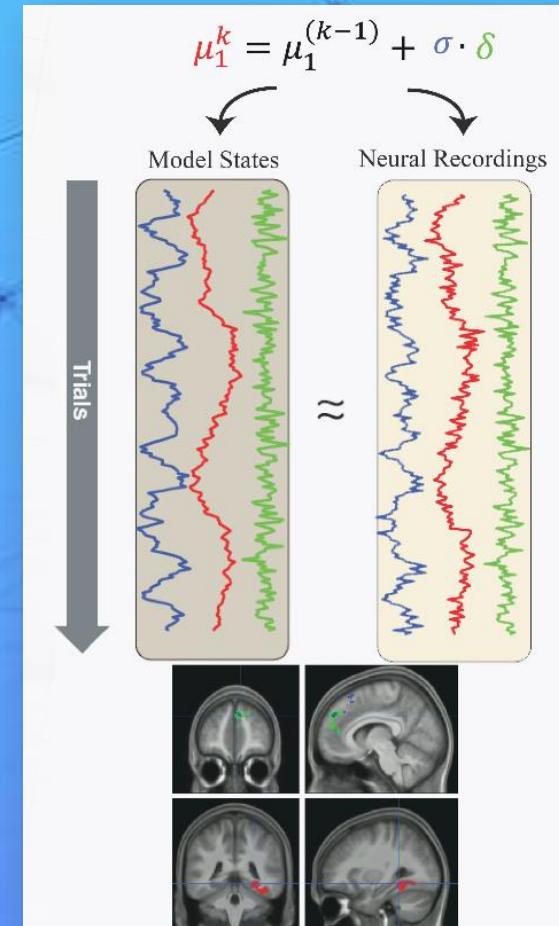




Computational Neuroimaging

Andreea Diaconescu

Methods & Models 2017



What is it all about?

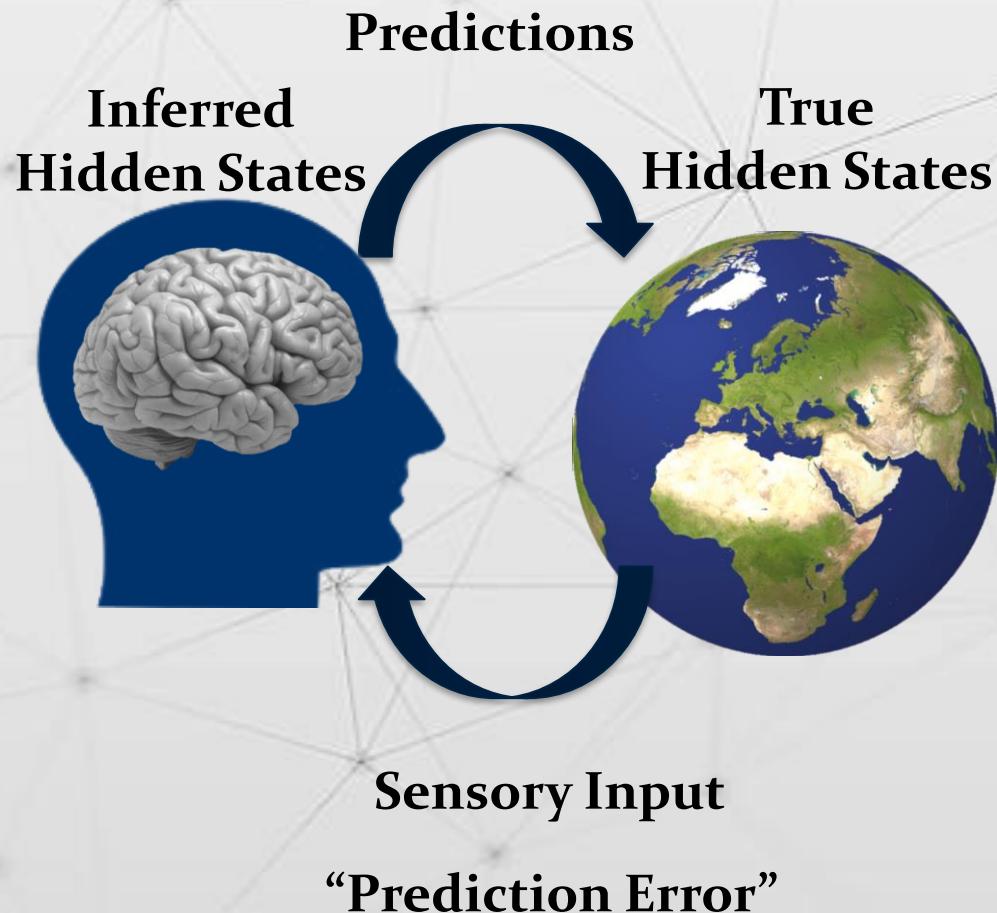


- Why do we use functional magnetic resonance imaging?
 - To measure brain activity
- When does the brain become active?
 - When it learns
 - i.e., when its predictions have to be adjusted
- Where do these predictions come from?
 - A model

How to build a model



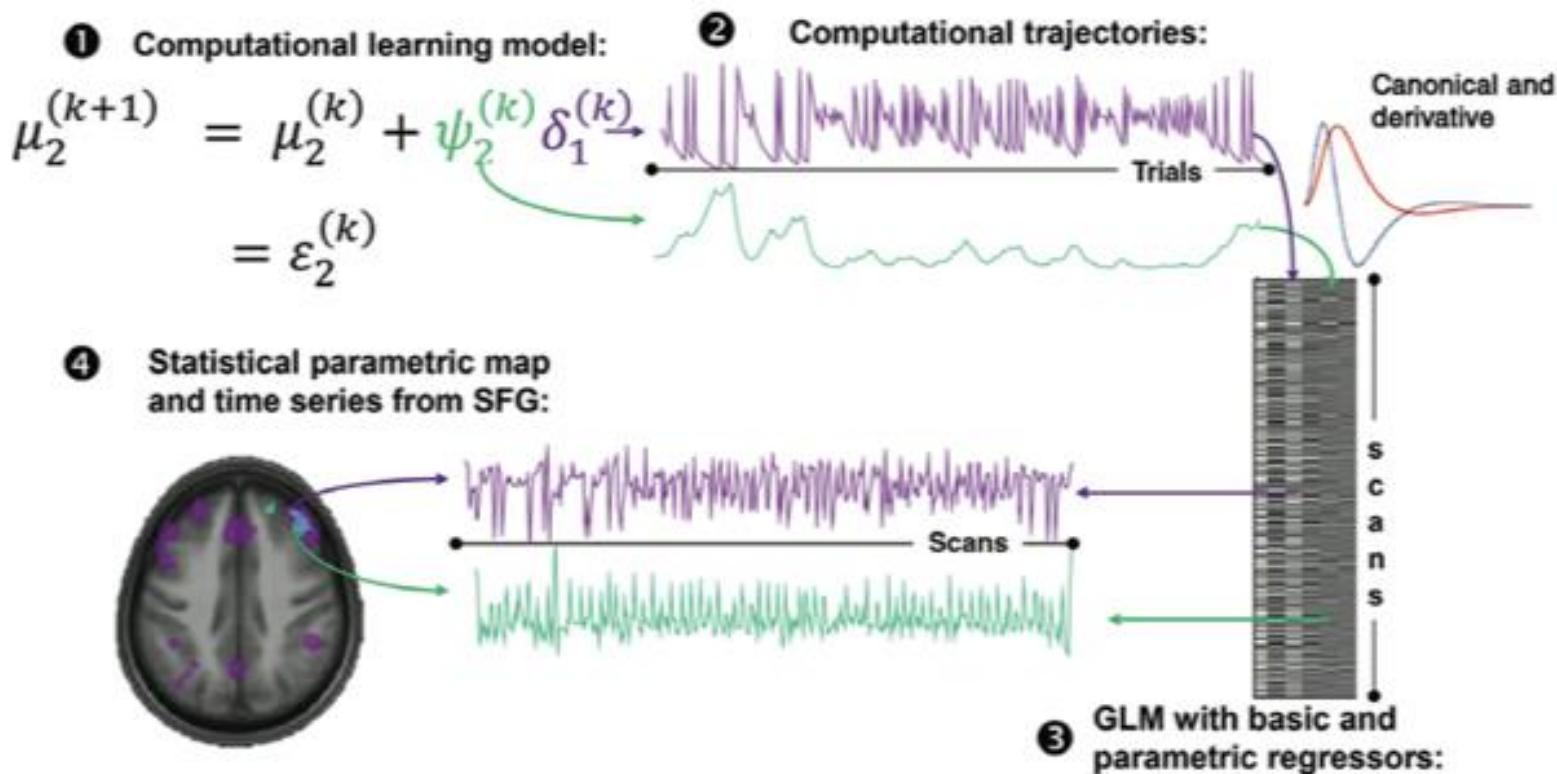
Translational Neuromodeling Unit



Computational Neuroimaging



Translational Neuromodeling Unit



Iglesias et al., 2016

Advantages of computational neuroimaging

- Computational neuroimaging permits us to:
 - **Infer** the computational mechanisms underlying brain function
 - **Localize** such mechanisms
 - **Compare** different models

Explanatory Gap



Translational Neuromodeling Unit



Biological

- Molecular
- Neurochemical



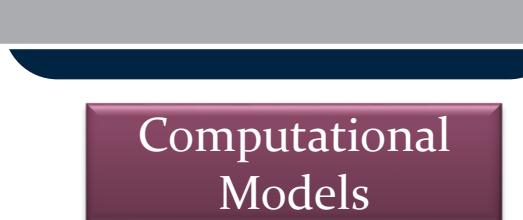
Cognitive

- Computational
- “cognitive/
- computational phenotyping”



Phenomenological

- Performance Accuracy
- Reaction Time
- Choices, preferences



Three Levels of Inference

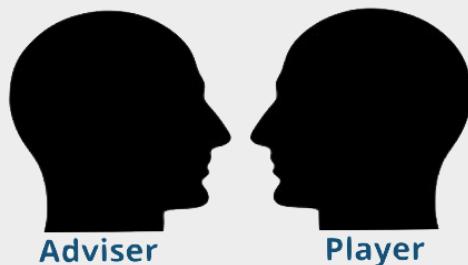
- *Computational Level:* predictions, prediction errors
- *Algorithmic Level:* reinforcement learning, hierarchical Bayesian inference, predictive coding
- *Implementational Level:* Brain activity, neuromodulation



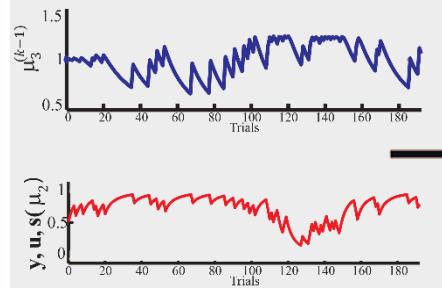
David Marr, 1982

■ 3 ingredients:

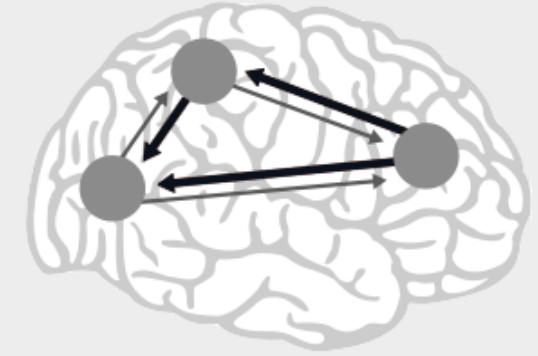
1. Experimental paradigm:



