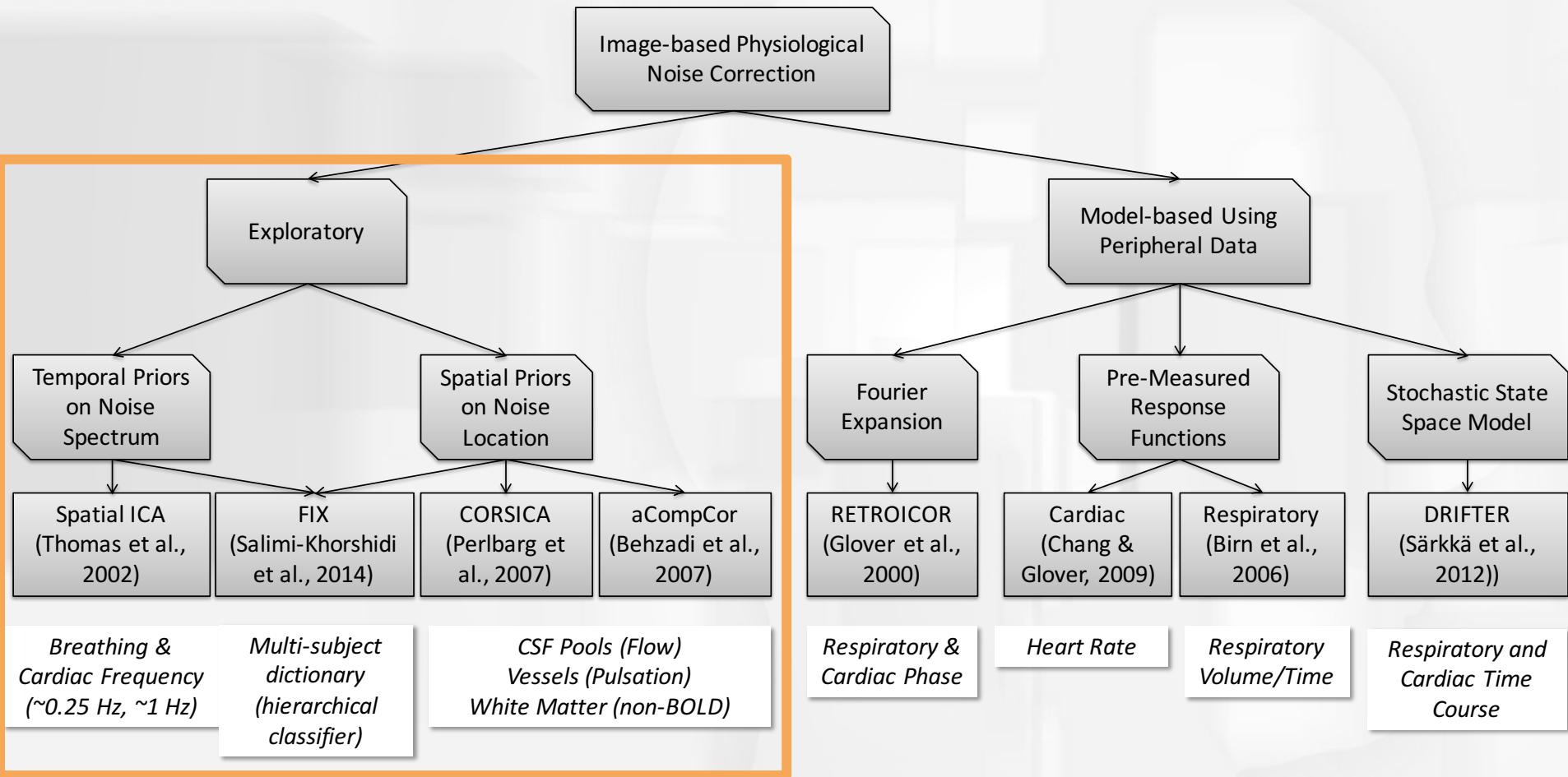


- Assuming convolution of heart rate/respiratory variability time course with unknown response function

$$y = X_r h_r + X_h h_h + \varepsilon$$

*Chang, Cunningham, Glover, 2009*

# Exploratory Phys Noise Correction



# Noise Component Modeling



- Use priors about physiological noise to identify noise components (time series)
  - Spatial Priors: Mechanisms of physiological noise implicate physiological noise in CSF, blood vessels
  - Temporal Priors: Knowledge about typical physiological frequency contents (heart  $\sim 1\text{Hz}$ , breathing 0.2-0.4 Hz)
    - Note that simple filtering is impossible (cf. aliasing)
  - Population Priors: Use dictionary learning from manually labelled training set of subjects (FIX)

# PCA VS ICA

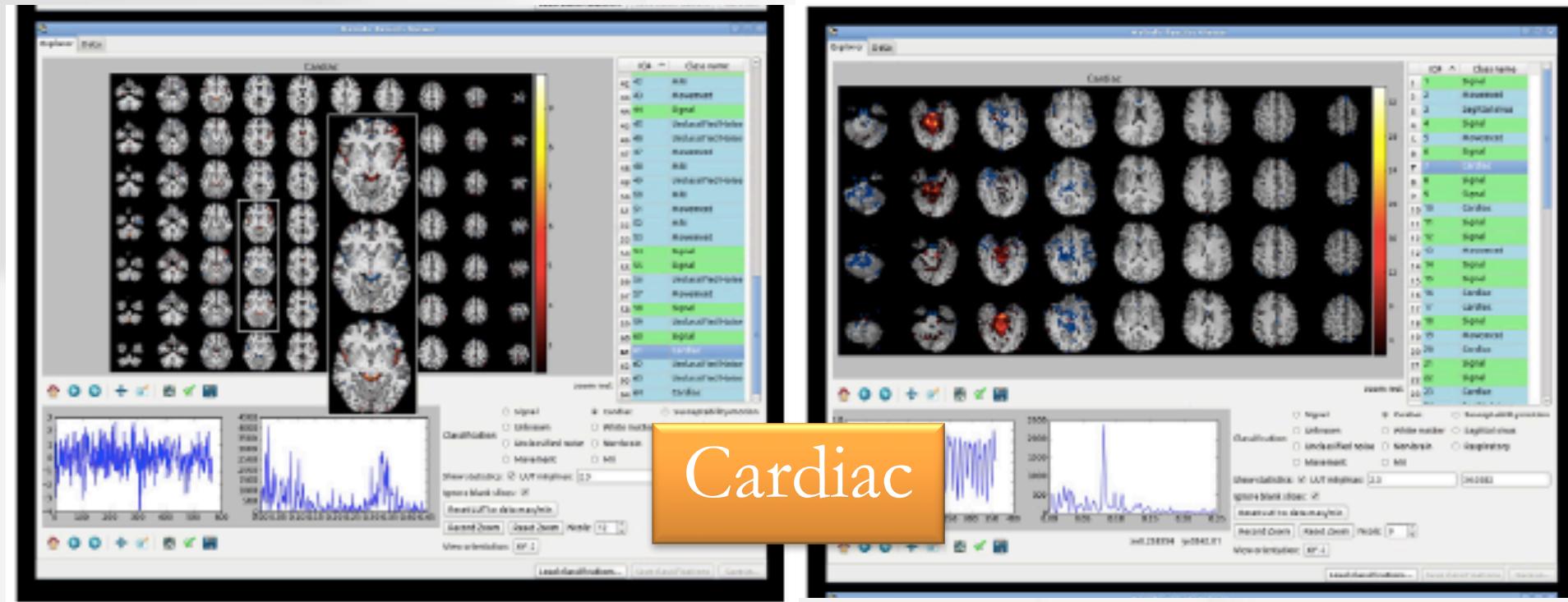


- Methods to extract components (i.e. summarize ROIs/spectra) differ:
  - Maximum variance time series: Principal Component Analysis (PCA) from region of interest (aCompCor, Behzadi 2007)
  - Maximally independent time courses/sites: spatial/temporal ICA, FSL MELODIC, FIX
- aCompCor is basically identical to a seed-based correlation analysis in resting-state fMRI
  - Here: seed is in region-of-no-interest and correlated time series regressed out
  - See resting state analysis for more details

# Preprocessing Techniques



- FSL MELODIC, FIX



# Other Physiological Corrections



- Non-linear models
  - DRIFTER: Kalman Filter, Bayesian, *Joint* Stochastic State-space model of peripheral physiology and BOLD
- Identify noise via task test-retest reproducibility
  - PHYCAA: e.g. via high-freq. autocorrelation, anatomy
  - GLMDenoise: PCA of noise regressors
- MEICA: Multi-Echo ICA
  - Use diff. TE-images to decompose proton density from T2\* changes

Särkkä, *NeuroImage*, 2012

Churchill, *NeuroImage*, 2012/13

Kay, *Front. Neurosci.*, 2013

Olafsson, *NeuroImage*, 2015

# Outline – Noise Correction



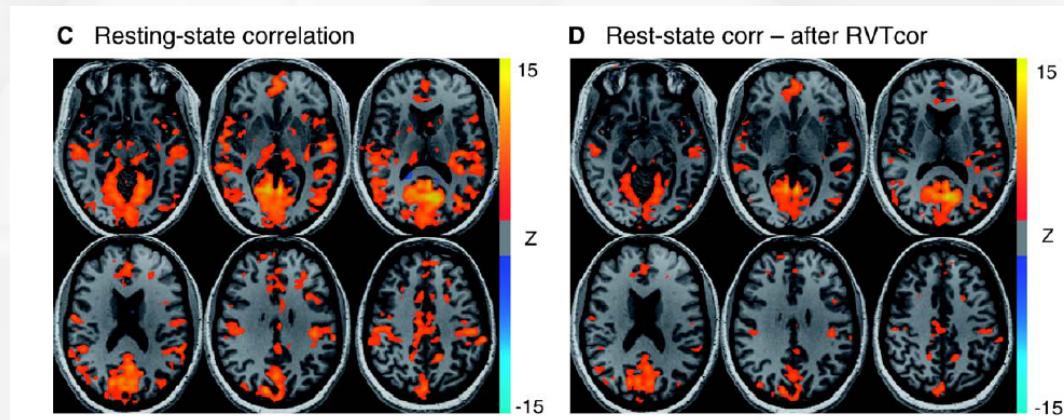
- MRI Time Series Recap and Noise Sources
  - Why de-noising? Structured Noise; Noise Pathways
- Noise Correction Approaches
  - Method: Modeling VS Preprocessing
  - Target: Motion, Cardiac/Breathing Cycle
  - Input: fMRI Data VS Peripheral Measures
- Prospects for Improving Group Statistics
- Limitations
  - Degrees of Freedom; Task-related “noise”; Interoception

# When? – Literature Evidence



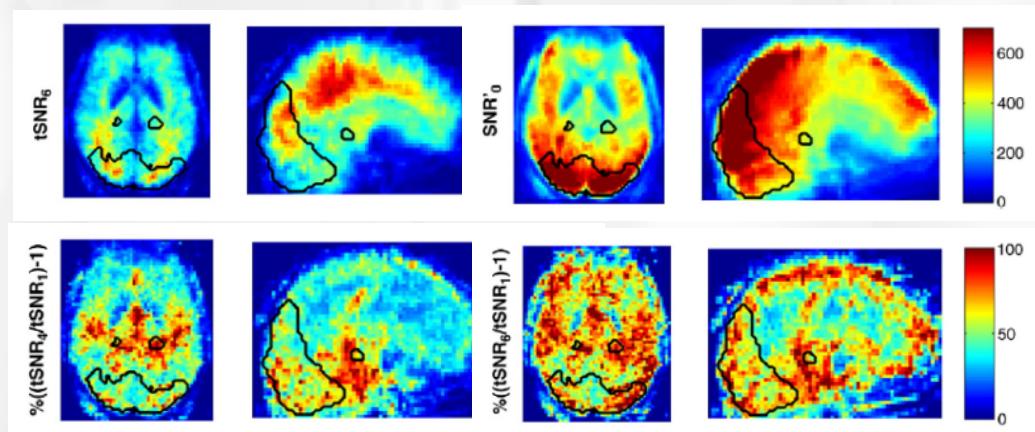
## ■ Resting-state:

- Birn, R. M. "The Role of Physiological Noise in Resting-state Functional Connectivity." *NeuroImage* 62, 2012
- Birn, R. M., et al. "Separating Respiratory-variation-related Fluctuations from Neuronal-activity-related Fluctuations in fMRI." *NeuroImage* 31, 2006



## ■ Task-based:

- Hutton, C., et al. "The Impact of Physiological Noise Correction on fMRI at 7 T." *NeuroImage* 57, 2011:



# All these methods, but...

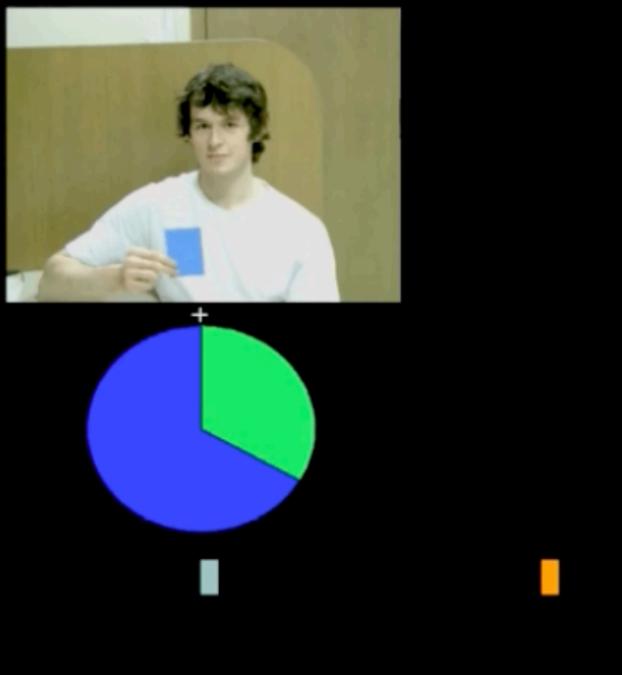


- Physiological noise correction not a default pre-processing step in task-based fMRI
- Reasons
  - Impact on group level fMRI
    - no reports for non-trivial paradigms
  - Existing Toolboxes lack...
    - robust, automatic implementation
    - dealing with variable peripheral data quality

# Paradigm: Learning from Advice



- Hierarchical learning of trustworthiness of advisor over time
- Contrasts: Prediction and Prediction Error about advice



recommendations of adviser were **veridical** (pre-recorded videos from behavioural study)

**volatility of advice** (changing intentions of adviser through incentive structure)

interactive, gender-matched (**40** male subjects)

**fMRI design:** Philips Achieva 3T  
TR/TE 2500/36ms, 2 x 2 x 3 mm<sup>3</sup>

*Diaconescu et al, 2014, PLoS Comp. Biol.*

# Group Level Impact PhysIO

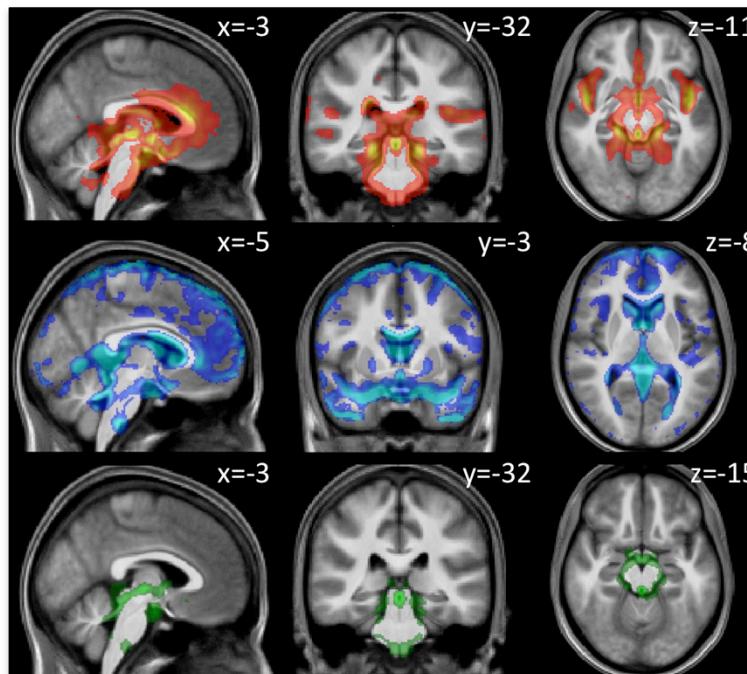


- Andreea Diaconescu (TNU): Social Learning Experiment 2012-2014, (N=35)
- F-contrast: Where does physiological noise model explain significant variance?

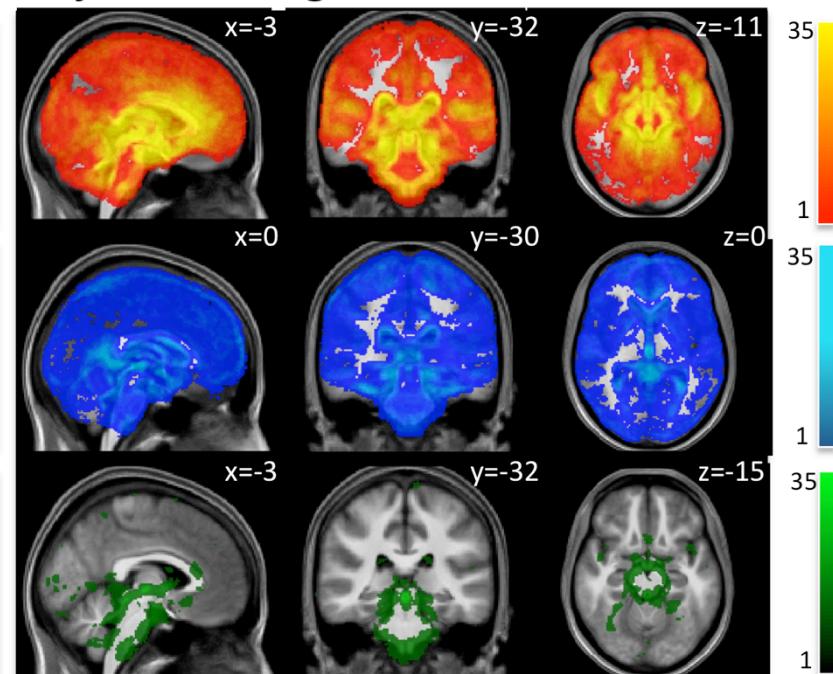
A

Cardiac  
Regressors

2nd-level F-Contrasts



Subjects with Significant Noise Reduction



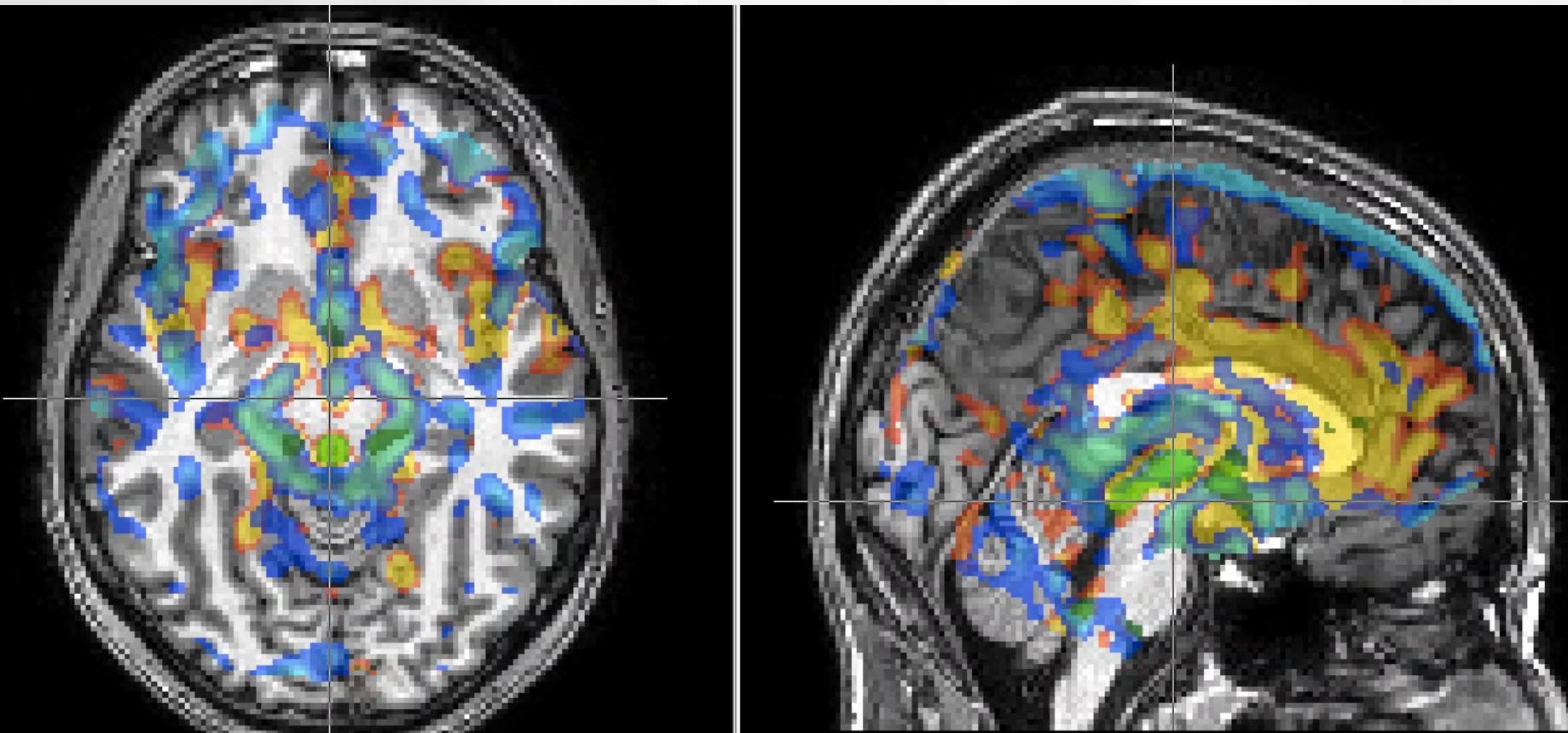
Respiratory  
Regressors

Interaction  
Regressors  
(Cardiac X  
Respiration)