2. Computational model of learning:



3. Model-based fMRI analysis:



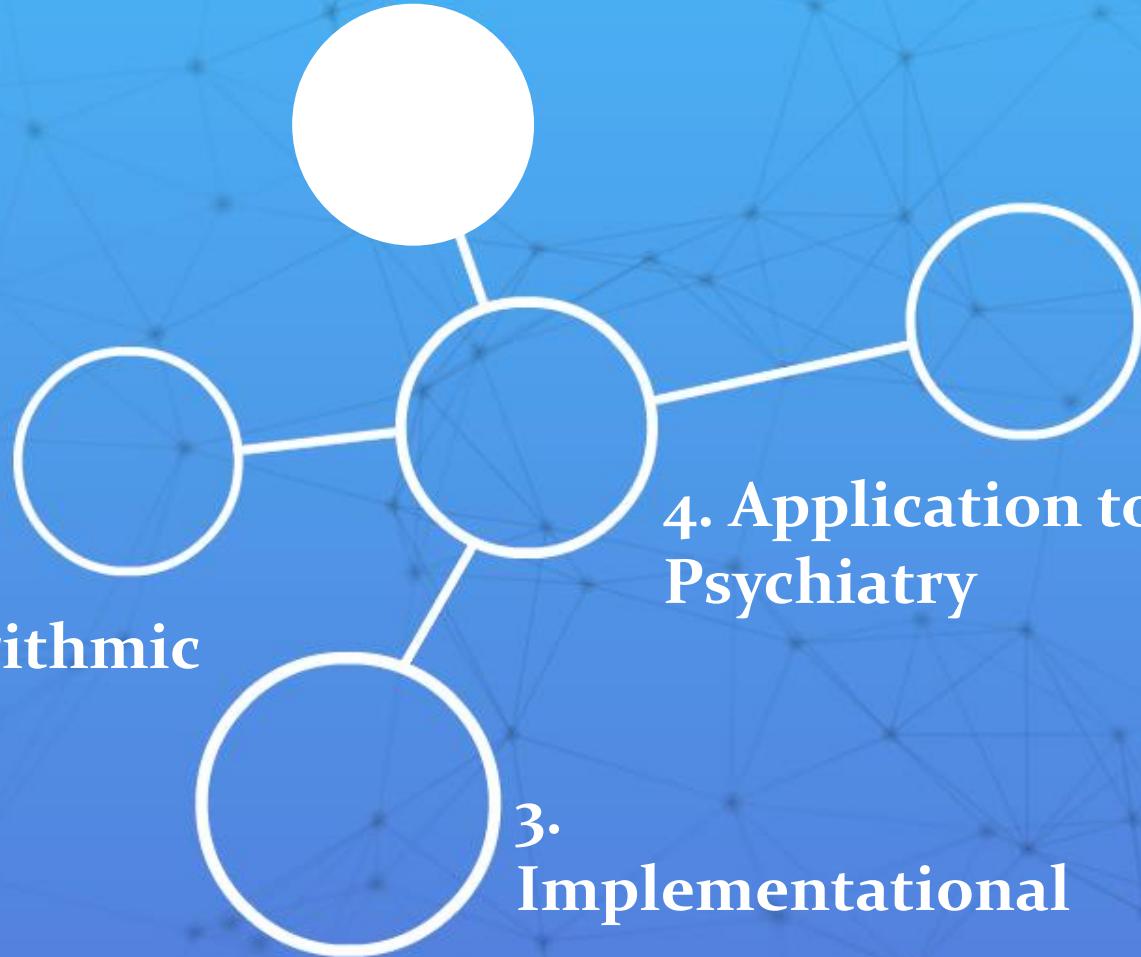
Outline

1. Computational

2.
Algorithmic

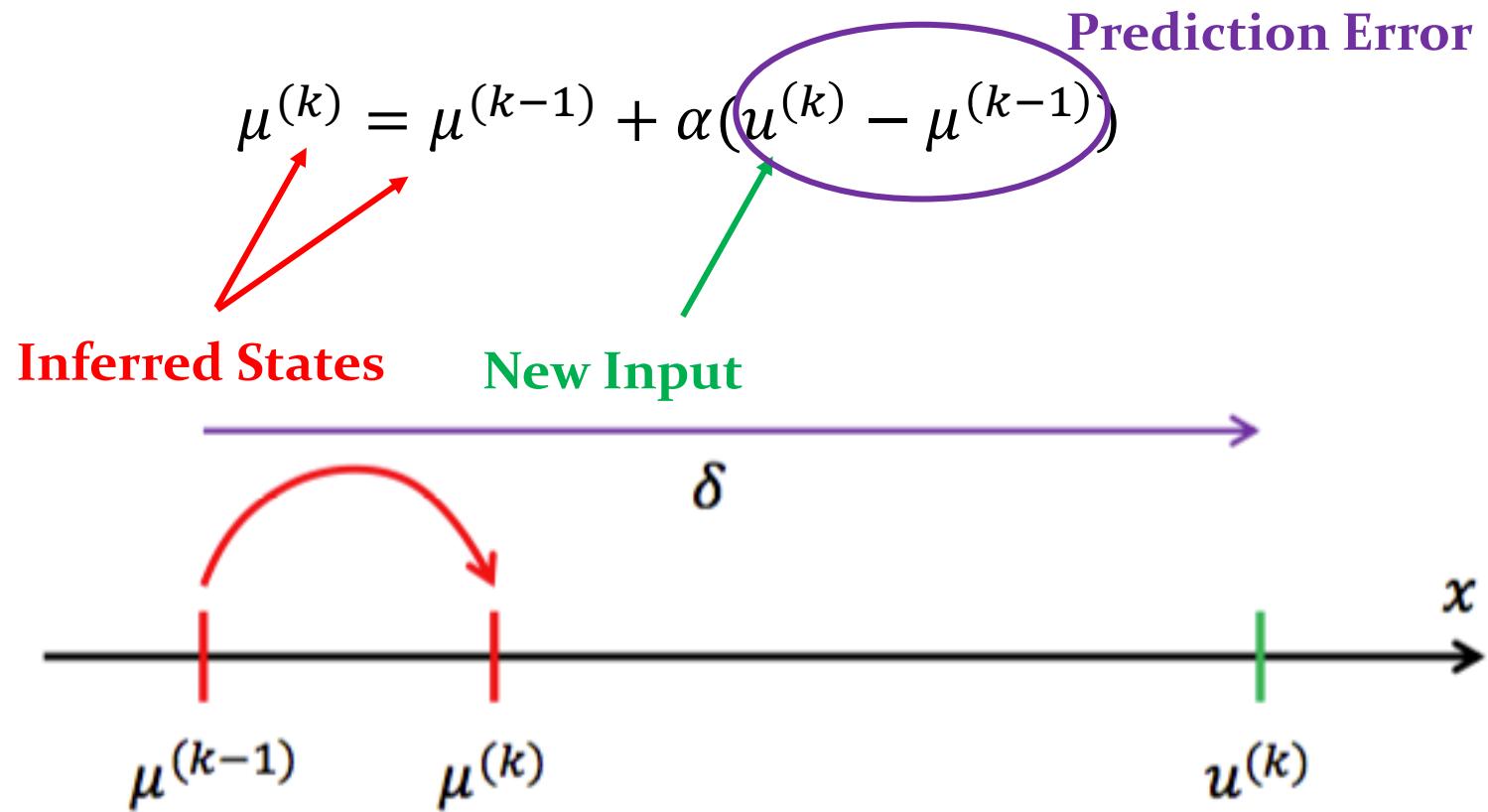
3.
Implementational

4. Application to
Psychiatry



Example of a simple model

Rescorla-Wagner Learning:

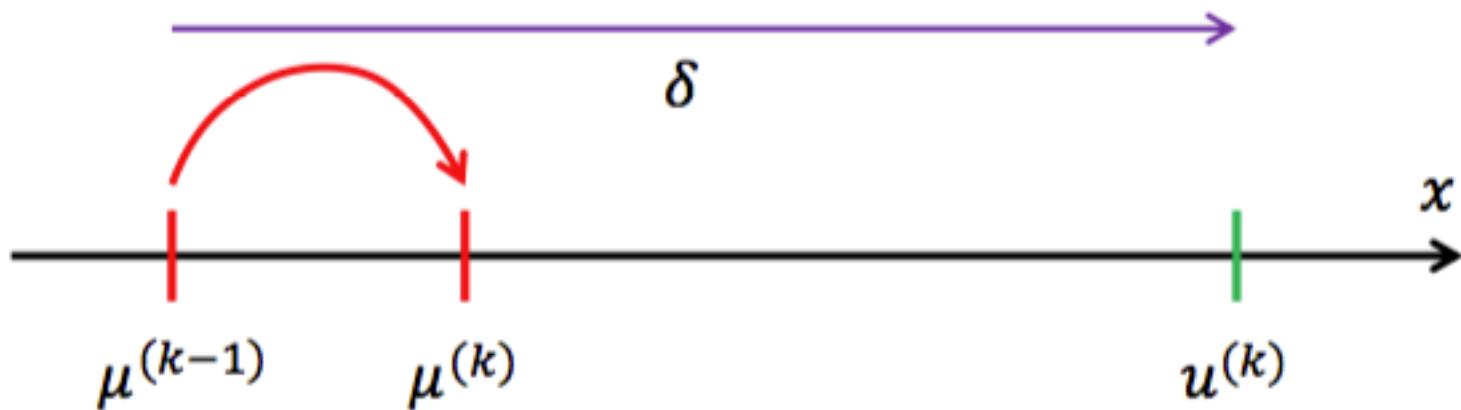


Example of a simple model

Rescorla-Wagner Learning:

Learning Rate

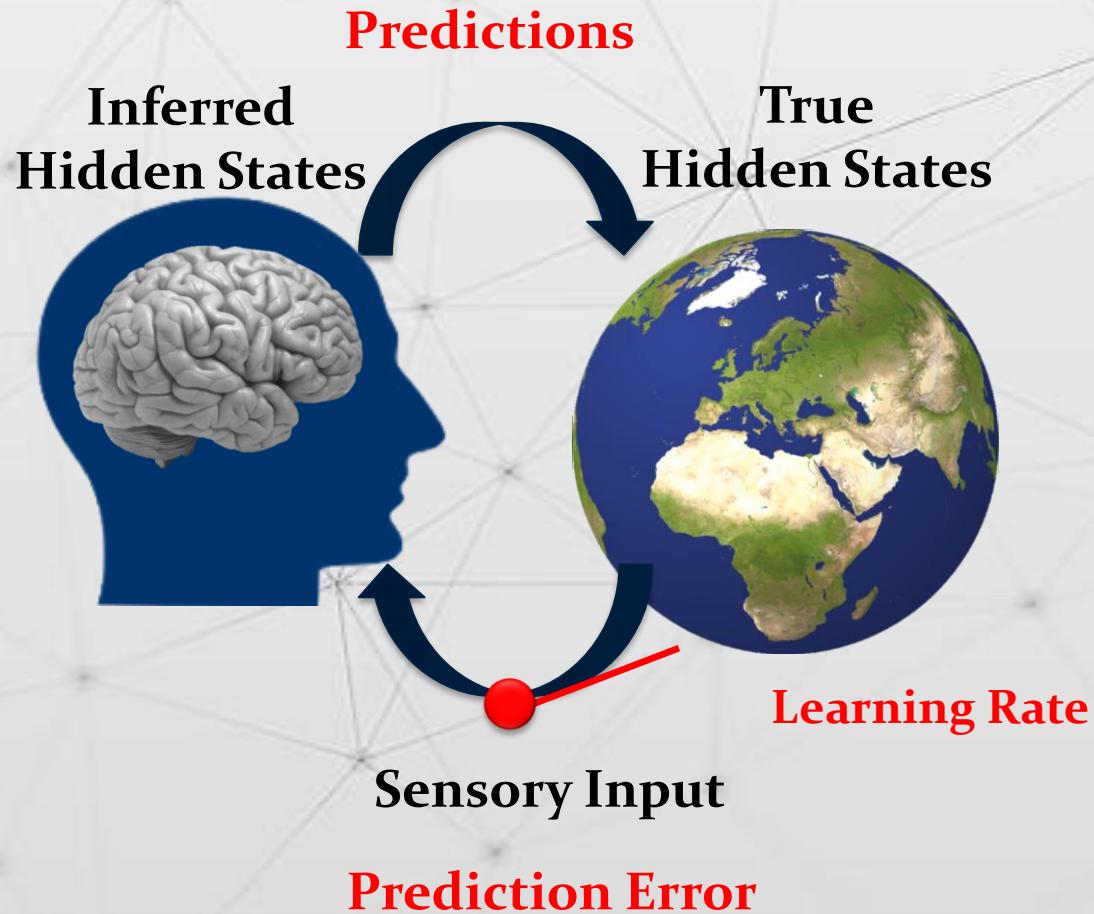
Belief Update → $\Delta\mu^{(k)} \propto \alpha\delta$



Computational Variables



Translational Neuromodeling Unit

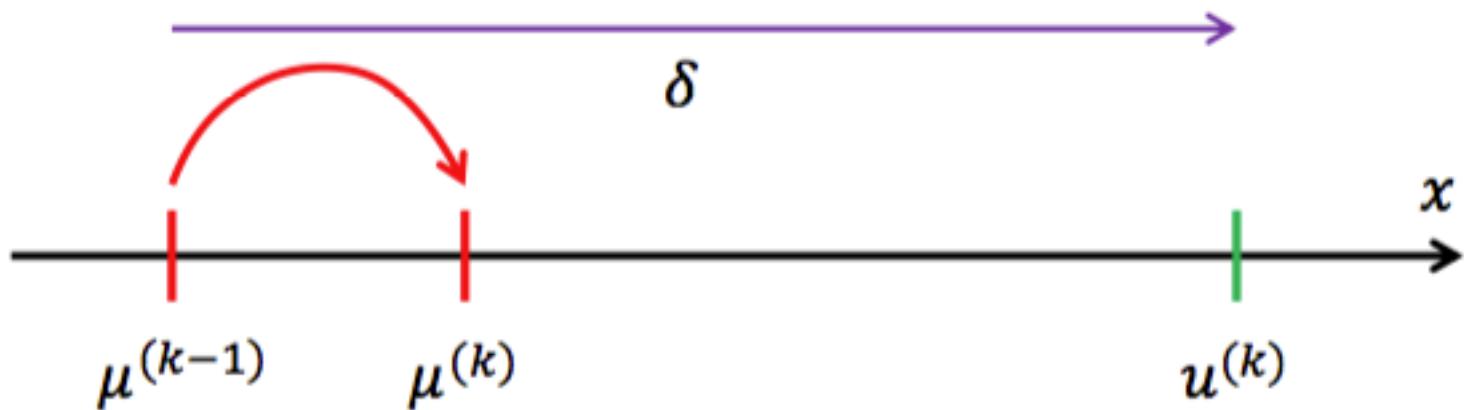


Example of a simple model

Rescorla-Wagner Learning:

Learning Rate

Belief Update → $\Delta\mu^{(k)} \propto \alpha\delta$



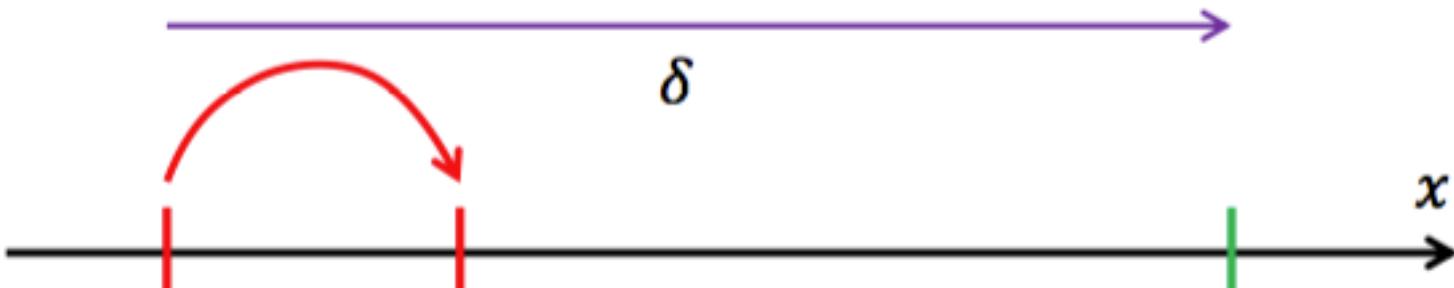
Example of a hierarchical model

Hierarchical Gaussian Filter :

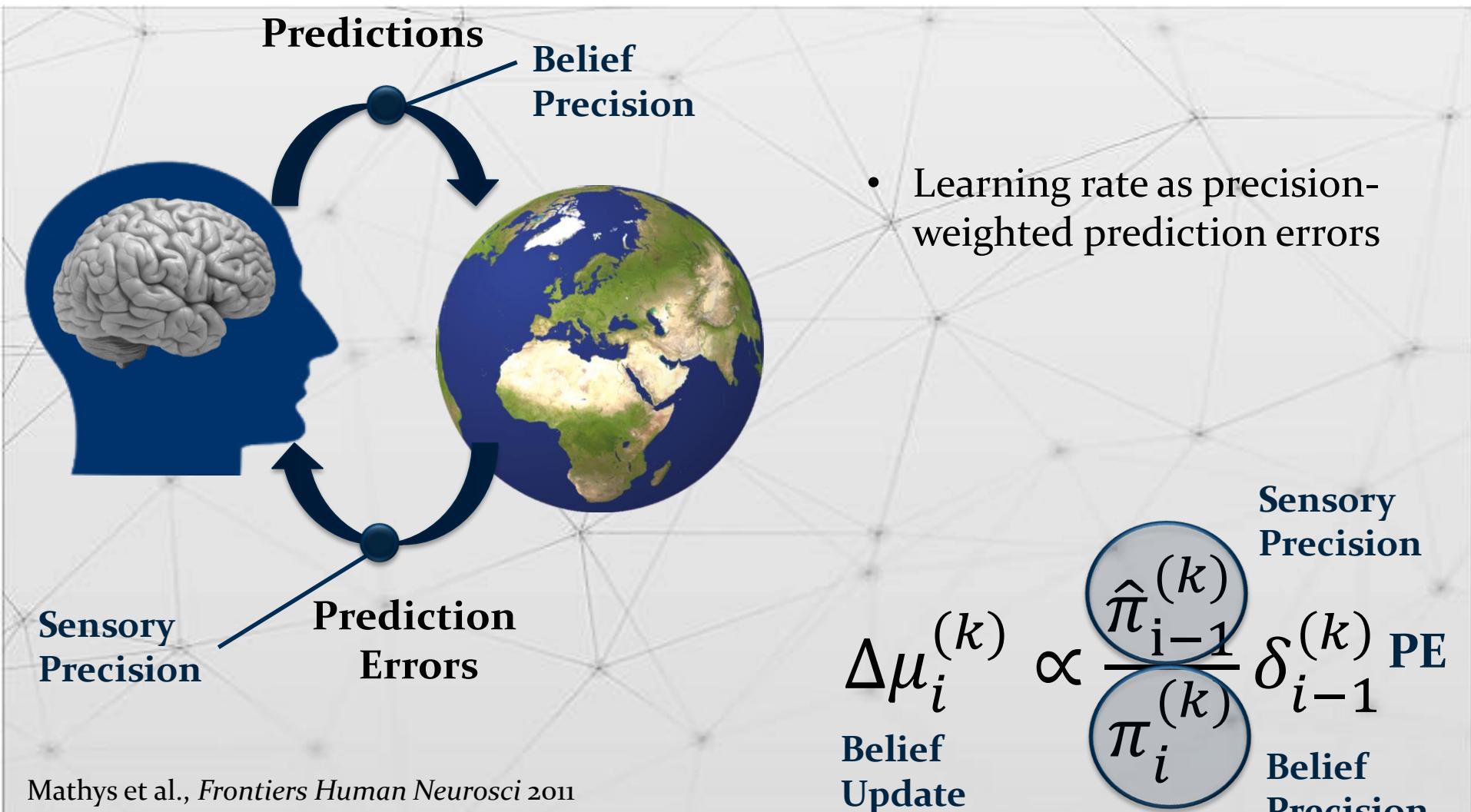
Weight

Belief Update → $\Delta\mu^{(k)} \propto \frac{\hat{\pi}_{i-1}^{(k)}}{\pi_i^{(k)}} \delta$