# Relevance for Neuromodulation



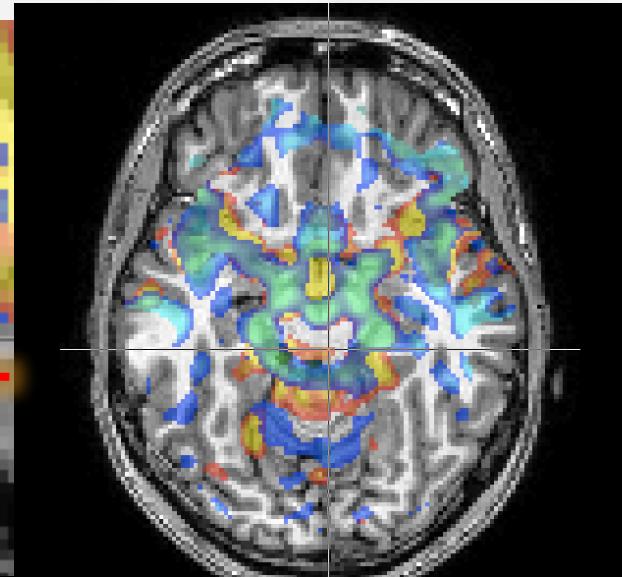
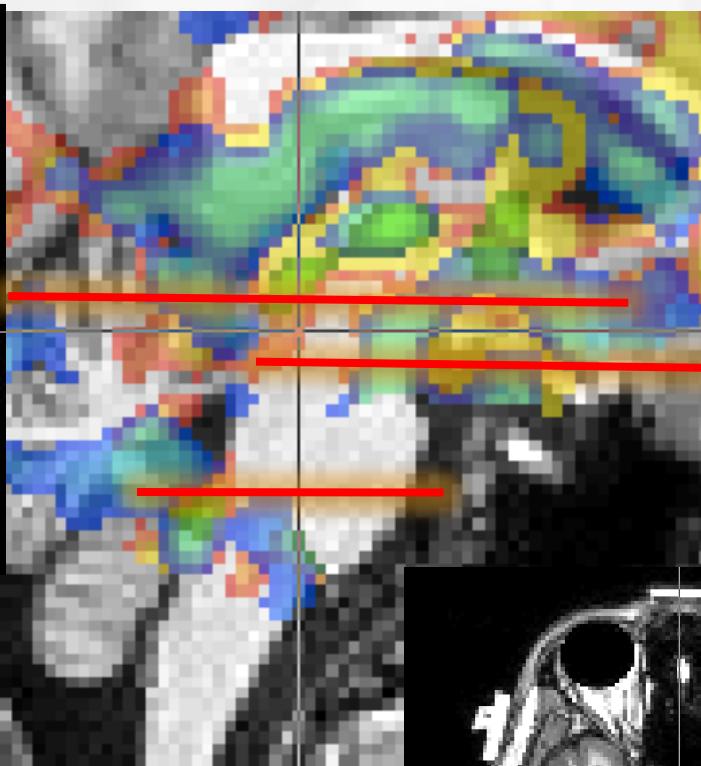
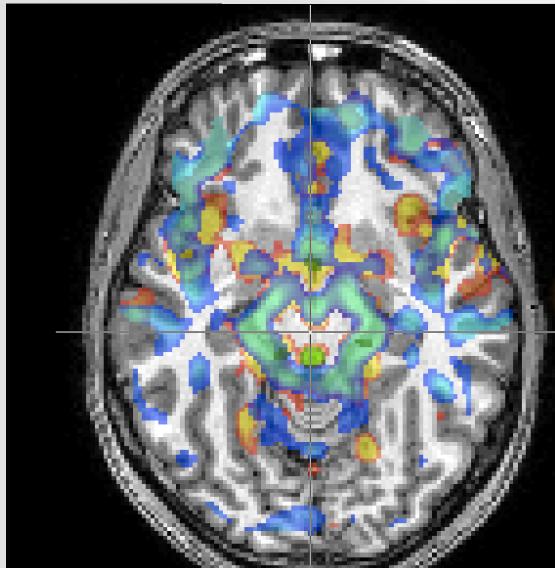
- cardiac (red), respiratory (blue), cardXresp (green)



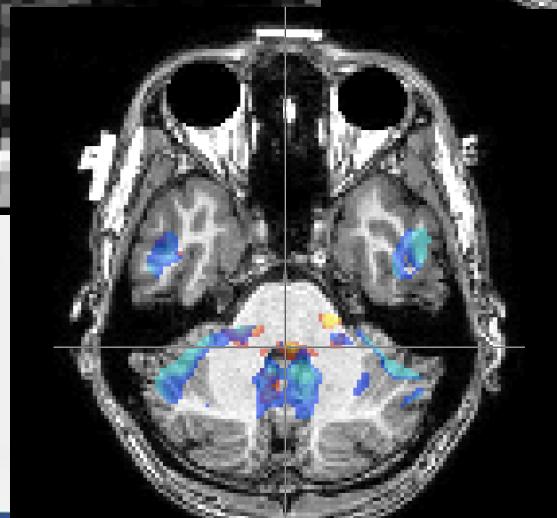
# Relevance for Neuromodulation



- VTA (DA)



- Raphe Nuclei (5-HT)

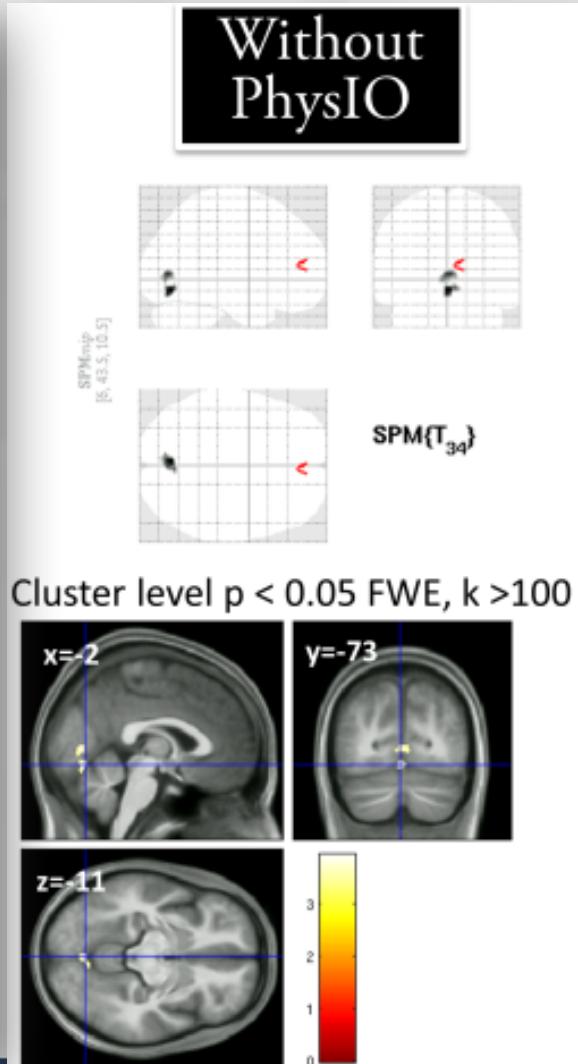
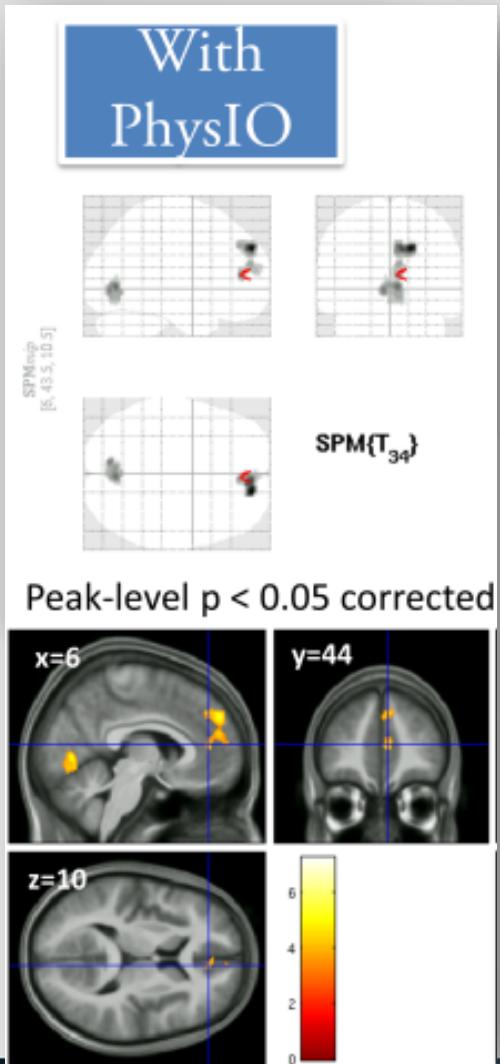


- Locus coeruleus (NA)

# Effects on Group Contrasts

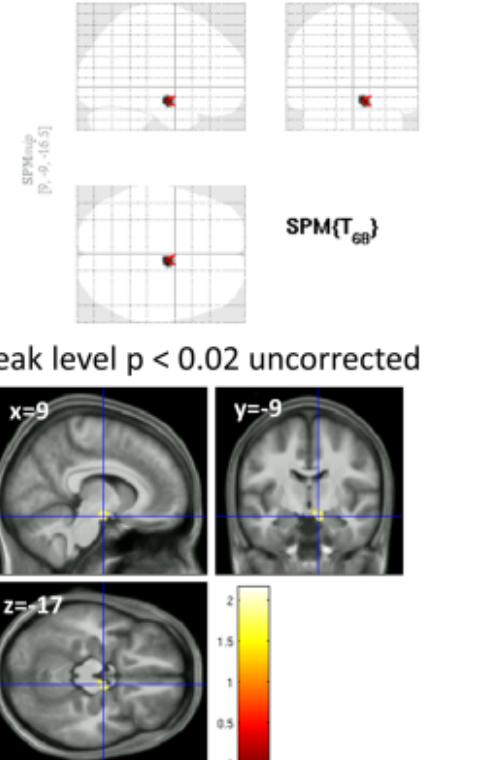


## Higher Sensitivity



## False Positives

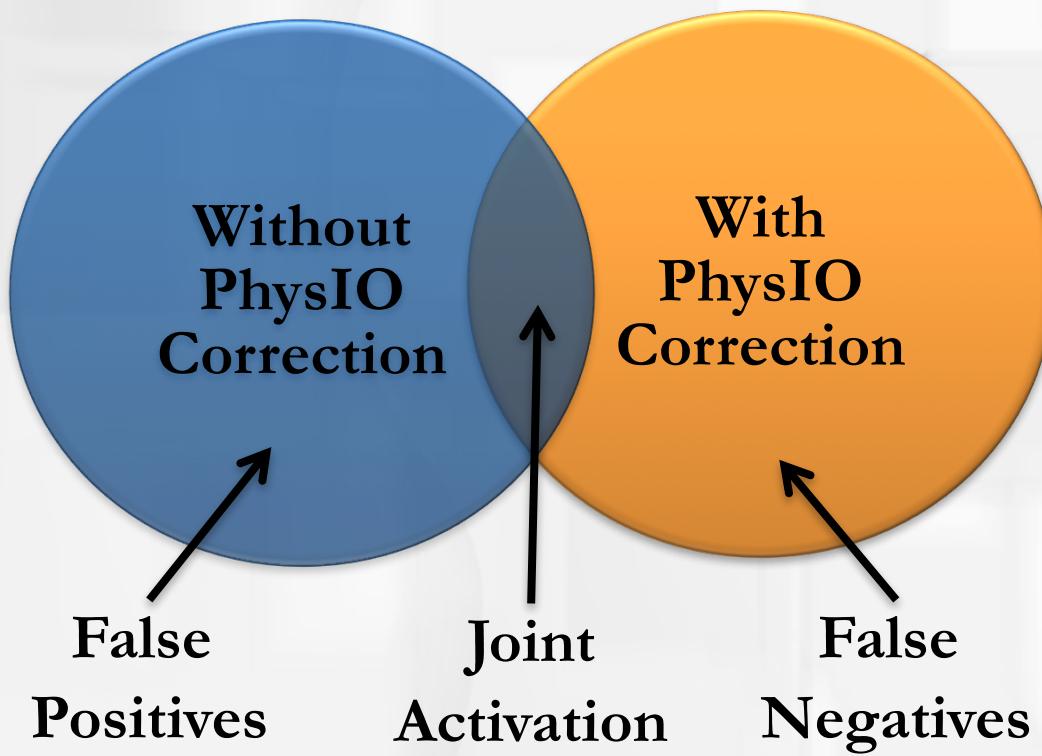
NoPhysIO > PhysIO



# Venn-Diagramme Cluster Analysis



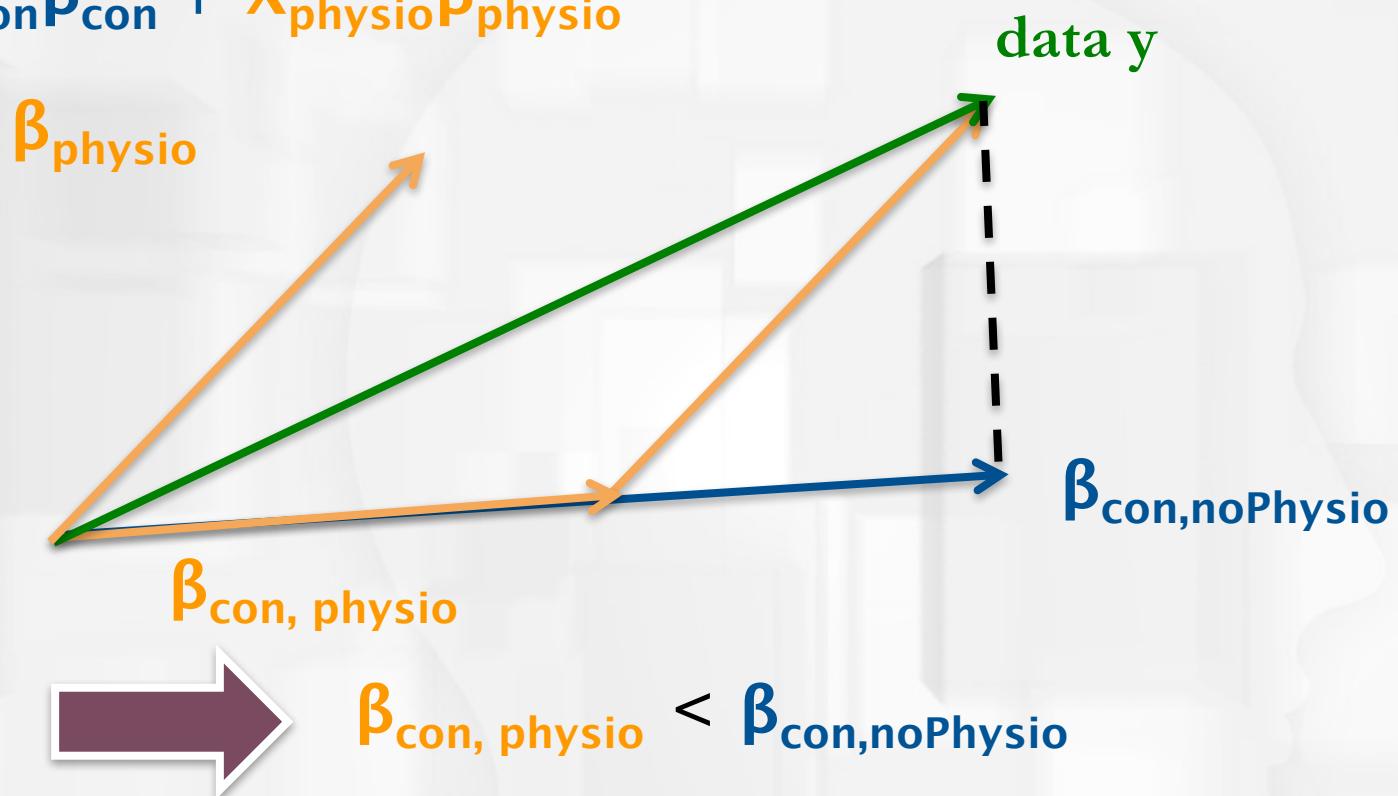
## Significant Clusters



# Noise modeling impact on task?



$$y = X_{\text{con}}\beta_{\text{con}} + X_{\text{physio}}\beta_{\text{physio}}$$



- Phys noise correction can change parameter estimates for regressors of interest (correlation!)
- Thereby change distribution of  $\beta$   $\Rightarrow$  Mean? Variance?

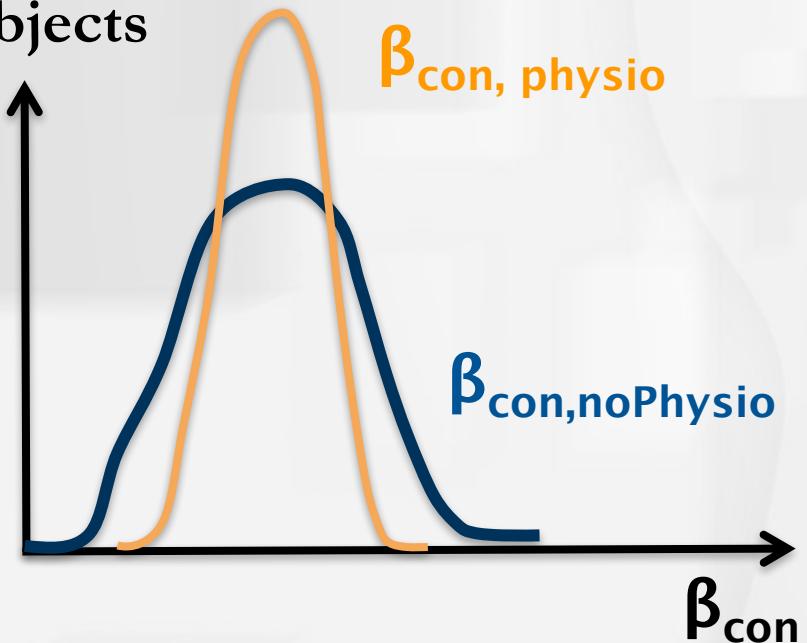
# Group Effect: Correlated Regressors



- Two mechanisms imaginable

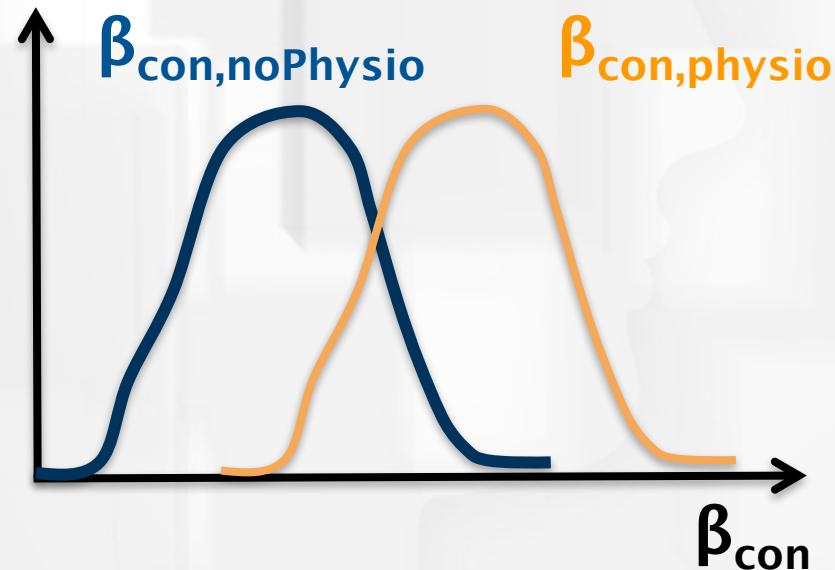
Reduced inter-subject variance

frequency of subjects



Increased inter-subject mean estimates

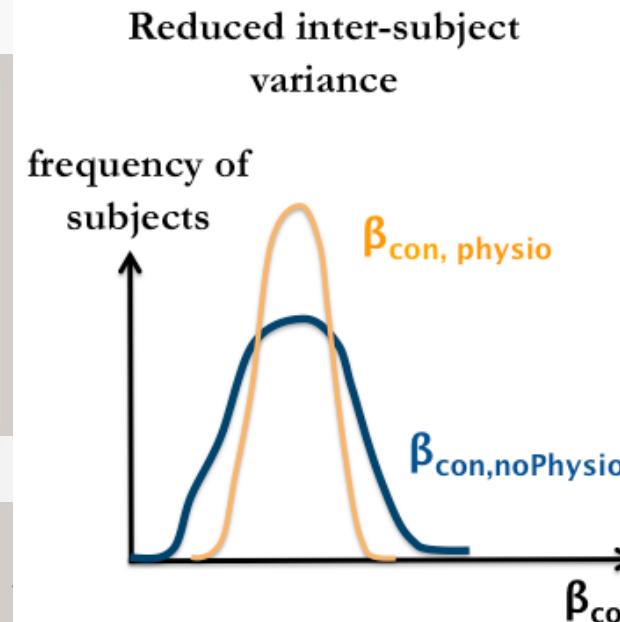
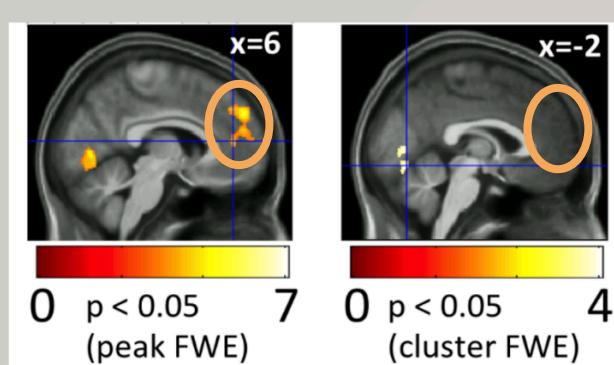
frequency of subjects