$= \frac{\text{how much we're learning here}}{\text{how much we already know}}$

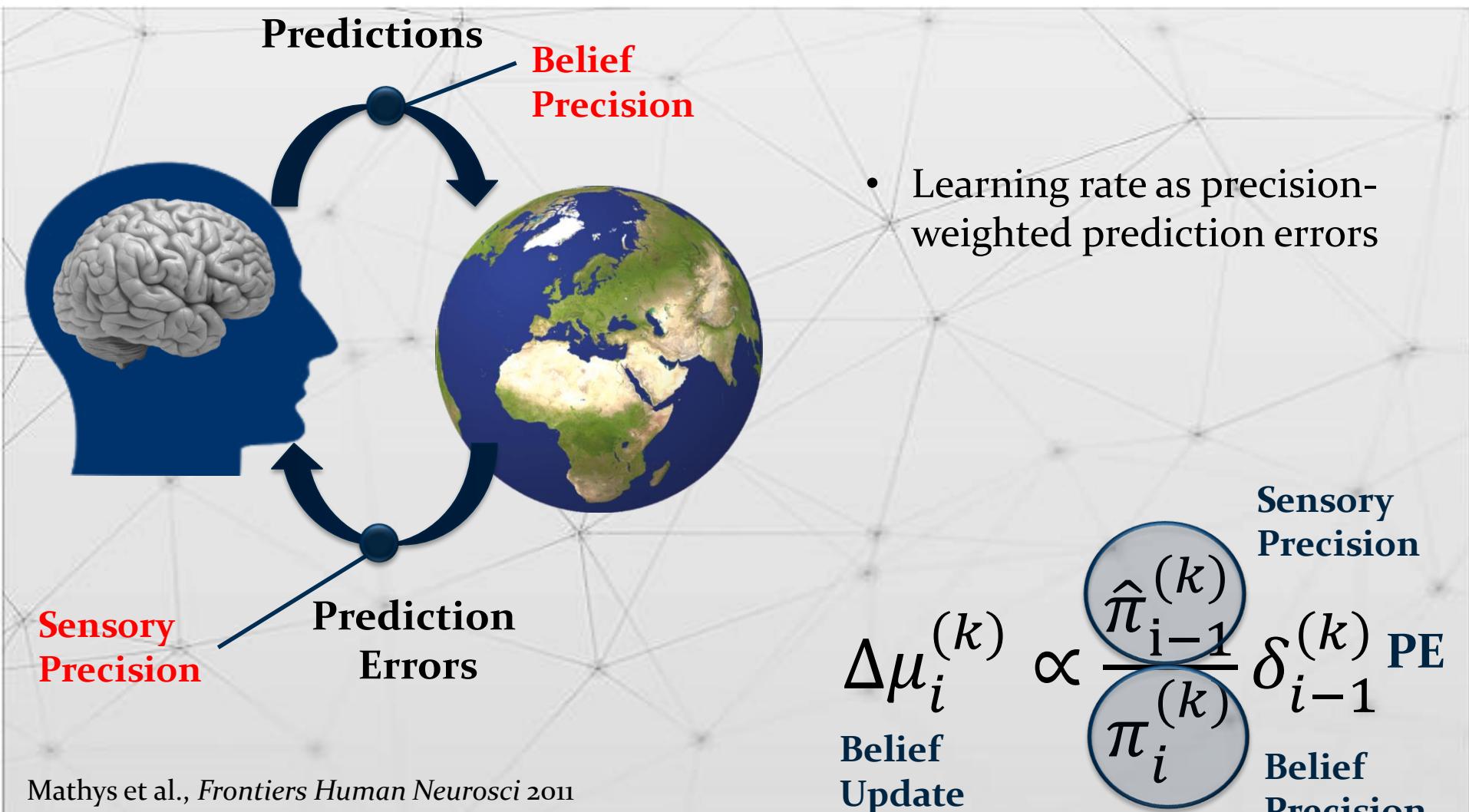

$$\Delta\mu^{(k)} \propto \frac{\hat{\pi}_{i-1}^{(k)}}{\pi_i^{(k)}} \delta$$
$$= \frac{\text{how much we're learning here}}{\text{how much we already know}}$$

Inference is Hierarchical



Mathys et al., *Frontiers Human Neurosci* 2011

Inference is Hierarchical



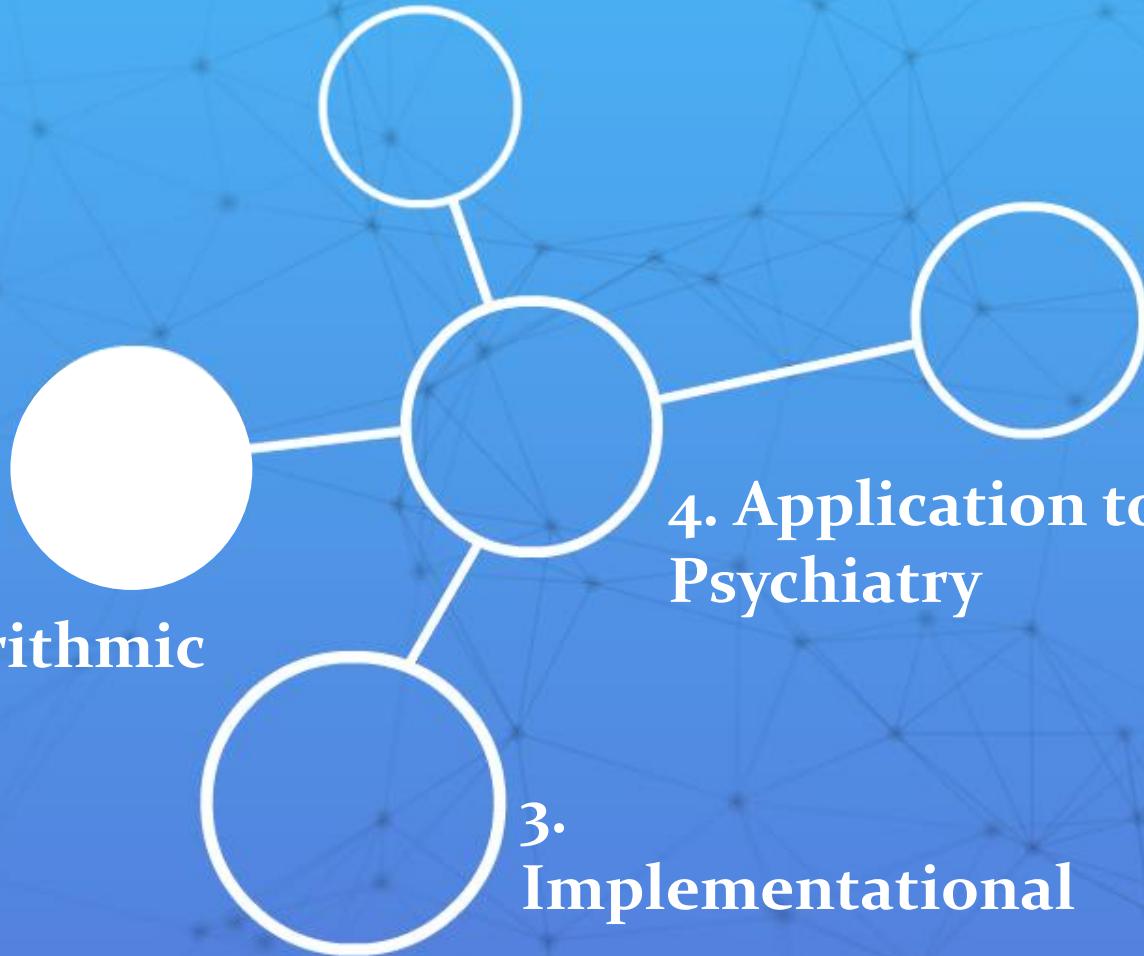
Mathys et al., *Frontiers Human Neurosci* 2011

Outline

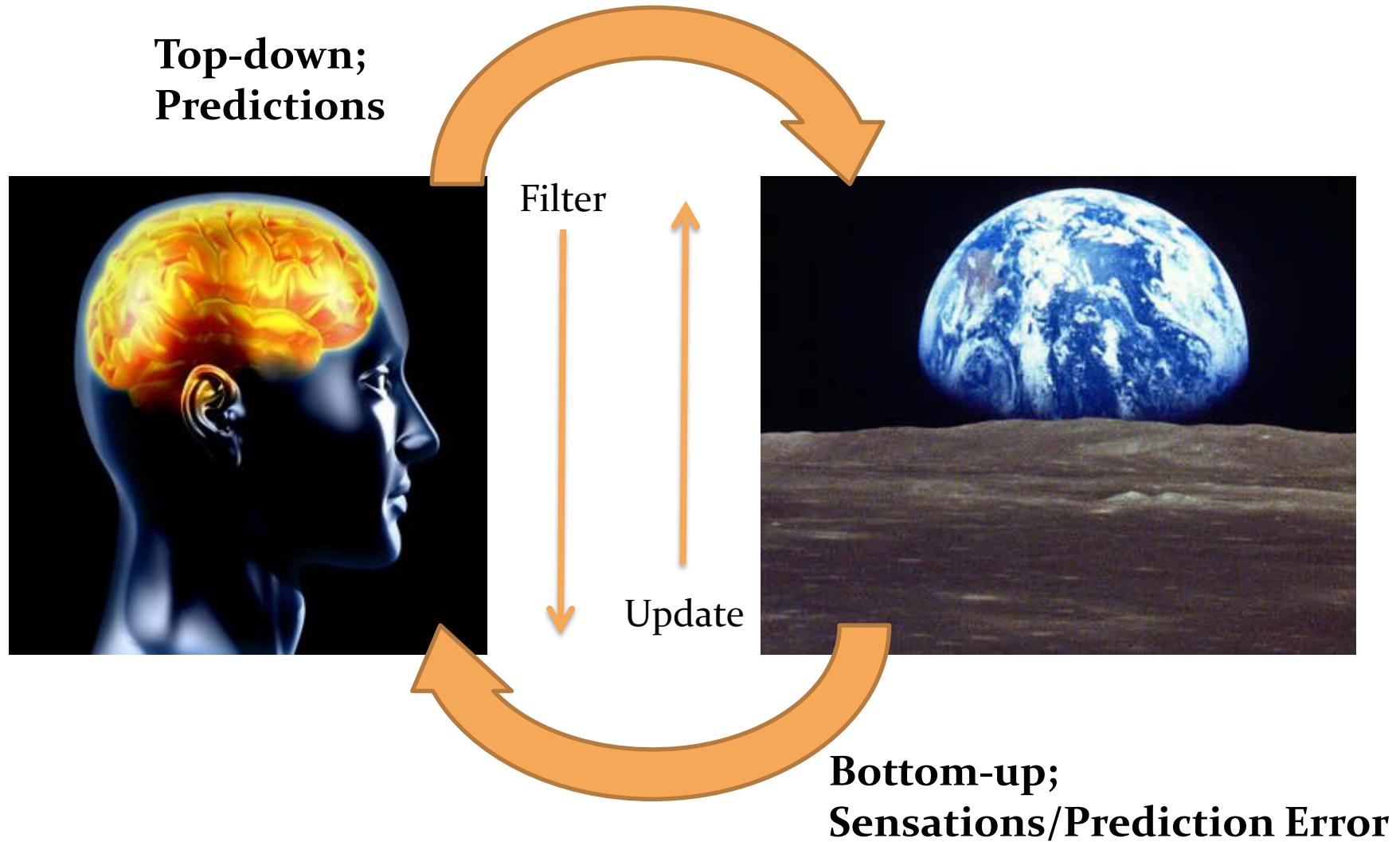
1. Computational

2.
Algorithmic

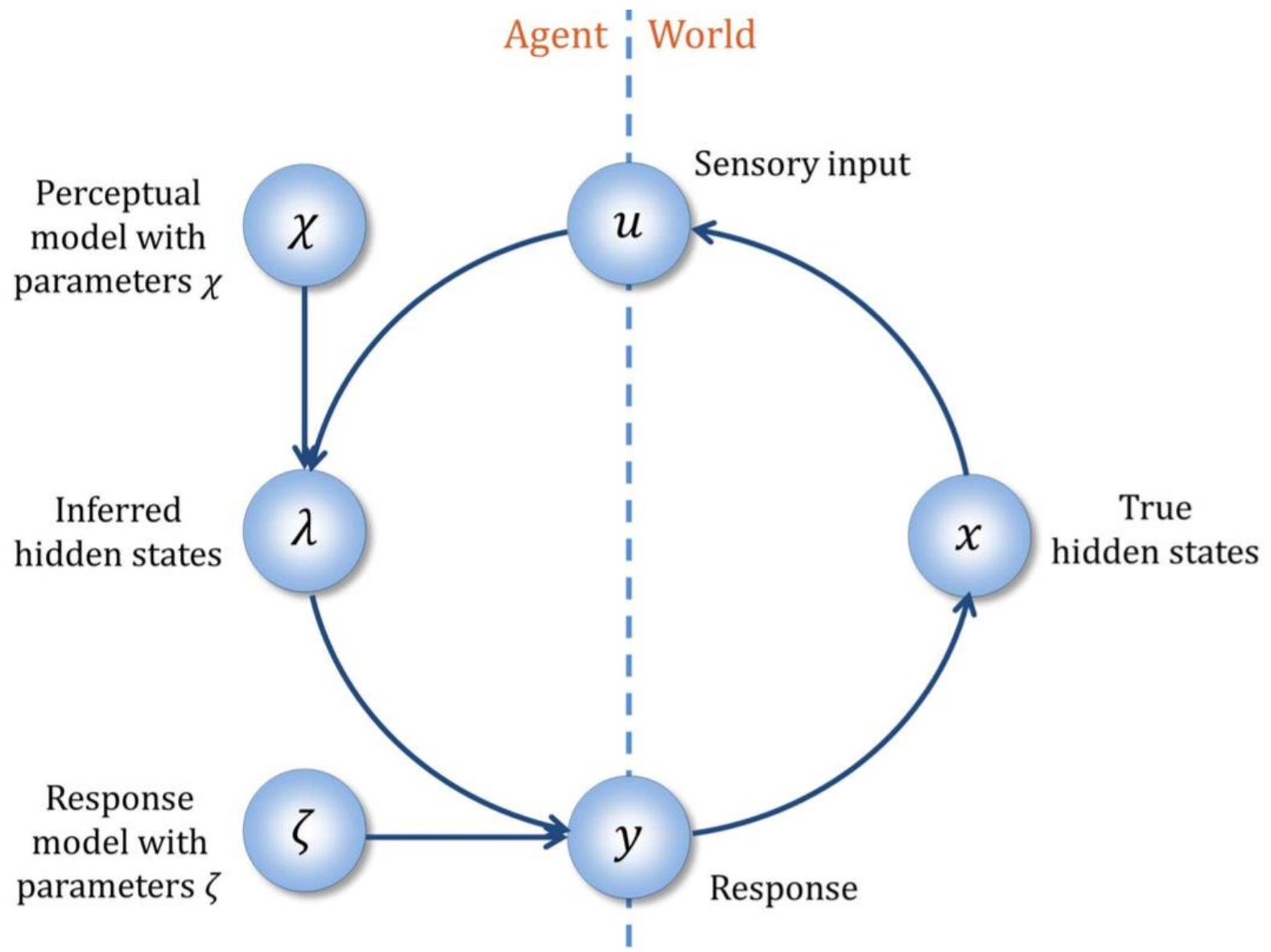
3.
Implementational
4. Application to Psychiatry