# The Corrective Mechanism

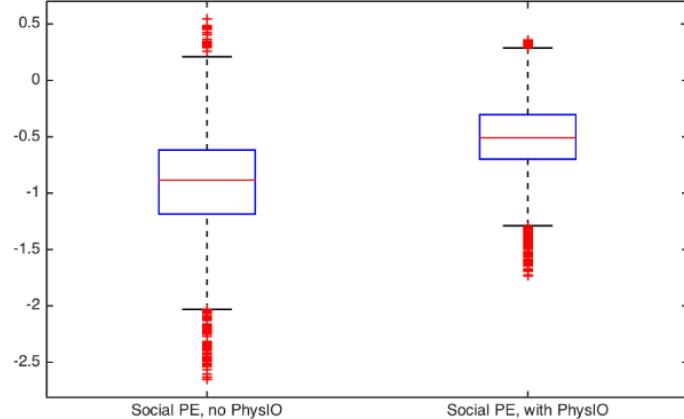


## Social Pred. Error

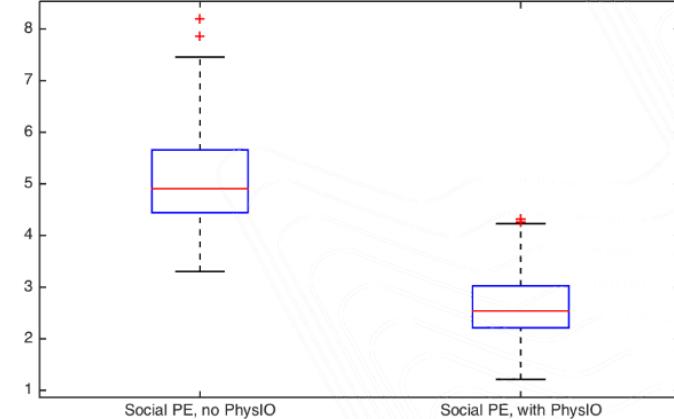


## Mean

Mean Beta (over Subjects) distribution of voxels within ROI



Standard Deviation Beta (over Subjects) distribution of voxels within ROI



# Outline – Noise Correction



- MRI Time Series Recap and Noise Sources
  - Why de-noising? Structured Noise; Noise Pathways
- Noise Correction Approaches
  - Method: Modeling VS Preprocessing
  - Target: Motion, Cardiac/Breathing Cycle
  - Input: fMRI Data VS Peripheral Measures
- Prospects for Improving Group Statistics
- **Limitations**
  - Degrees of Freedom; Task-related “noise”; Interoception

# Limitations of Noise Modeling



- Degrees of freedom, sensitivity reduced by too many ineffective regressors
  - F-test informative
- Intrinsic correlations of functional areas of interoception and peripheral physiology
  - E.g. Amygdala, Insula, ACC
  - Controversial reading:  
[fMRI of the Amygdala: All In Vein? – Neuroskeptic](#)
- Alternative: Masking, Pure anatomical priors removing CSF, angiography (vessels)

# Conclusion



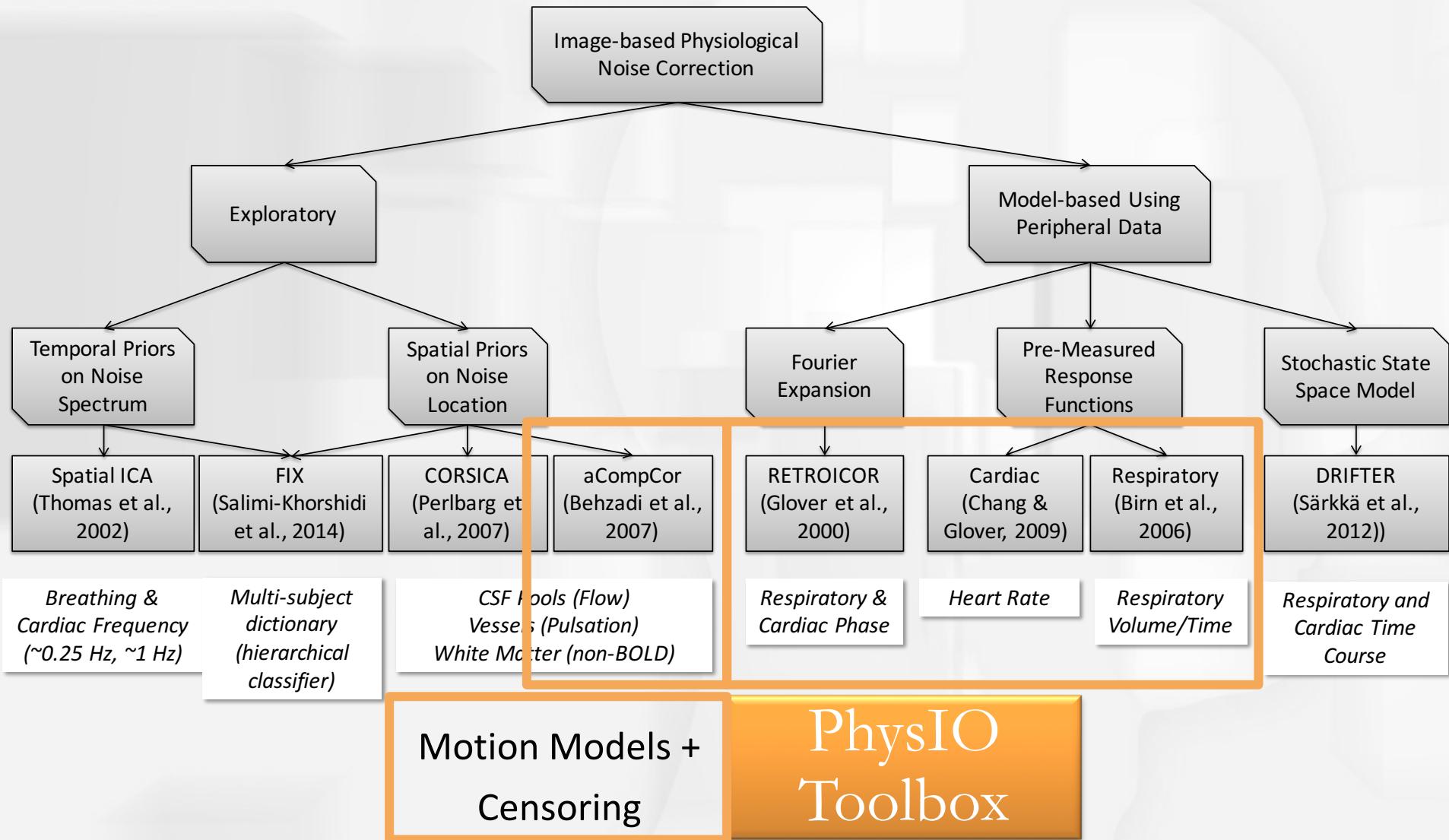
- MRI Time Series and Physiological Noise
- Model-based Correction
- Noise Modeling Prospects:  
Group FX
- The PhysIO Toolbox
- Structured noise through cardiac/resp cycle (70%)
- Within the GLM, Nuisance regressors from Fourier expansion, response functions
- Increase group sensitivity (lower inter-subject variability), fewer false positives
- Correction in SPM/Matlab in practice => **NOW!**

# Practical Session



- **Demo: The PhysIO Toolbox for Physiological Noise Correction in fMRI**
  - Features and Workflow
  - Image-based physiological noise correction in the GLM
    - RETROICOR, HRV, RVT
    - Noise-ROIs
  - Practical Demo (SPM Batch)
    - Estimating different Models
    - Understanding the Preprocessing Plots
    - Automatic Model Assessment, Diagnostics on Contrast