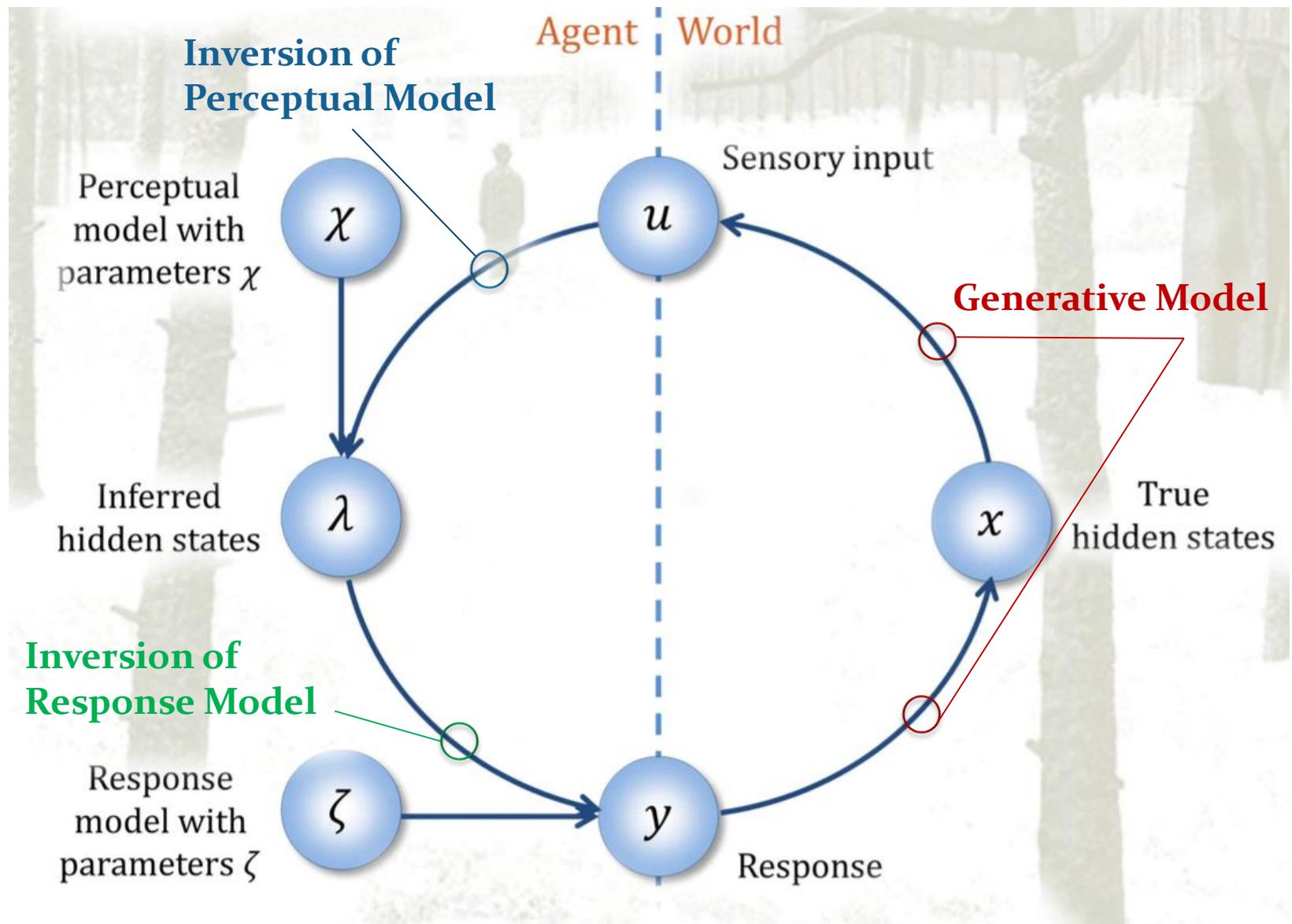
Perception (learning) via hierarchical interactions



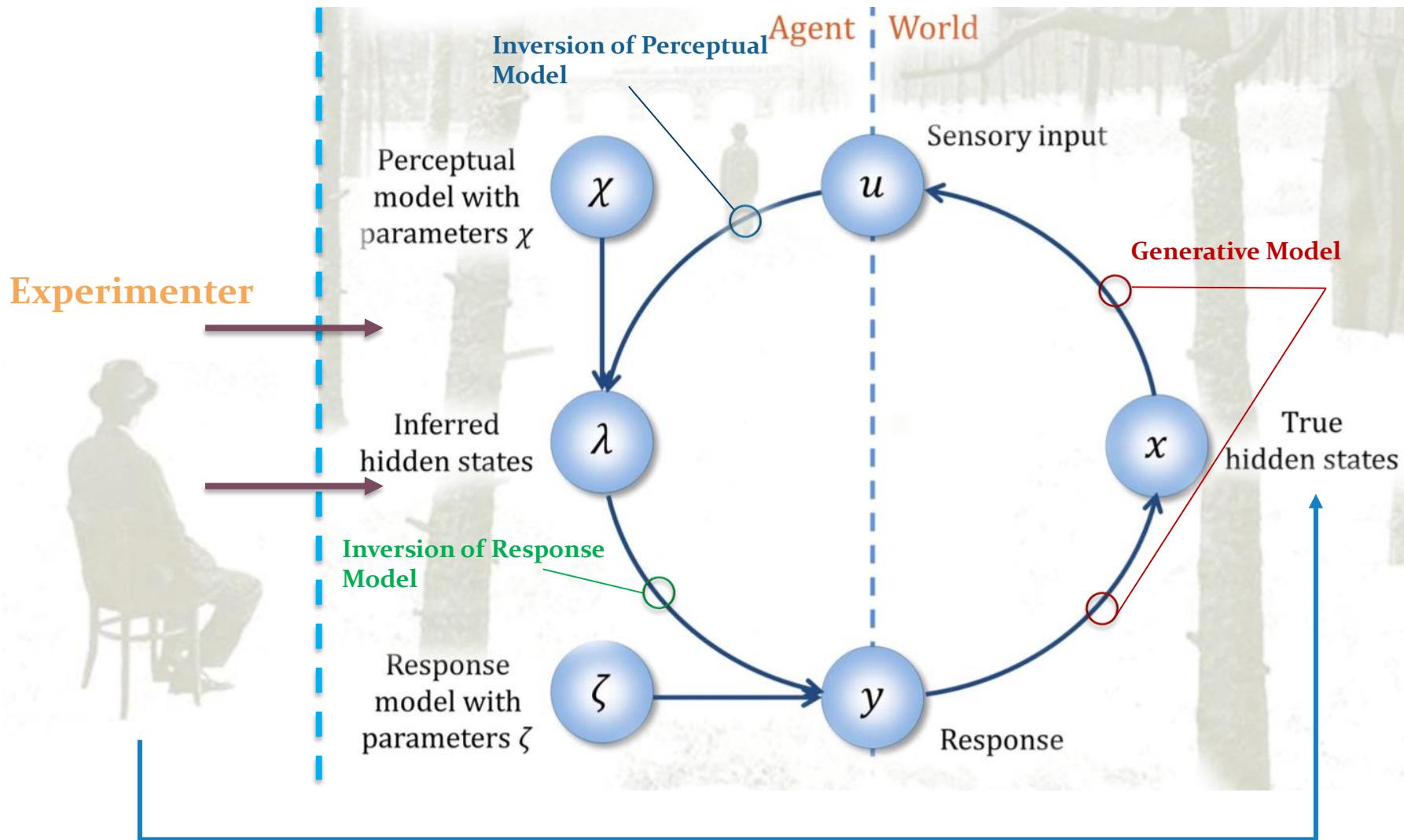
From perception to action



From perception to action

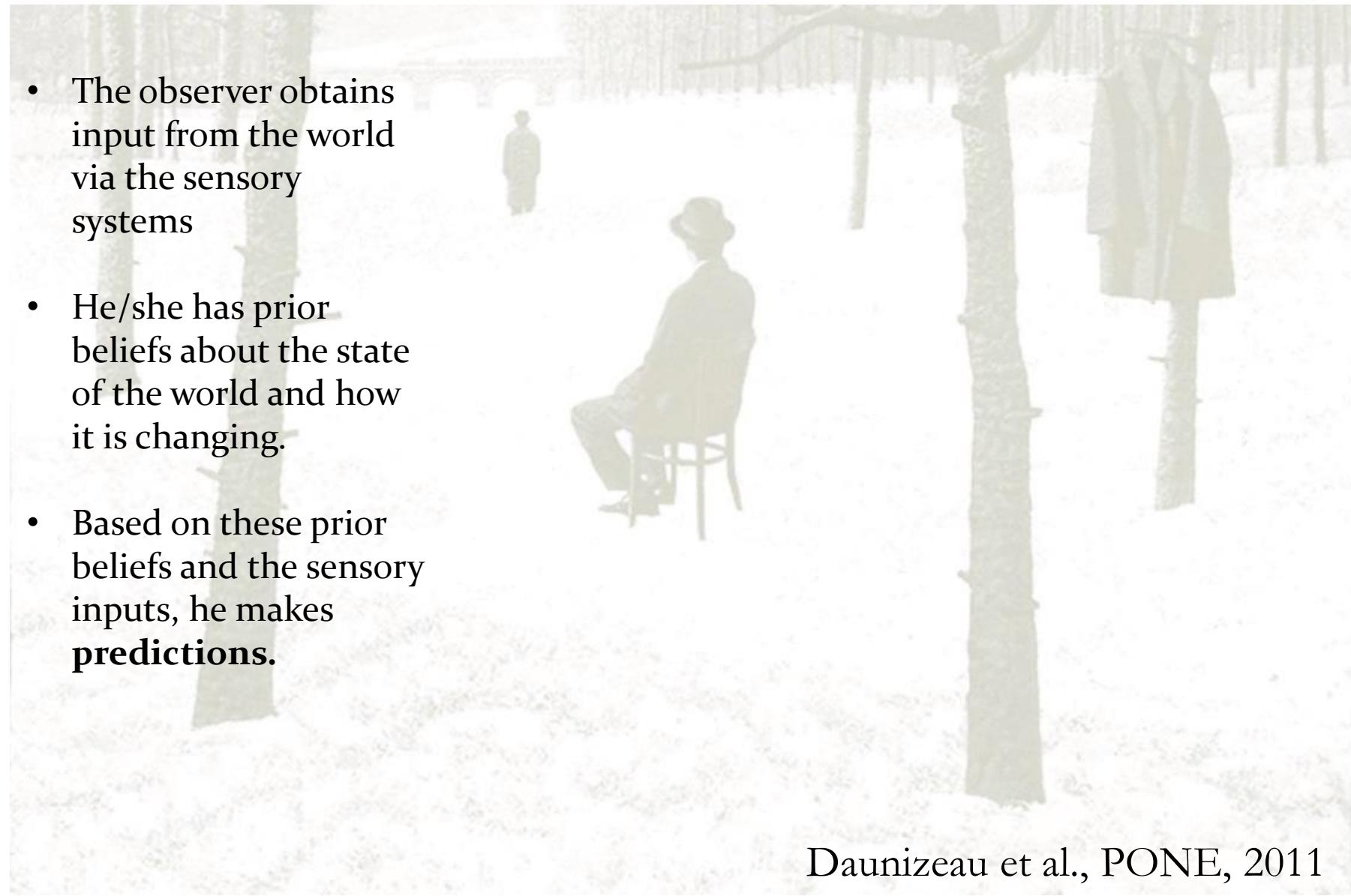


From perception to action to observation



Observing the observer

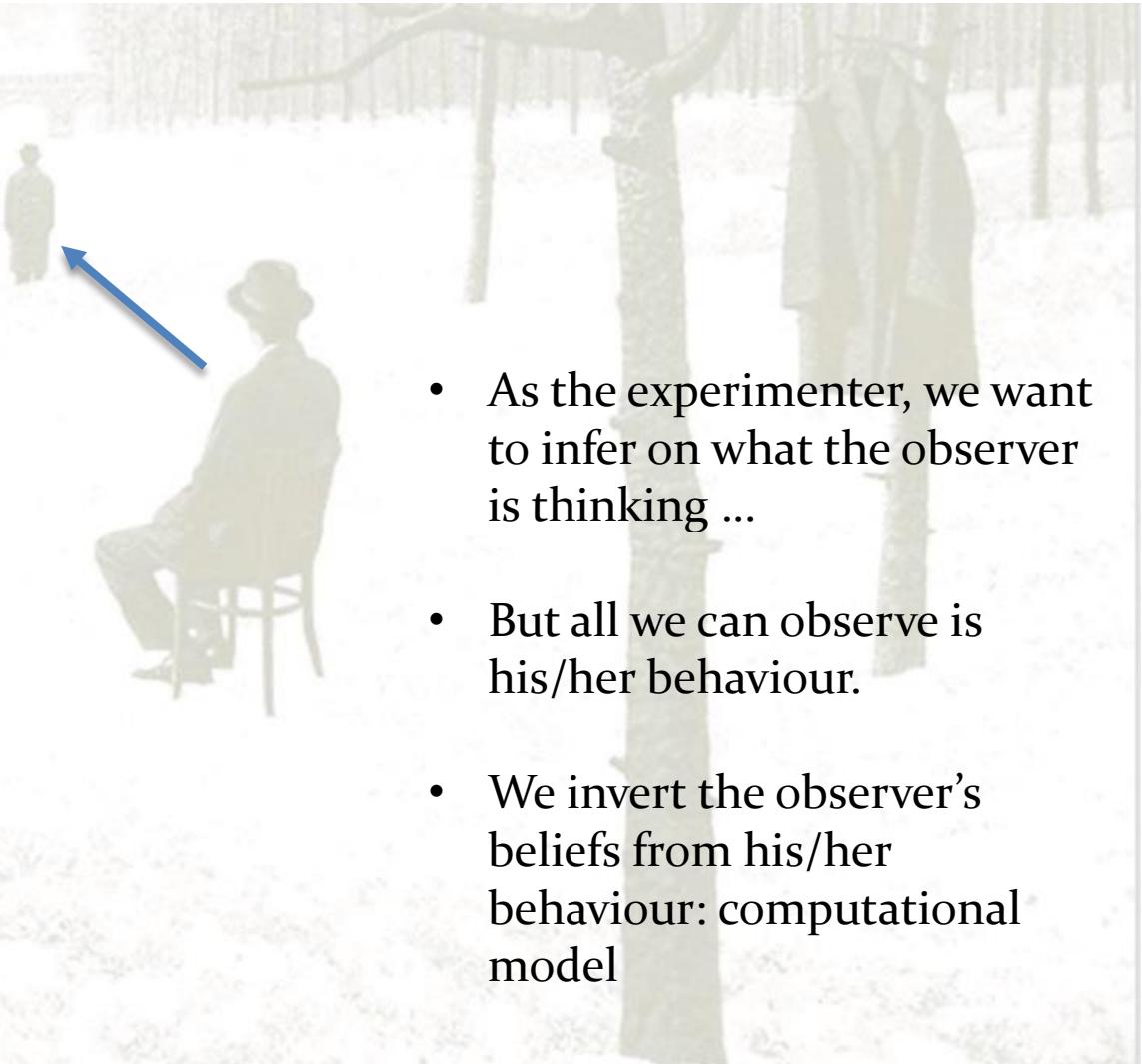
- The observer obtains input from the world via the sensory systems
- He/she has prior beliefs about the state of the world and how it is changing.
- Based on these prior beliefs and the sensory inputs, he makes **predictions**.



Daunizeau et al., PONE, 2011

Observing the observer

- The observer obtains input from the world via the sensory systems
- He/she has prior beliefs about the state of the world and how it is changing.
- Based on these prior beliefs and the sensory inputs, he makes **predictions**.



- As the experimenter, we want to infer on what the observer is thinking ...
- But all we can observe is his/her behaviour.
- We invert the observer's beliefs from his/her behaviour: computational model

Daunizeau et al., PONE, 2011

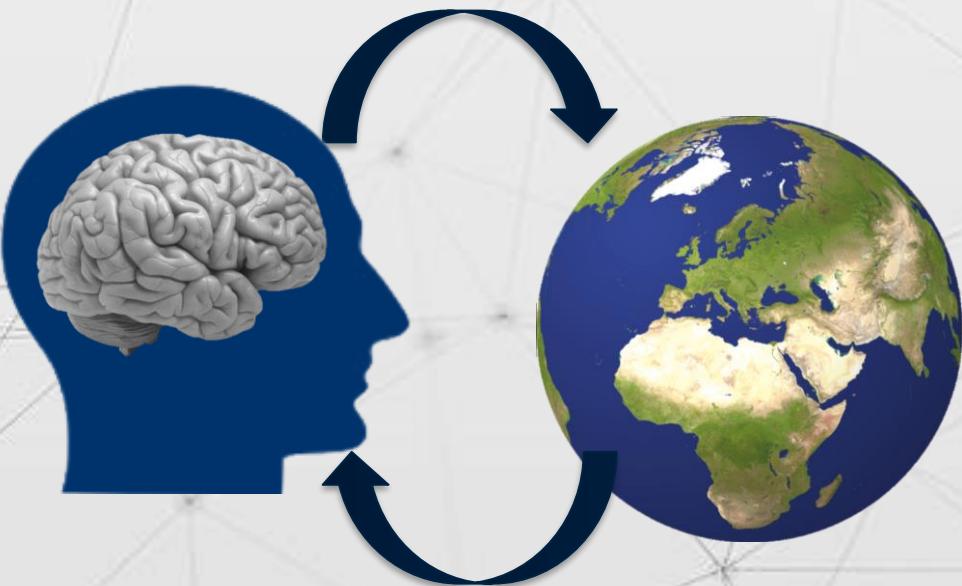
Bayesian Models



Translational Neuromodeling Unit

The Bayesian Brain

Predictions



Prediction Errors



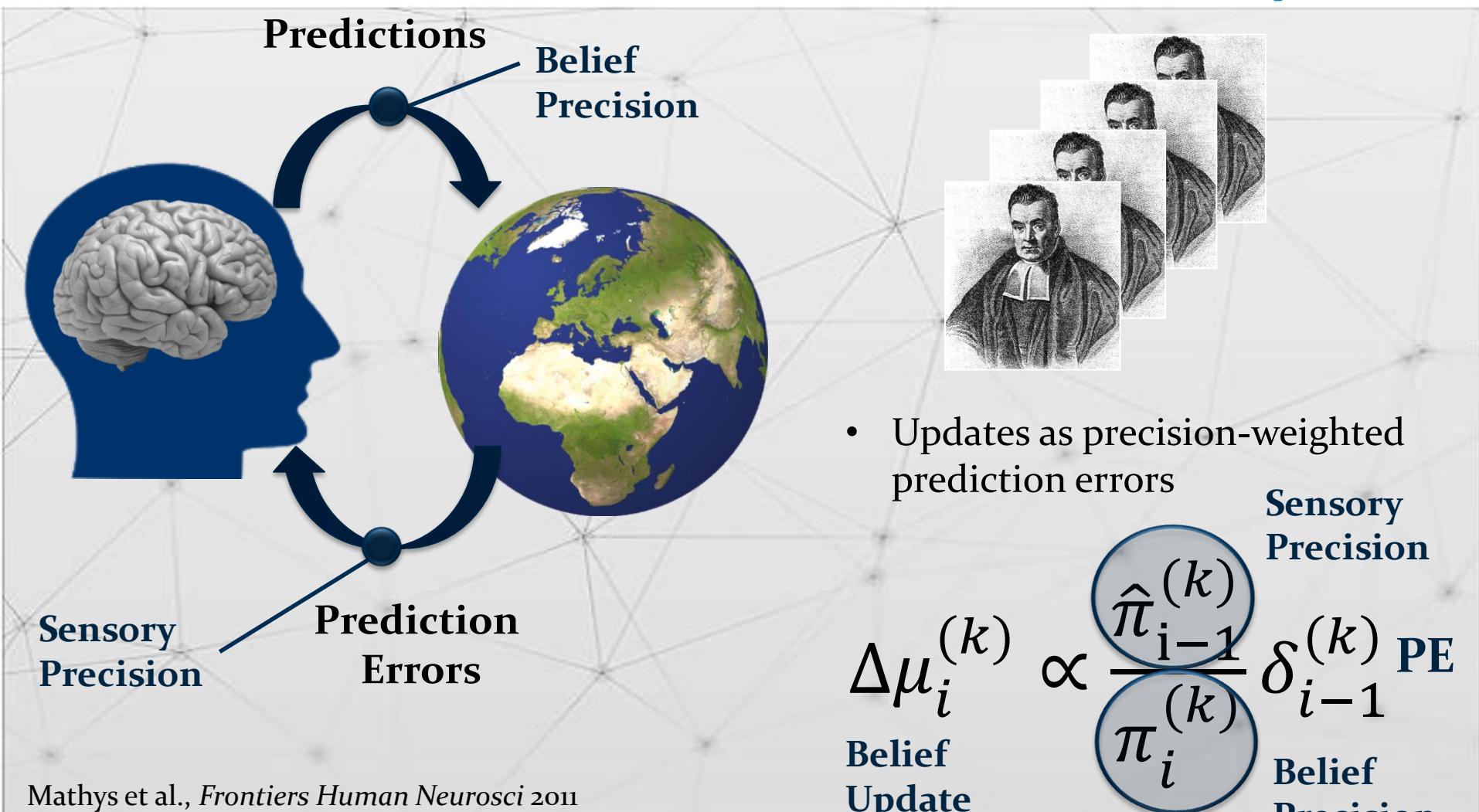
- The brain is an inference machine
- Conceptualise beliefs as probability distributions
- Updates via Bayes' rule:

$$p(\Theta|y, m) = \frac{p(\Theta|m)p(y|\Theta, m)}{\int p(\Theta|m)p(y|\Theta, m)d\Theta}$$

Prior Belief Sensory Data
Posterior Belief Evidence

Hierarchical Gaussian Filter

Hierarchy

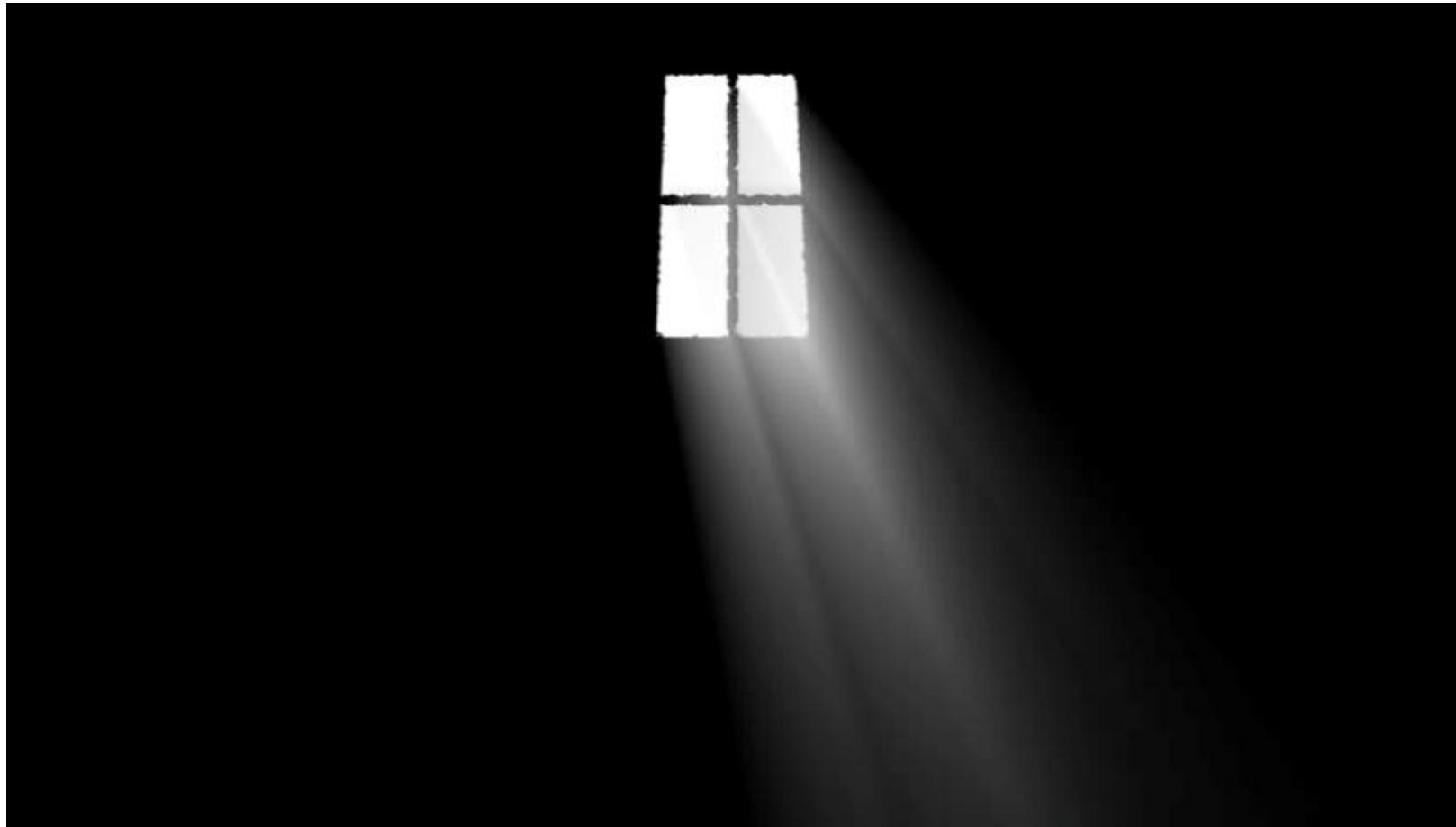


Mathys et al., *Frontiers Human Neurosci* 2011
 Mathys et al., *Frontiers Human Neurosci* 2014

Dark Room Experiment



Translational Neuromodeling Unit



The hierarchical Gaussian filter (HGF): a computationally tractable model for individual learning under uncertainty

Level 3: Phasic volatility

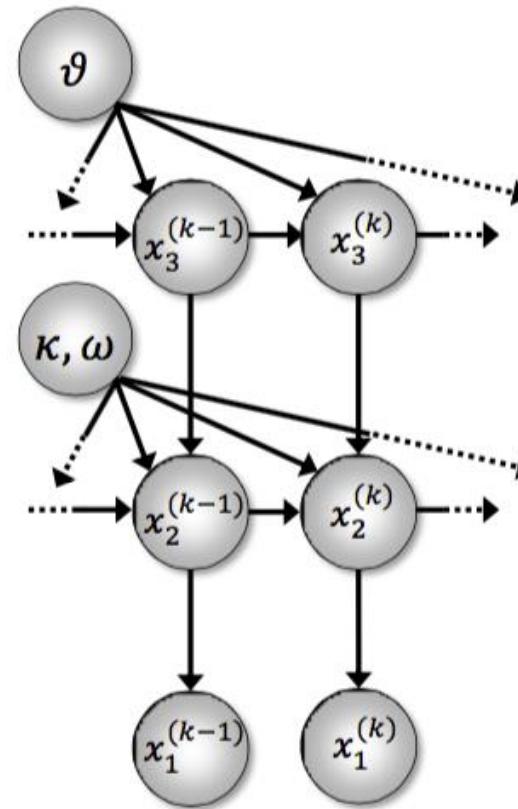
$$p(x_3^{(k)}) \sim \mathcal{N}(x_3^{(k-1)}, \vartheta)$$

Level 2: Tendency towards category 1

$$p(x_2^{(k)}) \sim \mathcal{N}(x_2^{(k-1)}, e^{(\kappa x_3^{(k-1)} + \omega)})$$

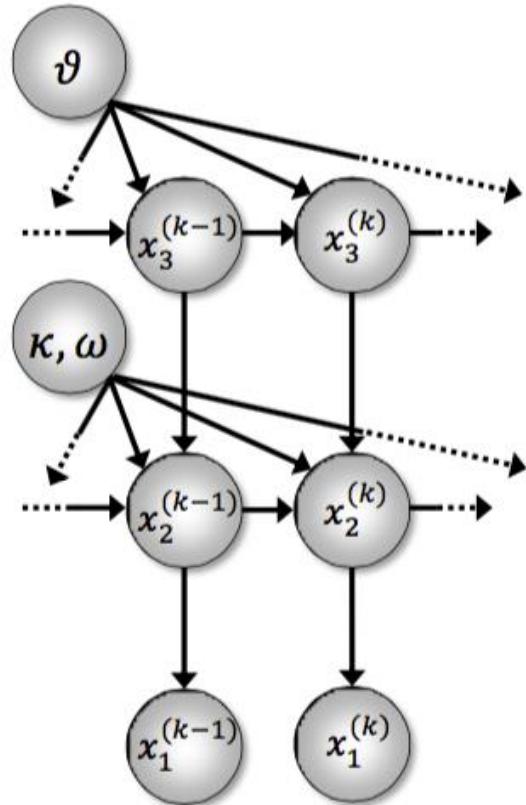
Level 1: Stimulus category

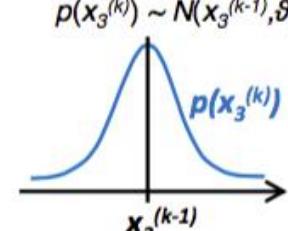
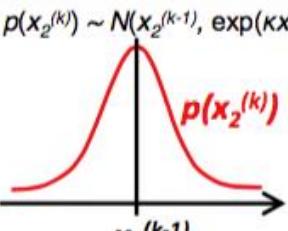
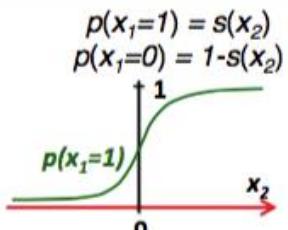
$$p(x_1 = 1) = \frac{1}{1 + e^{-x_2}}$$



Mathys et al., *Front Hum Neurosci*, 2011

The hierarchical Gaussian filter (HGF): a computationally tractable model for individual learning under uncertainty



State of the world	Model
Log-volatility x_3 of tendency	$p(x_3^{(k)}) \sim N(x_3^{(k-1)}, \vartheta)$ 
Tendency x_2 towards category "1"	$p(x_2^{(k)}) \sim N(x_2^{(k-1)}, \exp(\kappa x_3 + \omega))$ 
Stimulus category x_1 ("0" or "1")	$p(x_1=1) = s(x_2)$ $p(x_1=0) = 1 - s(x_2)$ 

Mathys et al., *Front Hum Neurosci*, 2011

HGF: Variational inversion and update equations

- Inversion proceeds by introducing a mean field approximation and fitting quadratic approximations to the resulting variational energies.
- This leads to simple one-step update equations for the sufficient statistics (mean and precision) of the approximate Gaussian posteriors of the hidden states x_i .
- The updates of the means have the same structure as value updates in Rescorla-Wagner learning:

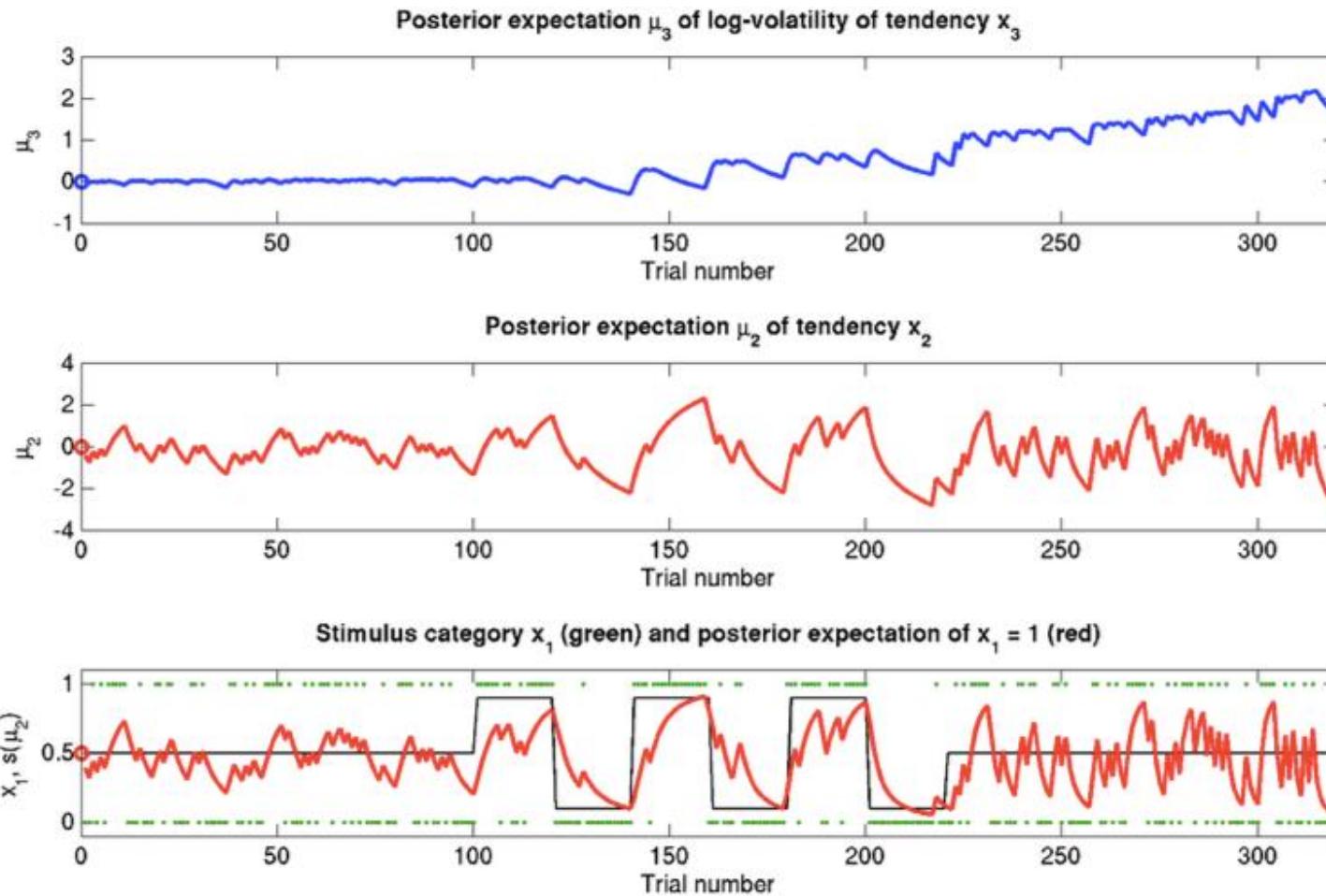
$$\Delta\mu_i = \frac{\hat{\pi}_{i-1}}{\pi_i} \delta_{i-1}$$