# Image-based Noise Correction

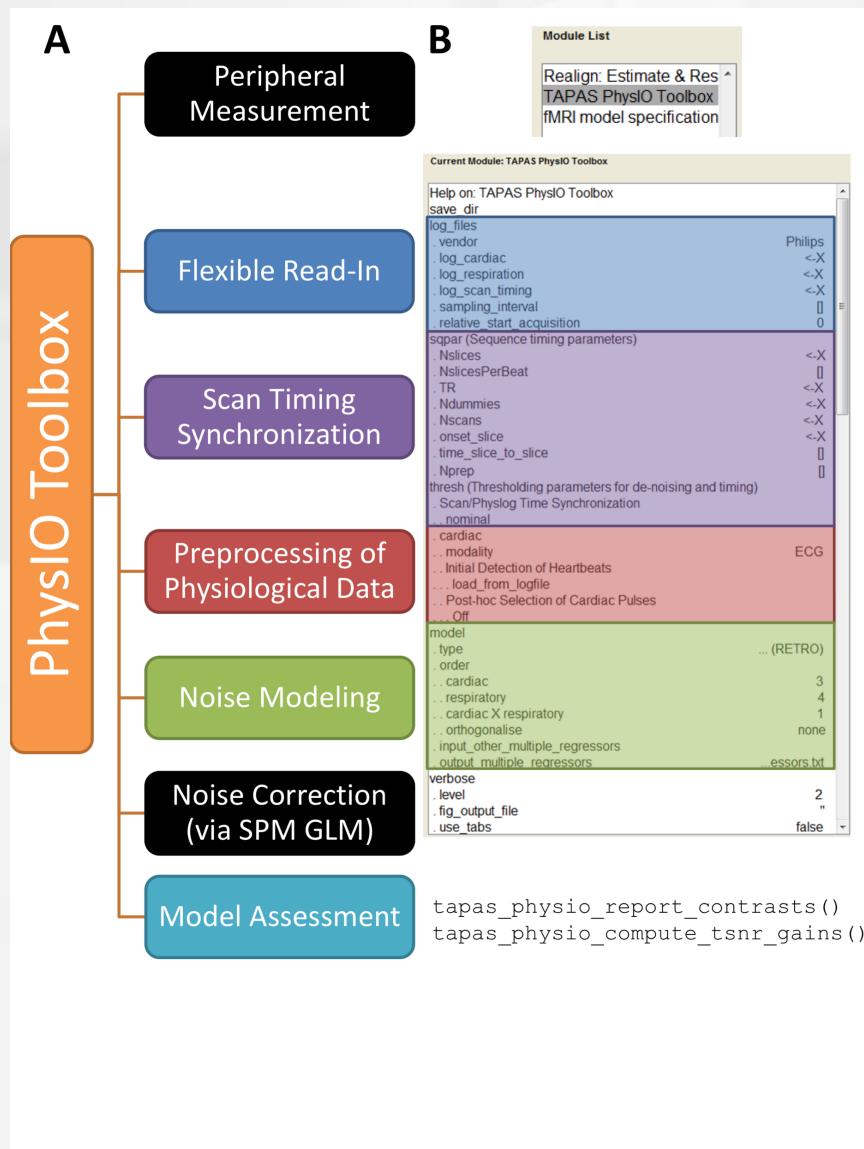


# The PhysIO Toolbox

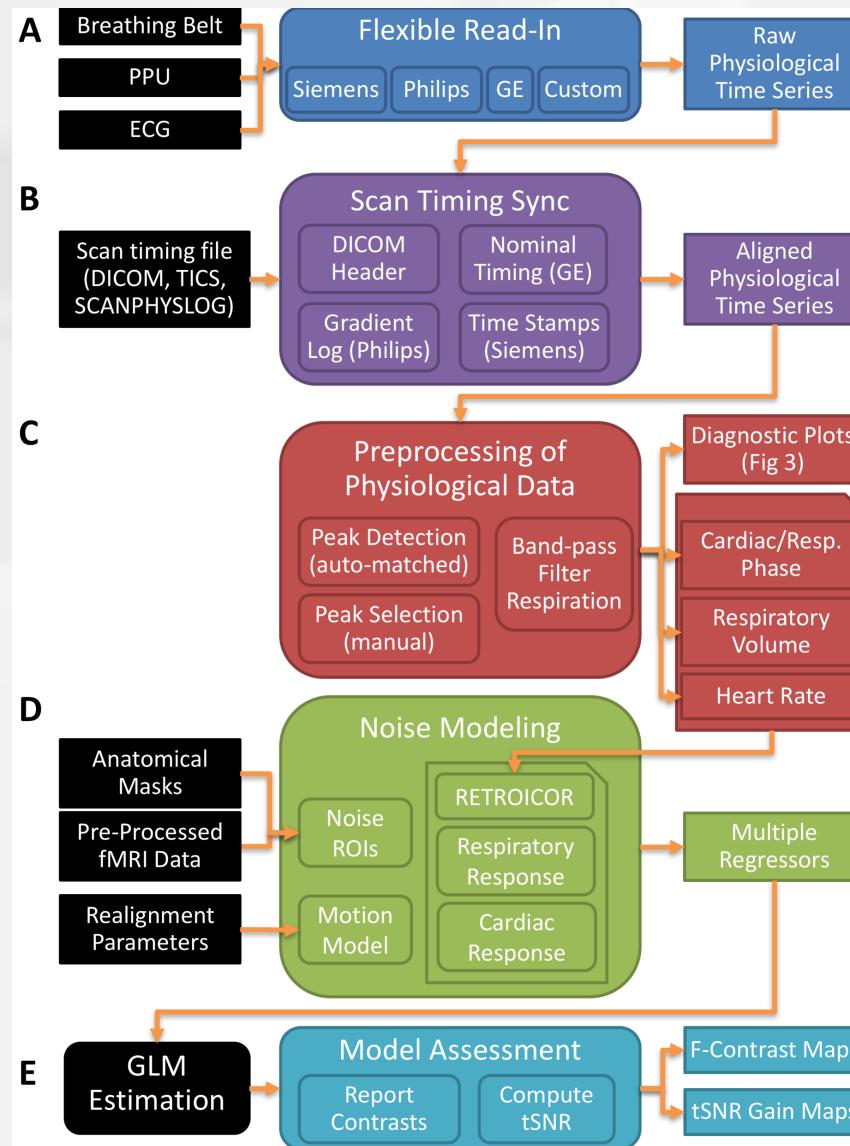


- Developed at the Translational Neuromodeling Unit (TNU) since 2008
  - Lead programmer: Lars Kasper (TNU)
  - Contributors: Jakob Heinze (TNU), Steffen Bollmann (KiSpi Zurich)
- Part of the TNU «TAPAS» software suite
- Used at the TNU, in Zurich and beyond by ~50 researchers
  - Iglesias 2013, Neuron; Kasper 2014, NeuroImage; Bollmann 2014, PhDThesis; Sulzer 2013, NeuroImage; Hauser 2014, NeuroImage; Grueschow 2015, Neuron
- Download & Example Data:
  - <https://translationalneuromodeling.org/tapas>
  - <https://www.tnu.ethz.ch/en/software/tapas/data.html>

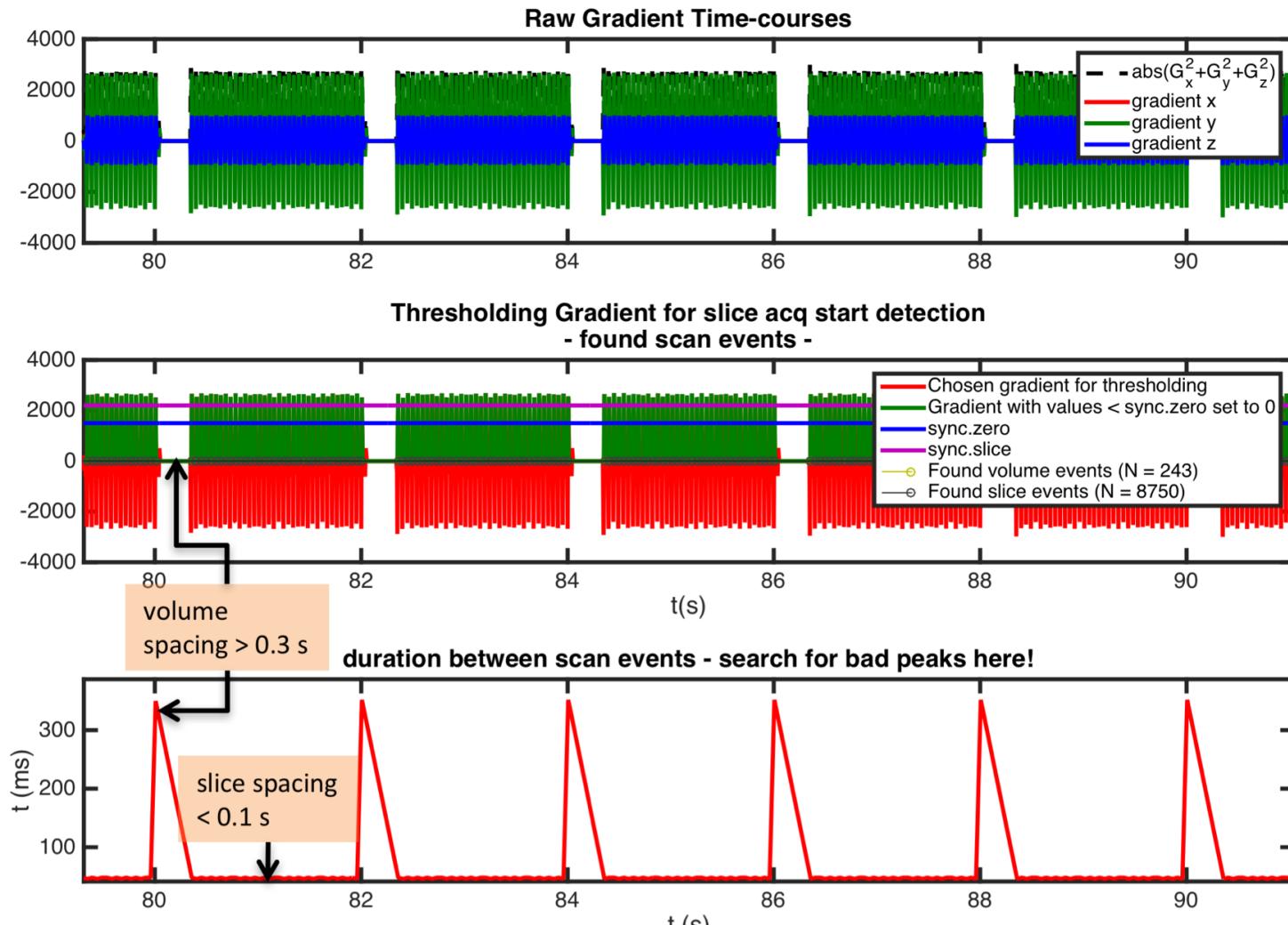
# Workflow of the PhysIO Toolbox



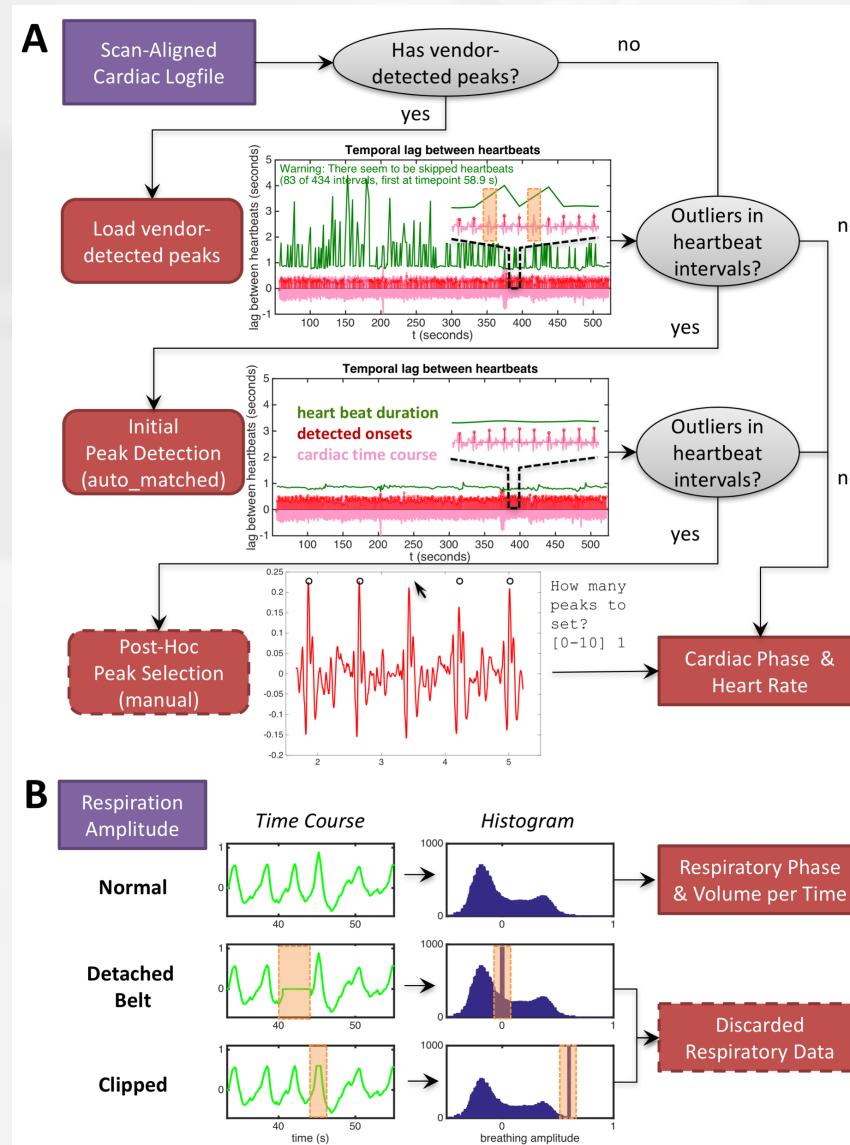
# Flowchart of Noise Correction



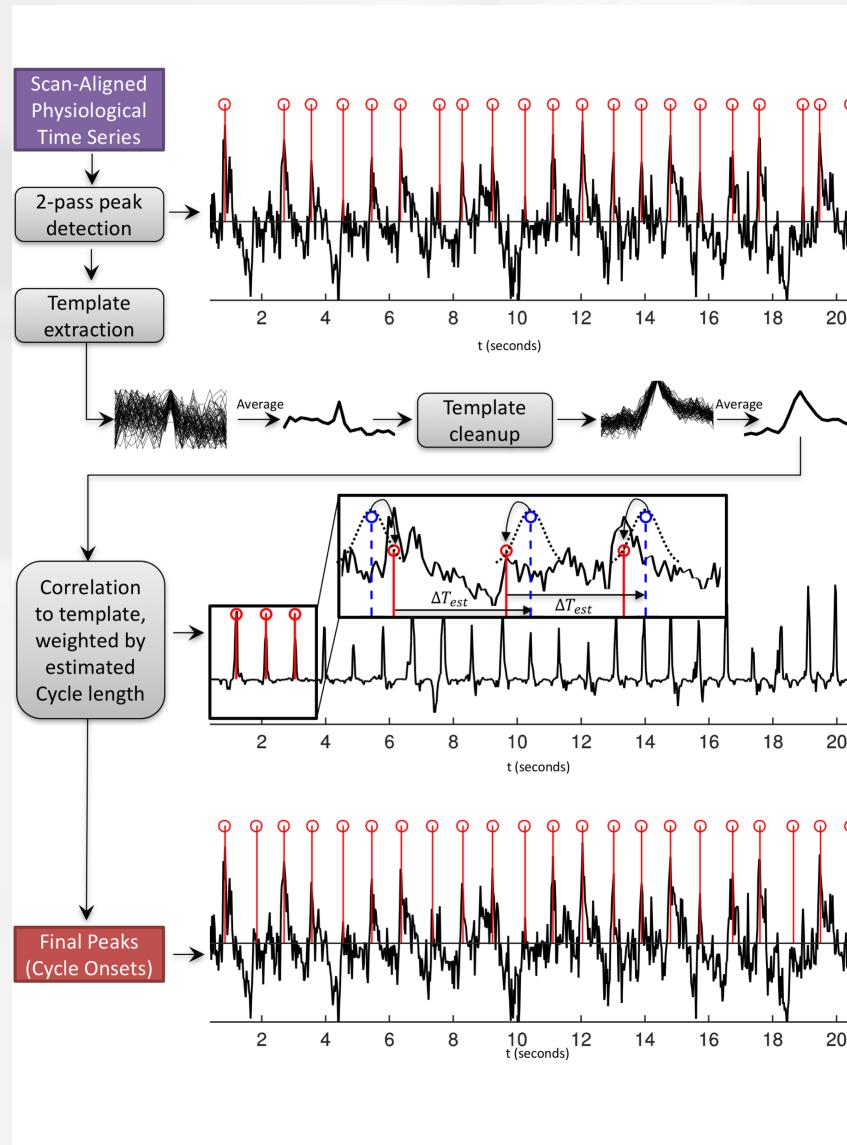
# Scan Sync with Philips Gradients



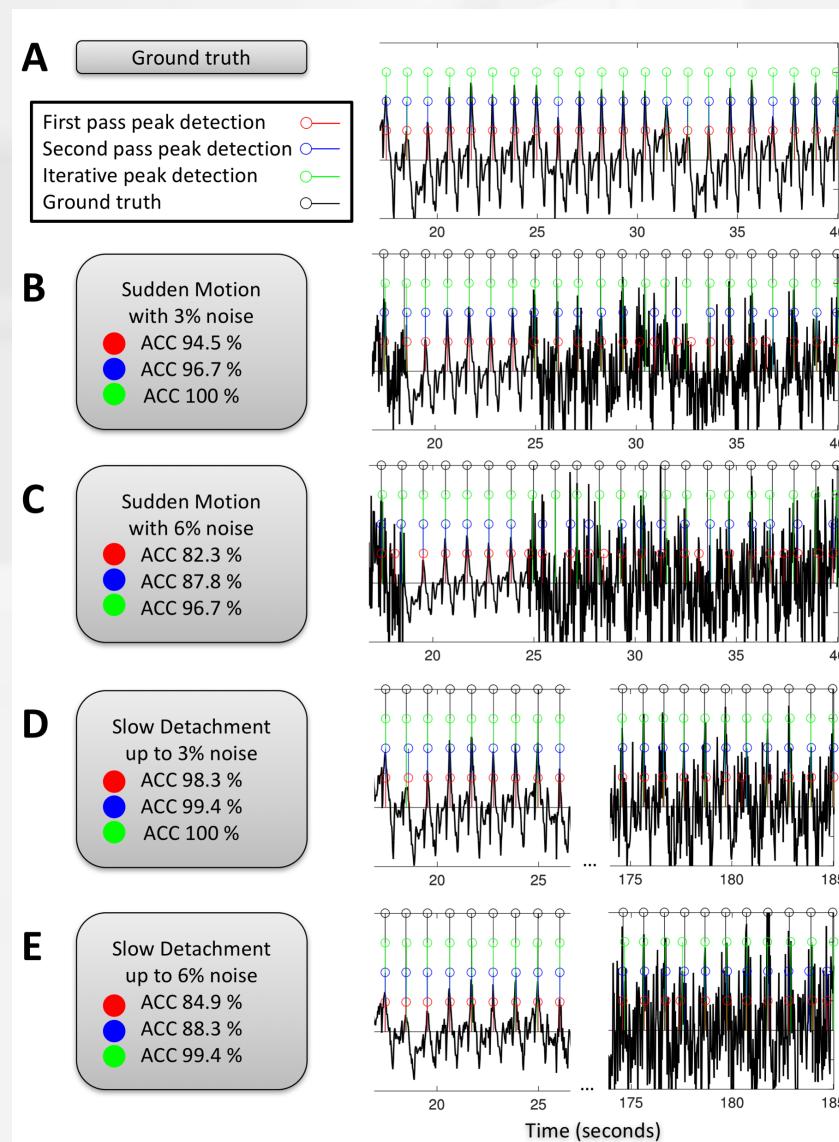
# Data Preprocessing Overview



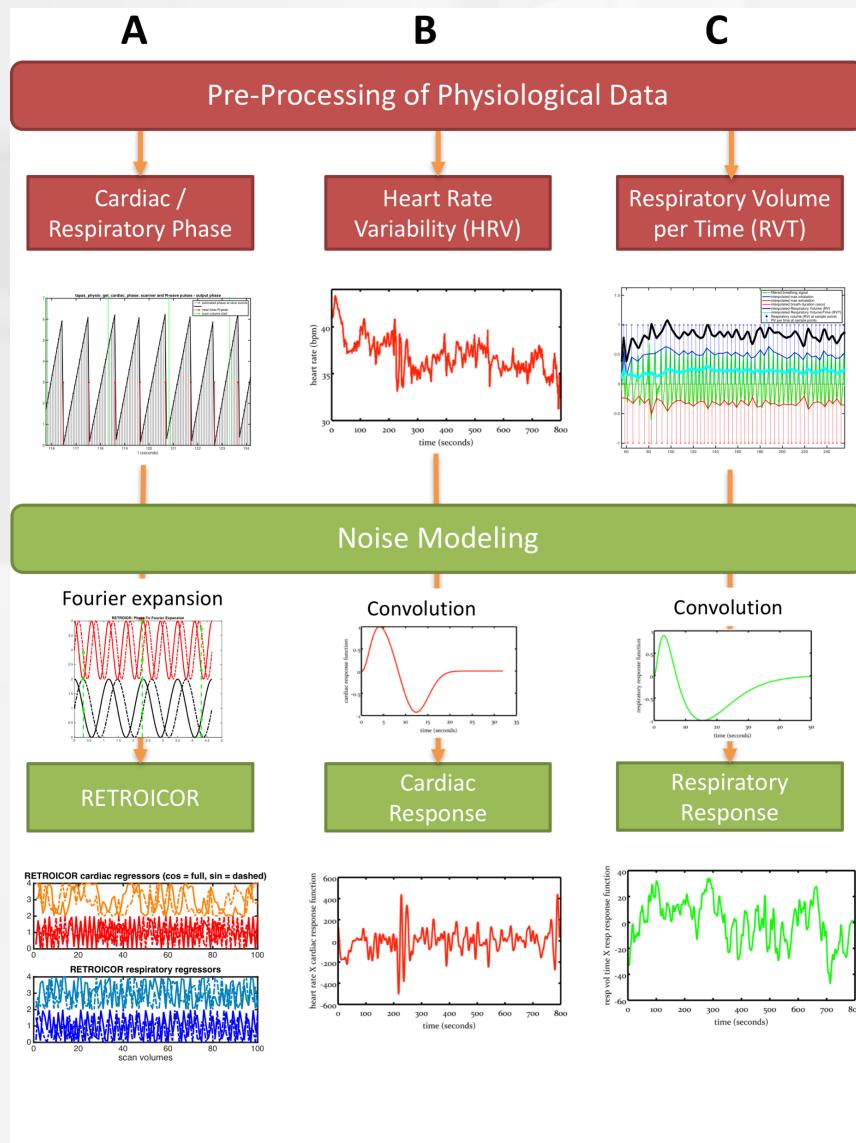
# Preprocessing: Peak Detection



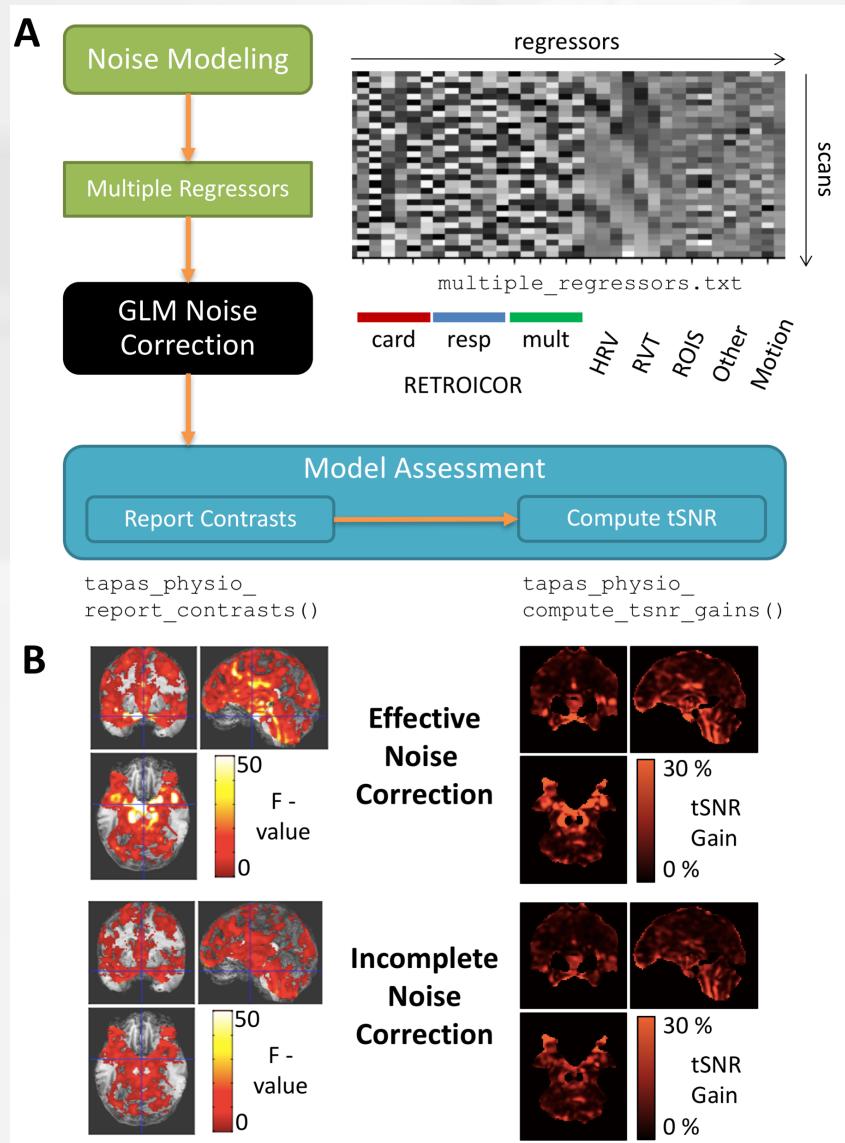
# Peak Detection: Robustness



# Noise Modeling



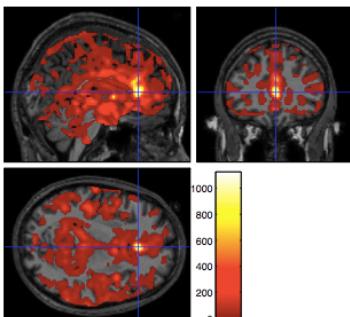
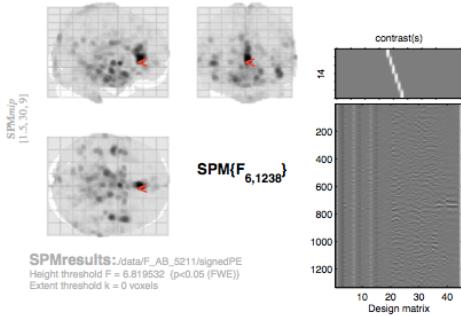
# Diagnostics: Model Assessment