Prediction
Error

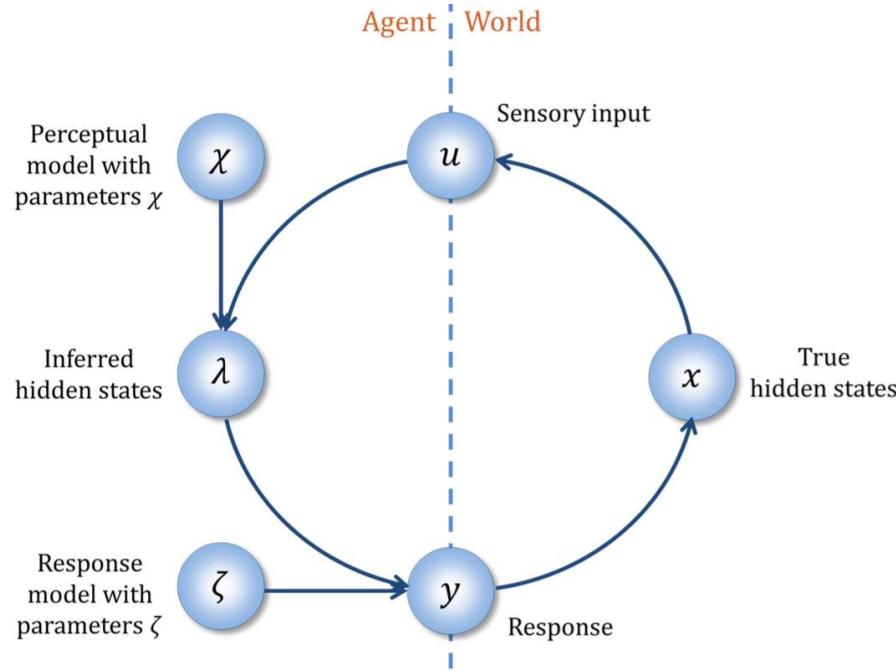
Precisions determine
the learning rate

Hierarchical Learning

Simulations: $\vartheta = 0.5$, $\omega = -2.2$, $\kappa = 1.4$



From perception to action



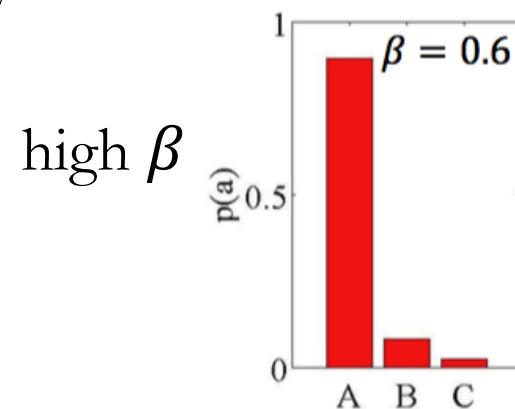
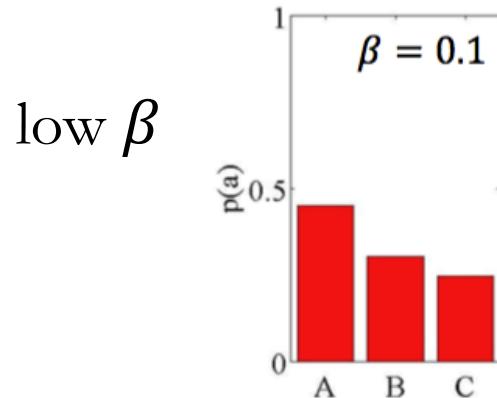
- In behavioural tasks, we observe actions a
- How do we use them to infer on beliefs λ ?
- Answer: we invert (estimate) a **response model**

Example of a simple response model

- Options A, B and C have values: $v_A = 8, v_B = 4, v_C = 2$
- We translate these values into action probabilities via a *Softmax* function:

$$p(a = A) = \frac{e^{\beta v_A}}{e^{\beta v_A} + e^{\beta v_B} + e^{\beta v_C}}$$

- Parameter β determines sensitivity to value differences:



All the necessary ingredients

- Perceptual model (updates based on prediction errors)
- Value function (inferred state to action value)
- Response model (action value to response probability)

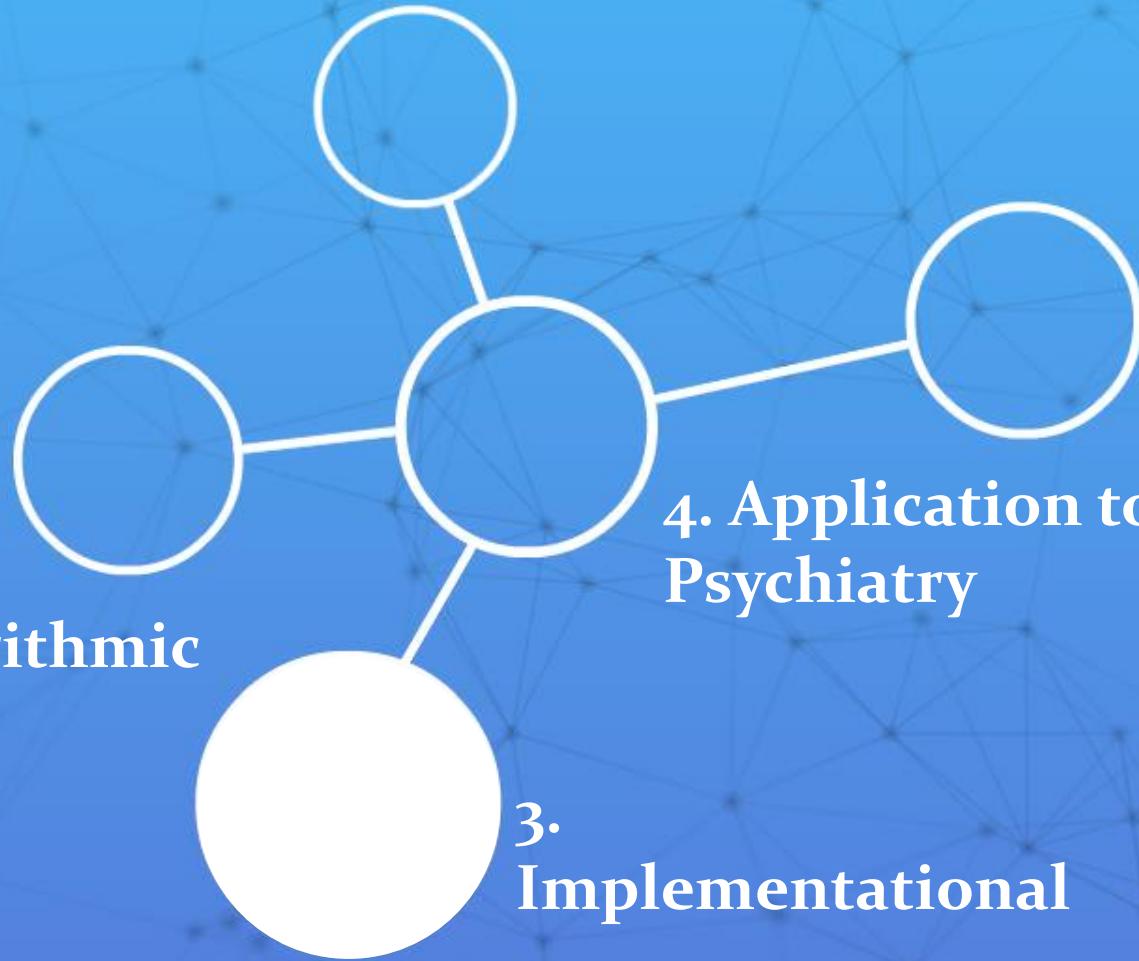
Outline

1. Computational

2.
Algorithmic

3.
Implementational

4. Application to
Psychiatry



Computational fMRI: The advantage



The question event-related/block designs answer:

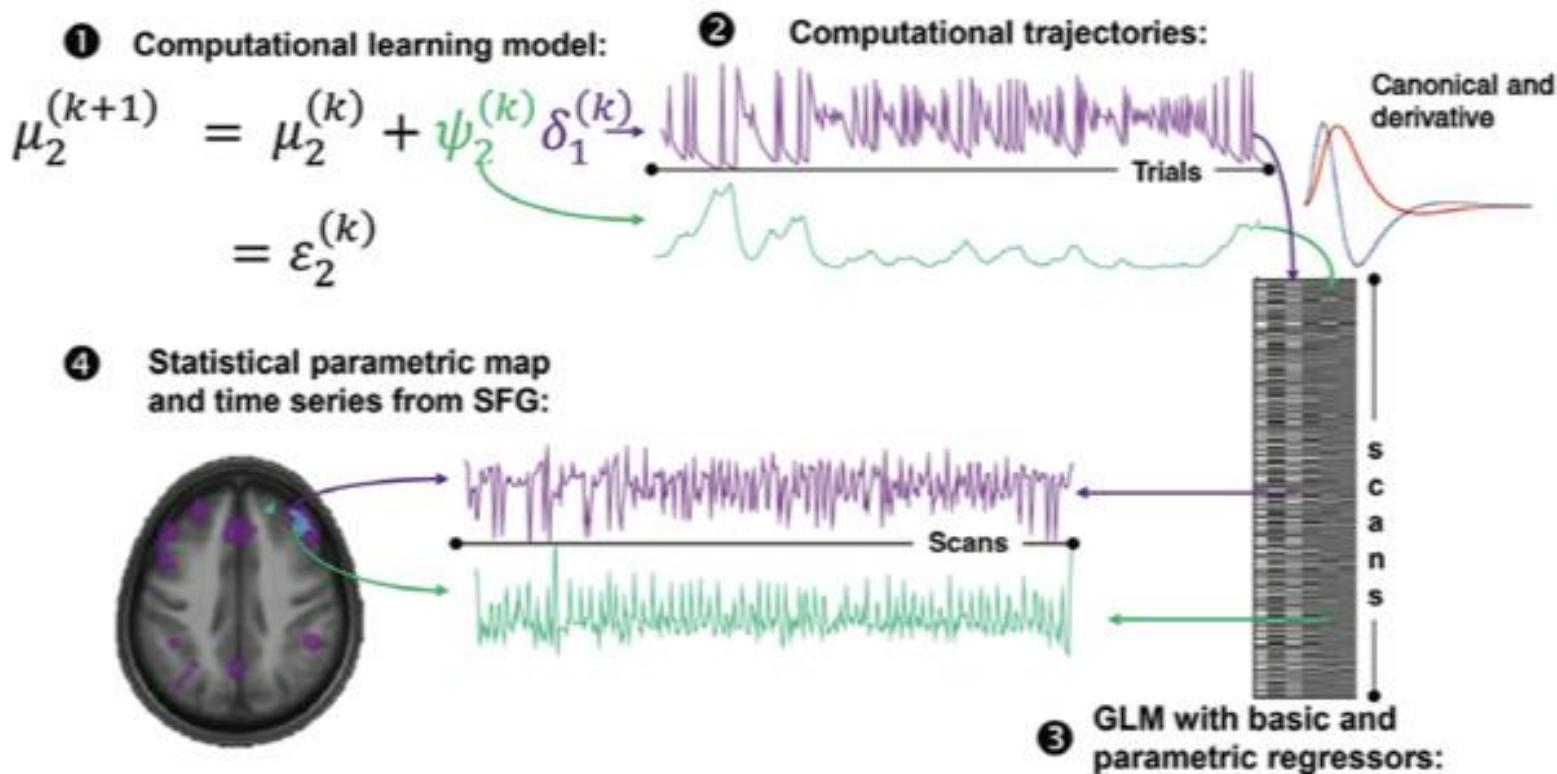
- Where in the brain do particular experimental conditions elicit BOLD responses?

The question model-based fMRI answers:

- How (i.e., by activation of which areas) does the brain implement a particular cognitive process?

It is able to do so because its regressors correspond to particular cognitive processes instead of experimental conditions.

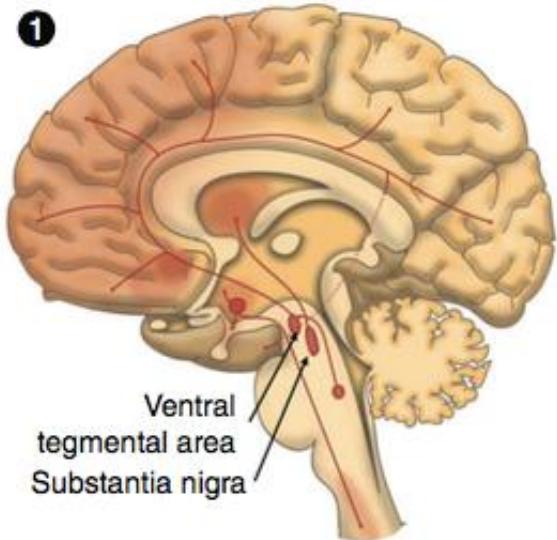
Computational fMRI analyses of neuromodulation



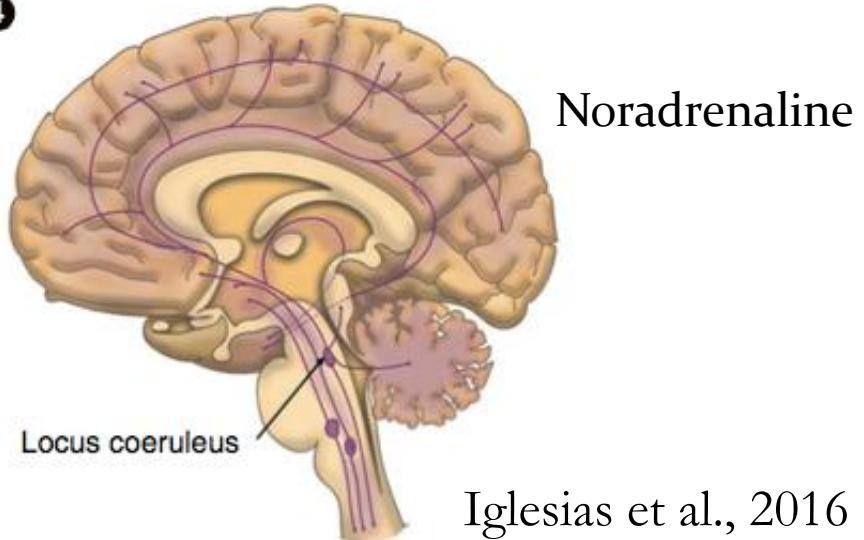
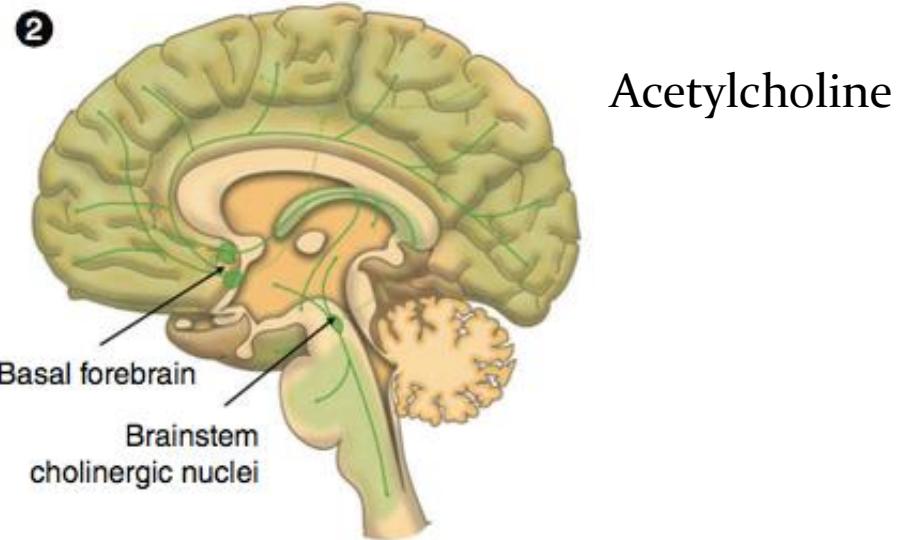
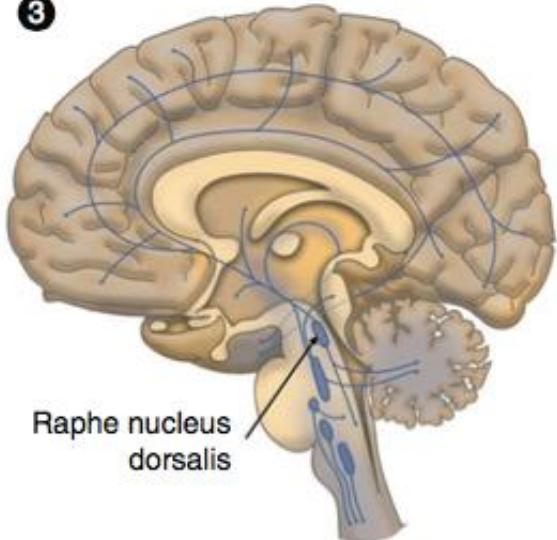
Iglesias et al., 2016