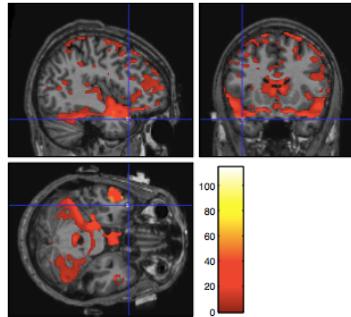
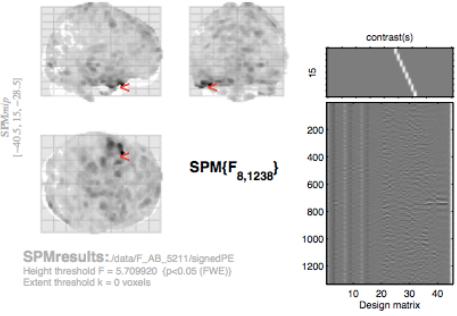
# Model Check: SPM F-contrasts



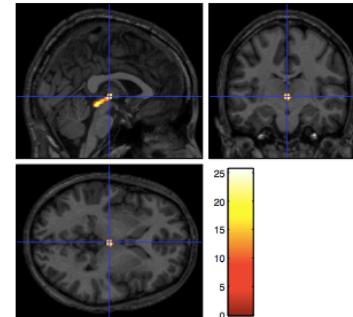
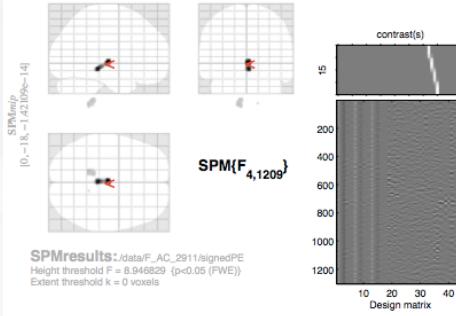
## Cardiac regressors



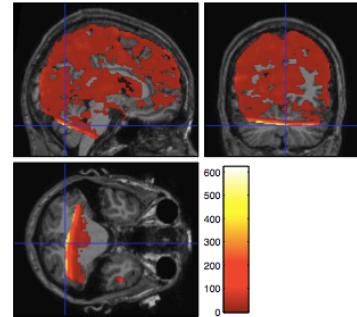
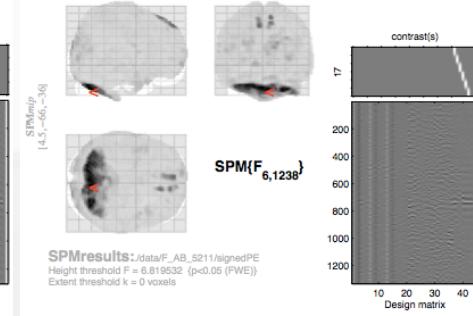
## Respiratory regressors



## Cardiac x Respiratory



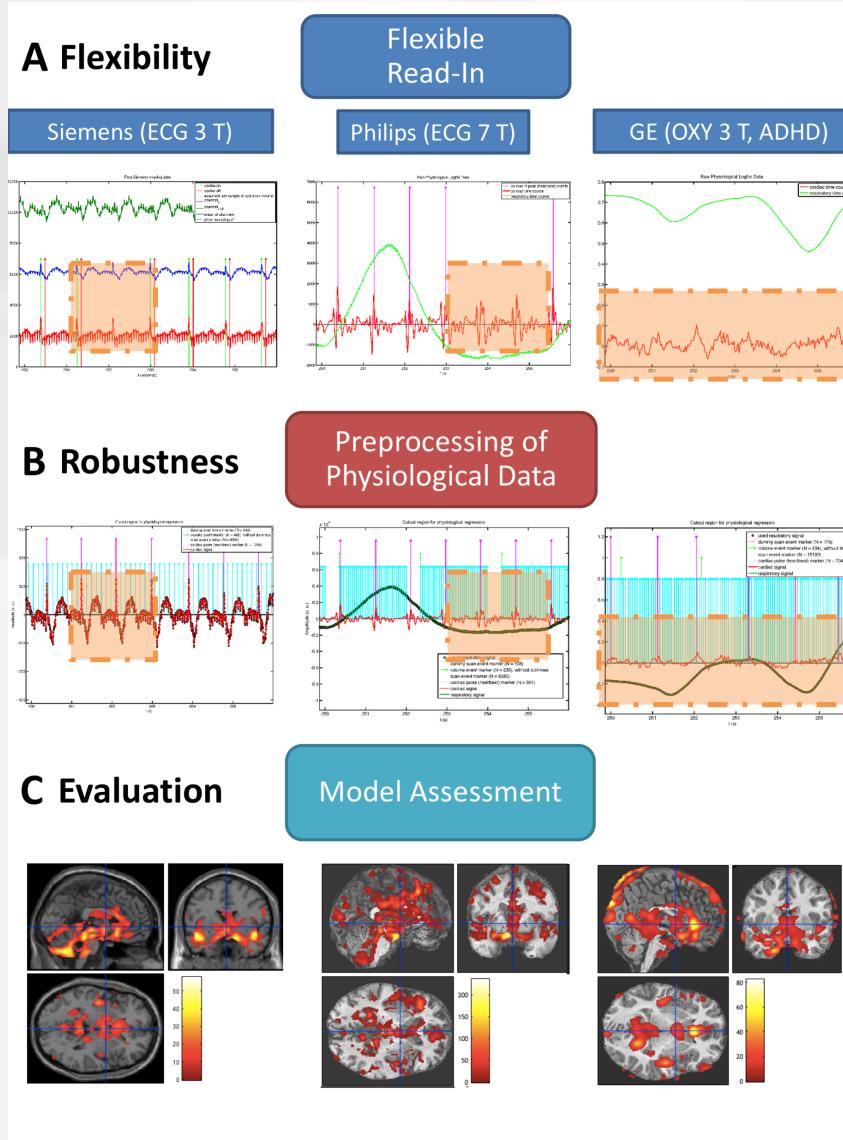
## Movement regressors



Finally:

- Check Influence of Physiological Noise (Correction) on Data
- SPM
  - F-contrast on 1st and second level

# Flexibility: Scanner vendors

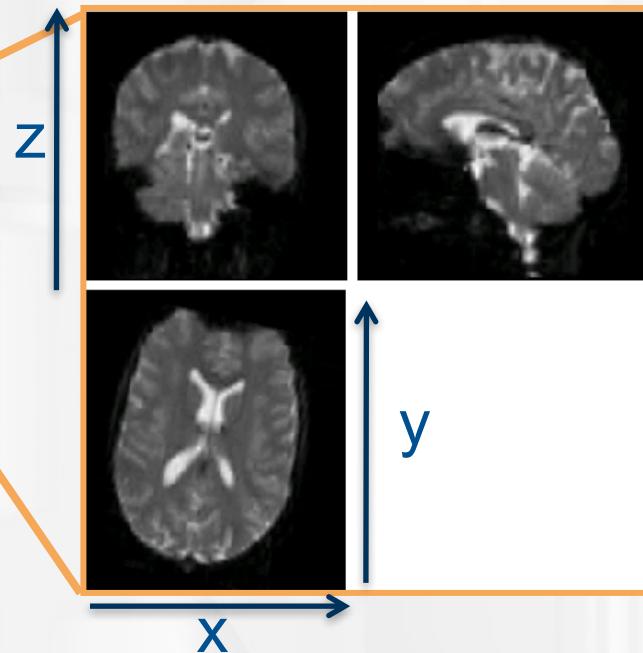




# References

- **Birn**, Rasmus M., Jason B. Diamond, Monica A. Smith, and Peter A. Bandettini. 2006. “Separating Respiratory-variation-related Fluctuations from Neuronal-activity-related Fluctuations in fMRI.” *NeuroImage* 31 (4) (July 15): 1536–1548. doi:10.1016/j.neuroimage.2006.02.048.
- **Glover**, G H, T Q Li, and D Ress. 2000. “Image-based Method for Retrospective Correction of Physiological Motion Effects in fMRI: RETROICOR.” *Magnetic Resonance in Medicine: Official Journal of the Society of Magnetic Resonance in Medicine / Society of Magnetic Resonance in Medicine* 44 (1) (July): 162–7.
- **Harvey**, Ann K., Kyle T.S. Pattinson, Jonathan C.W. Brooks, Stephen D. Mayhew, Mark Jenkinson, and Richard G. Wise. 2008. “Brainstem Functional Magnetic Resonance Imaging: Disentangling Signal from Physiological Noise.” *Journal of Magnetic Resonance Imaging* 28 (6): 1337–1344. doi:10.1002/jmri.21623.
- **Hutton**, C., O. Josephs, J. Stadler, E. Featherstone, A. Reid, O. Speck, J. Bernarding, and N. Weiskopf. 2011. “The Impact of Physiological Noise Correction on fMRI at 7 T.” *NeuroImage* 57 (1) (July 1): 101–112. doi:10.1016/j.neuroimage.2011.04.018.
- **Josephs**, O., Howseman, A.M., Friston, K., Turner, R., 1997. “Physiological noise modelling for multi-slice EPI fMRI using SPM.” Proceedings of the 5th Annual Meeting of ISMRM, Vancouver, Canada, p. 1682
- **Kasper, L.**, Bollmann, S., Diaconescu, A.O., Hutton, C., Heinze, J., Iglesias, S., Hauser, T.U., Sebold, M., Manjaly, Z.-M., Pruessmann, K.P., Stephan, K.E., 2017. The PhysIO Toolbox for Modeling Physiological Noise in fMRI Data. *Journal of Neuroscience Methods* 276, 56–72. doi:10.1016/j.jneumeth.2016.10.019

# fMRI = Acquiring Movies



- ...of three-dimensional Blood Oxygen-Level Dependent (BOLD) contrast images

- Run/Session:  
Time Series of  
Images