Computational fMRI analyses of neuromodulation

Dopamine



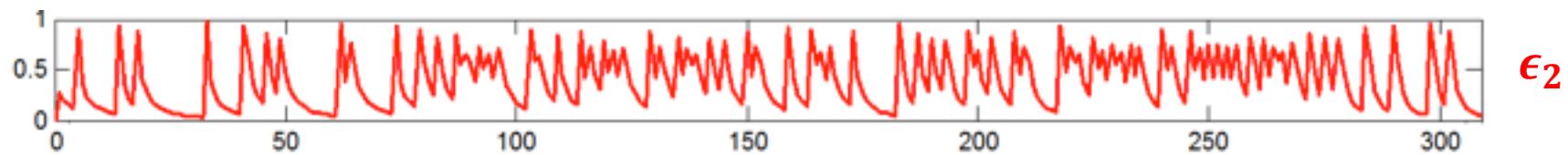
Serotonin



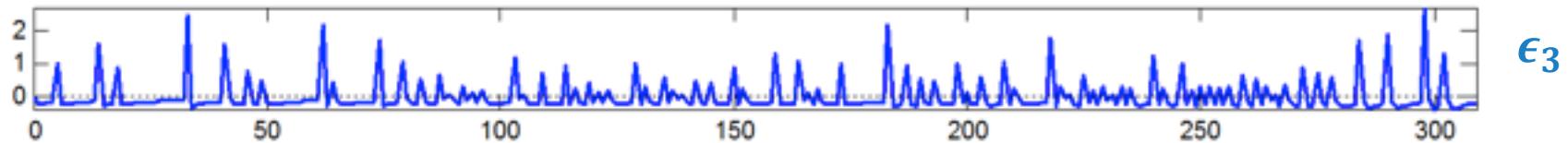
Iglesias et al., 2016

Application of the HGF: Two types of PEs

1. Outcome PE

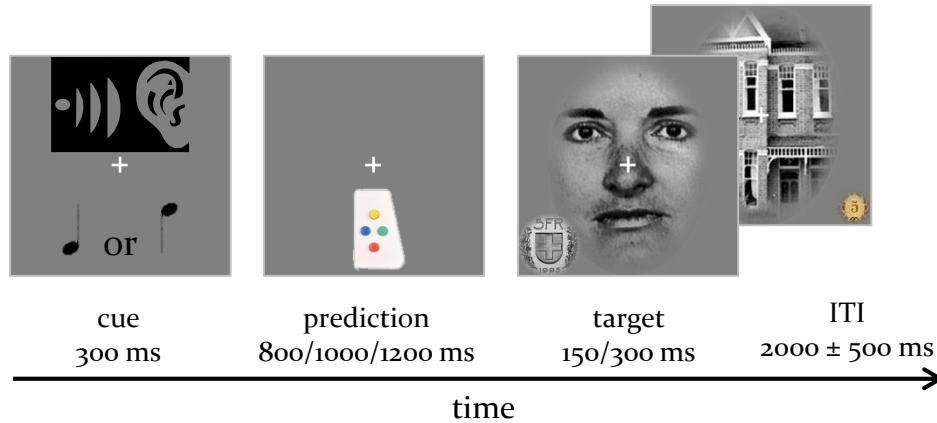


2. Cue-Outcome Contingency PE

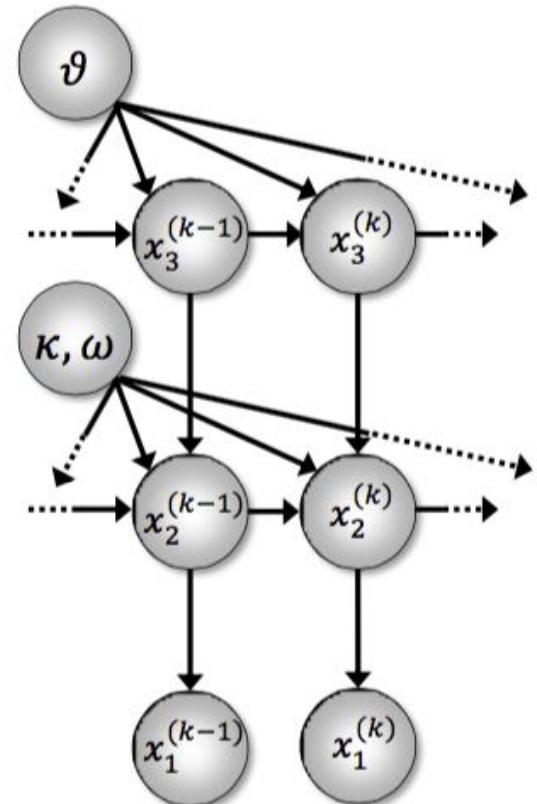
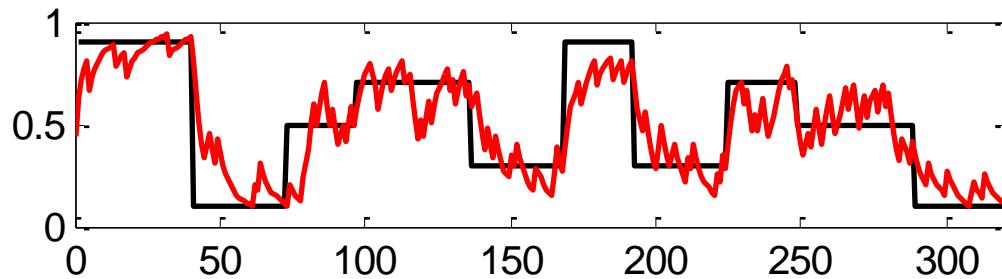


Iglesias et al., *Neuron*, 2013

Application of the HGF: Sensory Learning



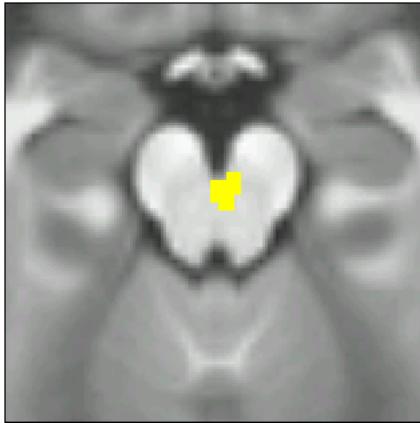
Changes in cue strength (black), and posterior expectation of visual category (red)



Iglesias et al., *Neuron*, 2013

Application of the HGF: Representation of precision-weighted PEs

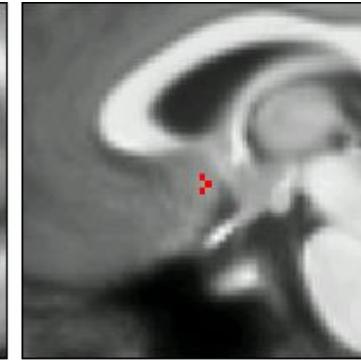
1. Outcome PE



$z = -18$

- right VTA
- Dopamine**

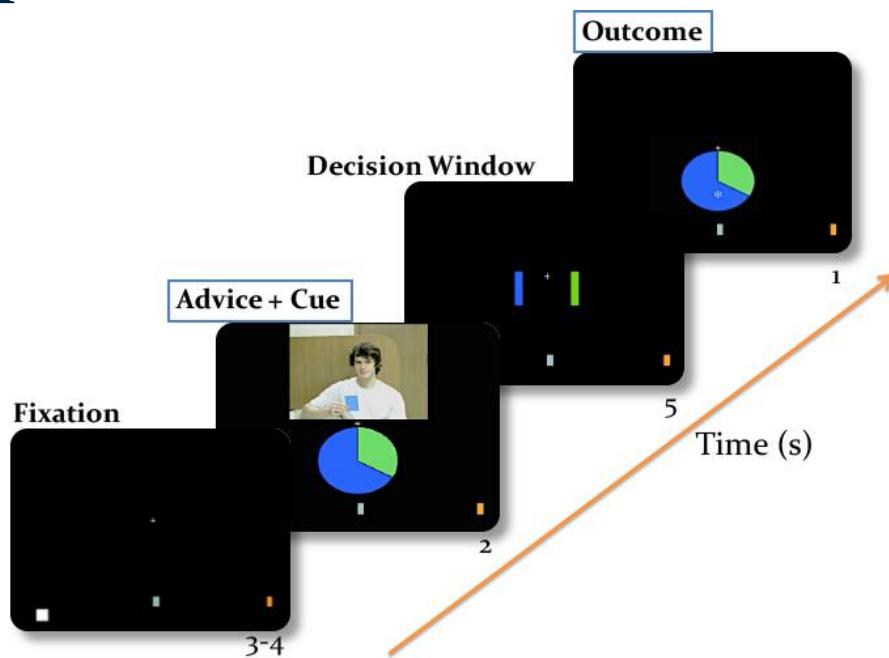
2. Probability PE



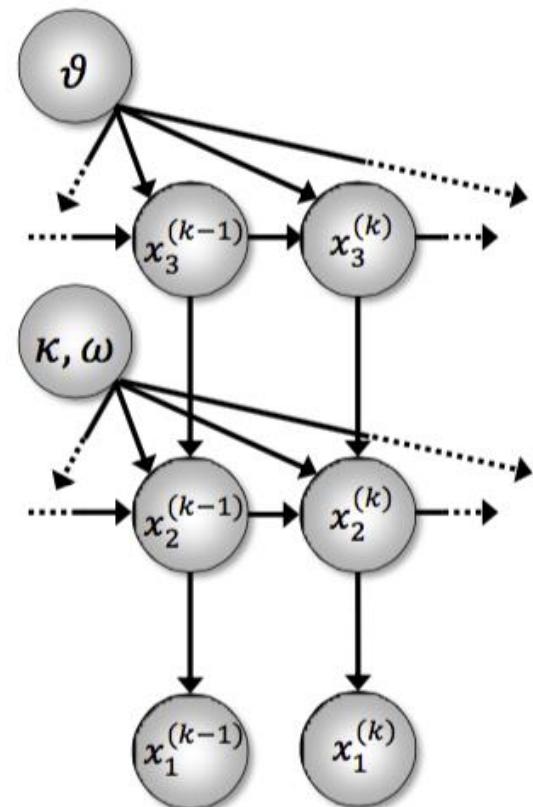
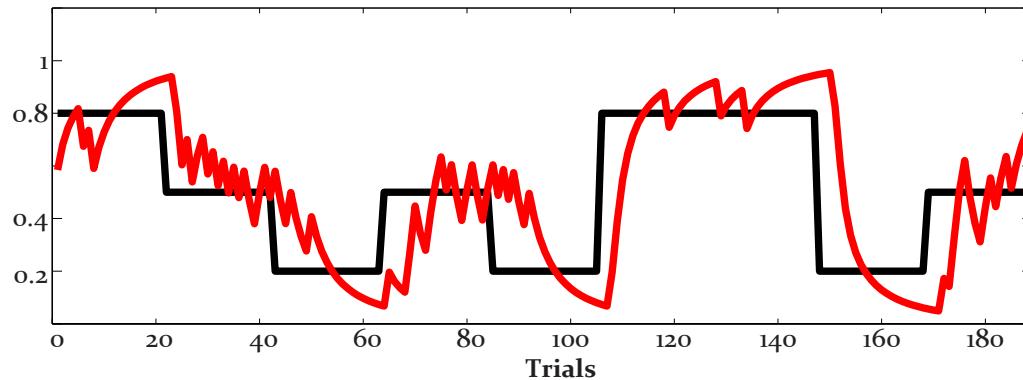
- left basal forebrain
- Acetylcholine**

Iglesias et al., *Neuron*, 2013

Application of the HGF: Social Learning



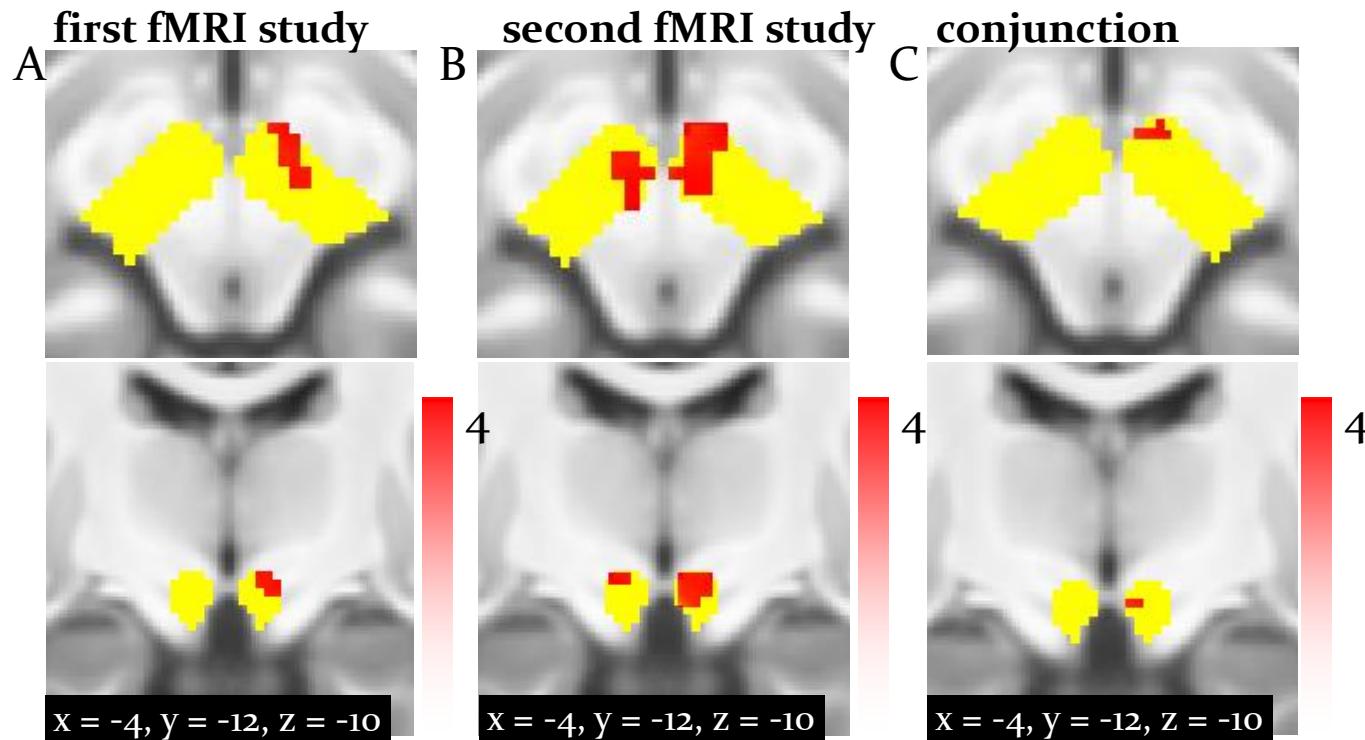
Changes in advice accuracy (black), and posterior expectation of adviser fidelity (red)



Diaconescu et al., SCAN, 2017

Representation of precision-weighted PEs in the social domain

1. Outcome PE

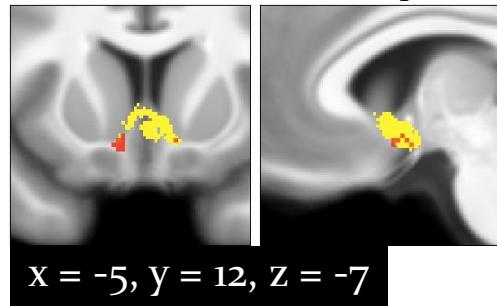


Diaconescu et al., *SCAN*, 2017

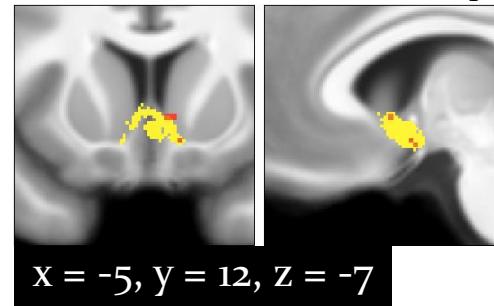
Representation of precision-weighted PEs in the social domain

2. Probability PE

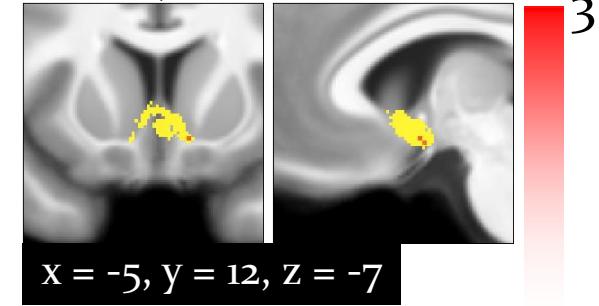
A. first fMRI study



B. second fMRI study

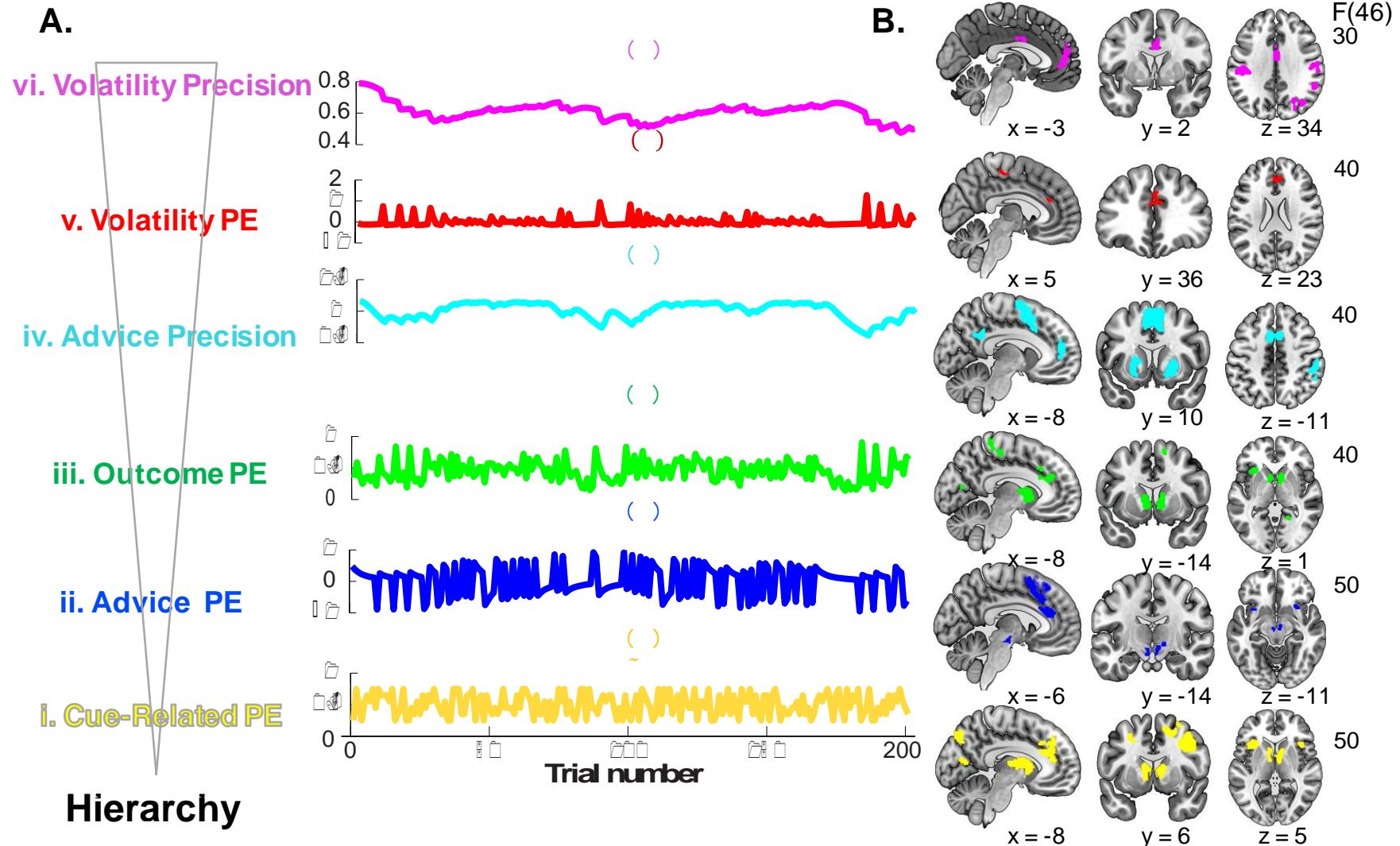


C. conjunction



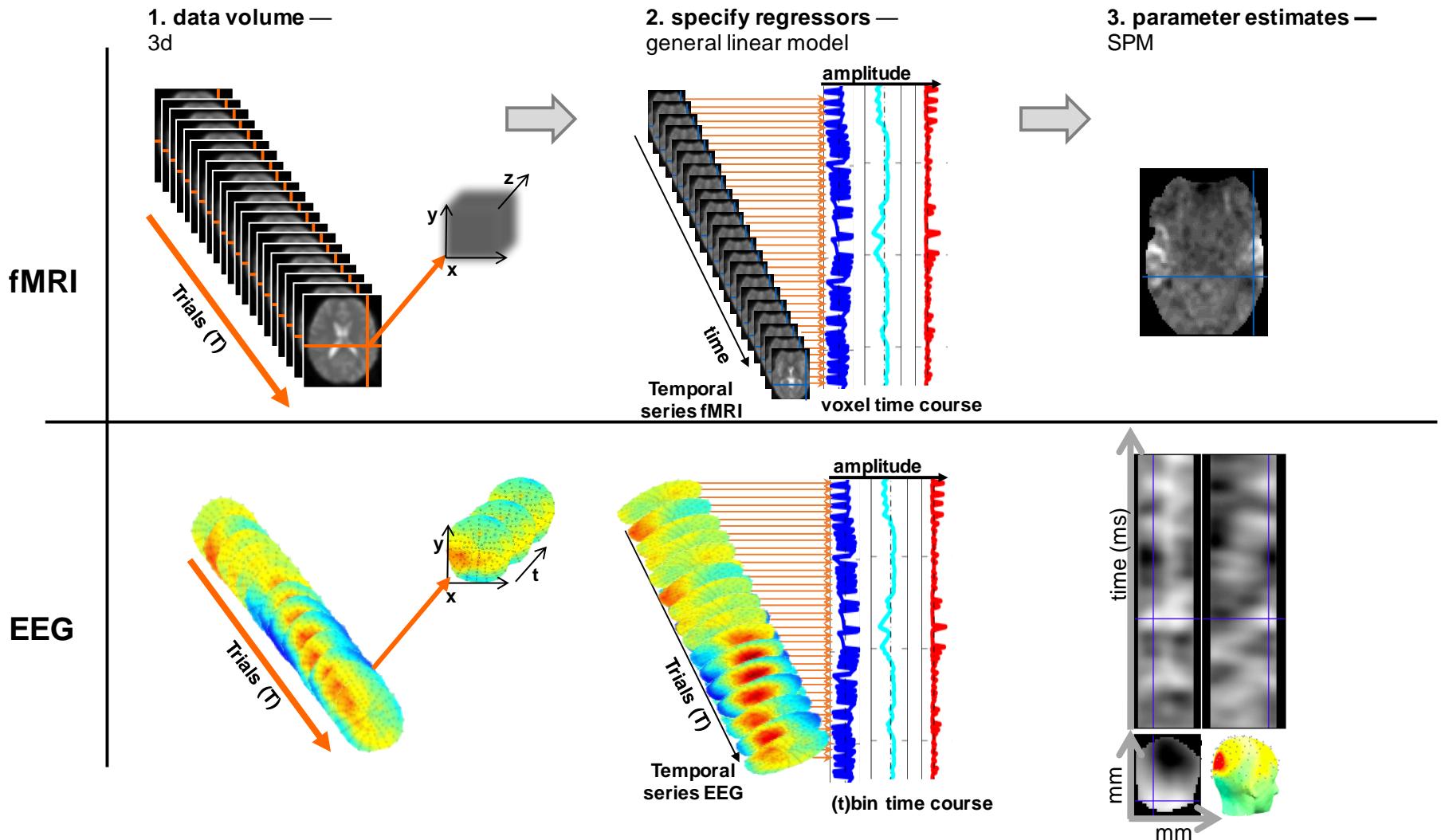
Diaconescu et al., *SCAN*, 2017

Computational hierarchy & its neural signature



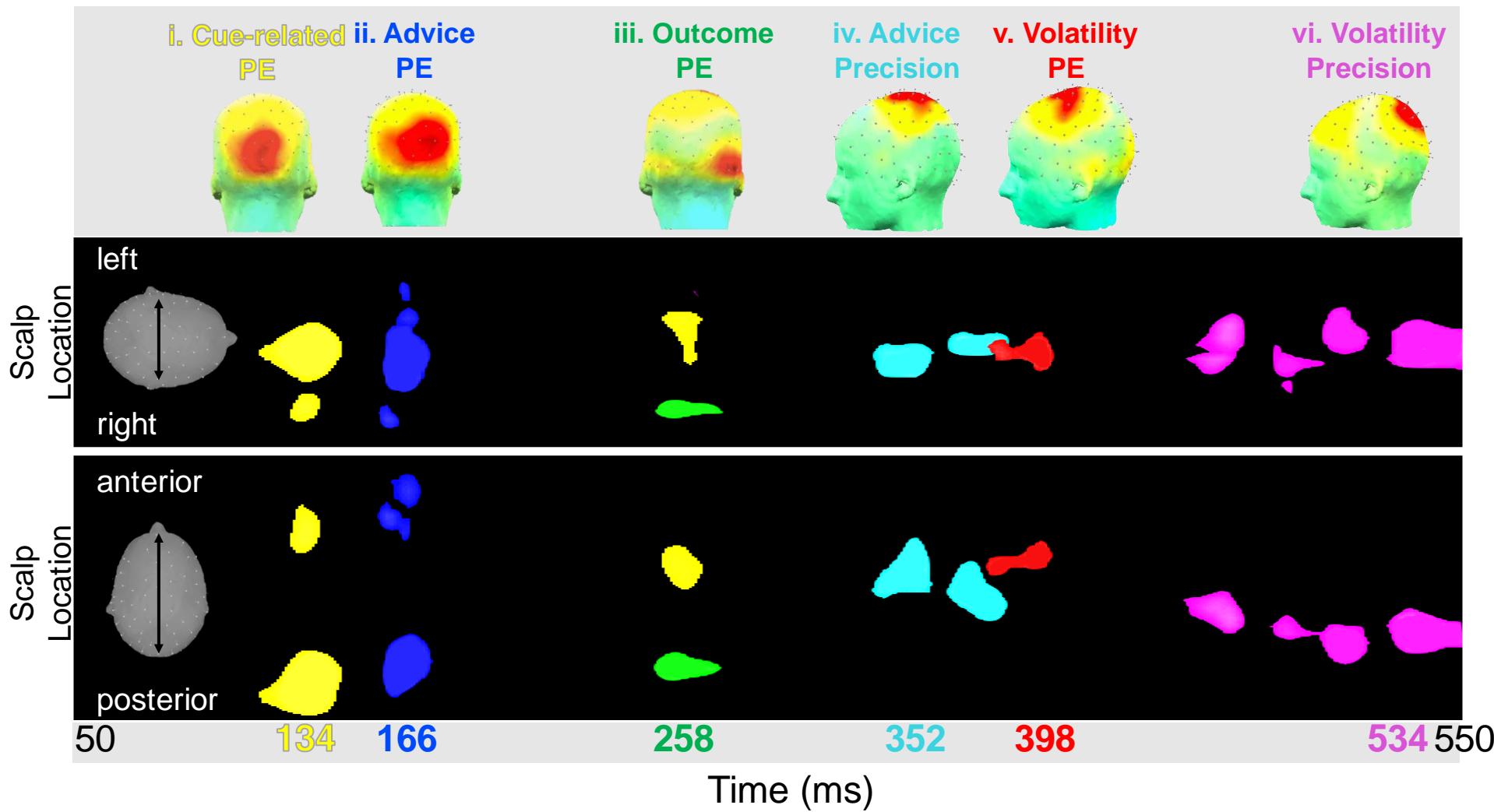
Diaconescu et al., Under Revision

Analogy to electrophysiological data



Diaconescu et al., Under Revision

Temporal hierarchy



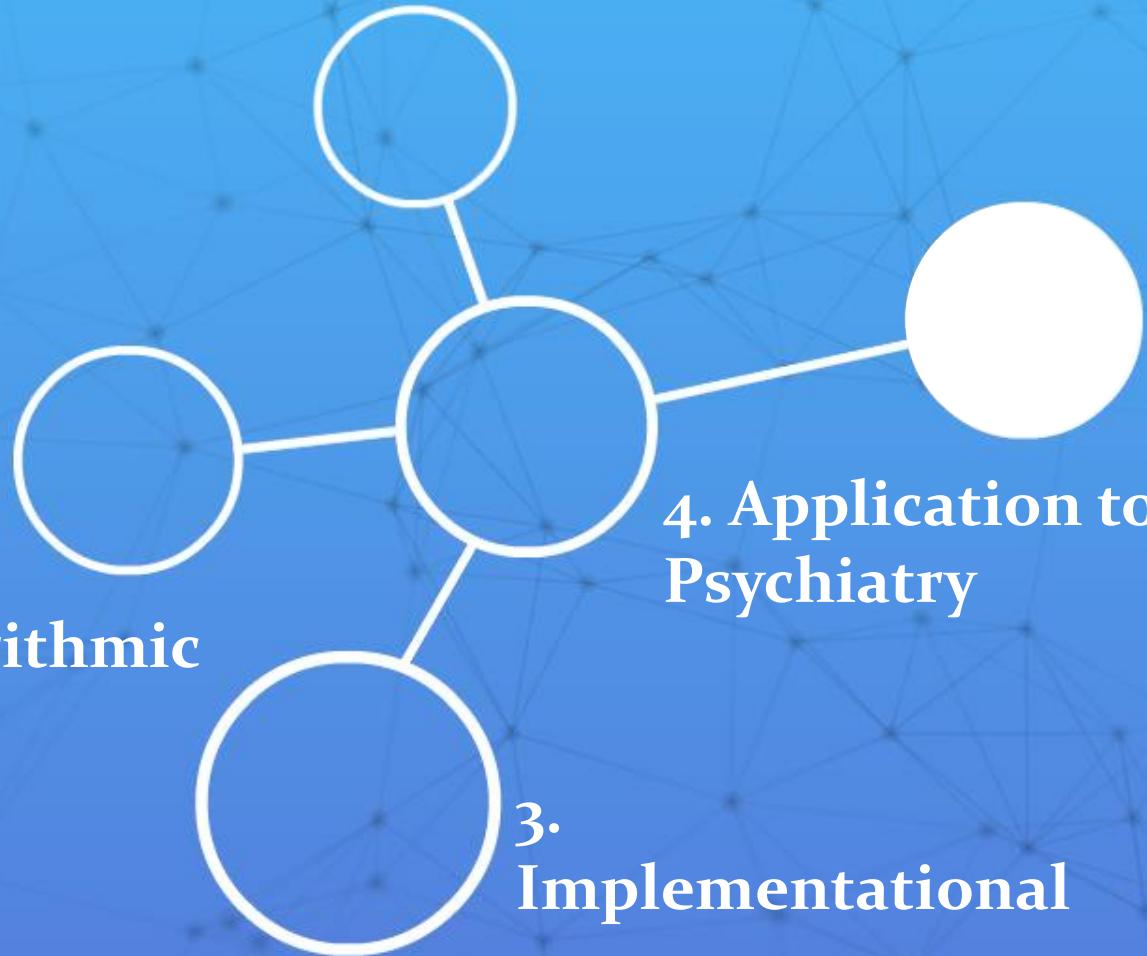
Diaconescu et al., Under Revision

Outline

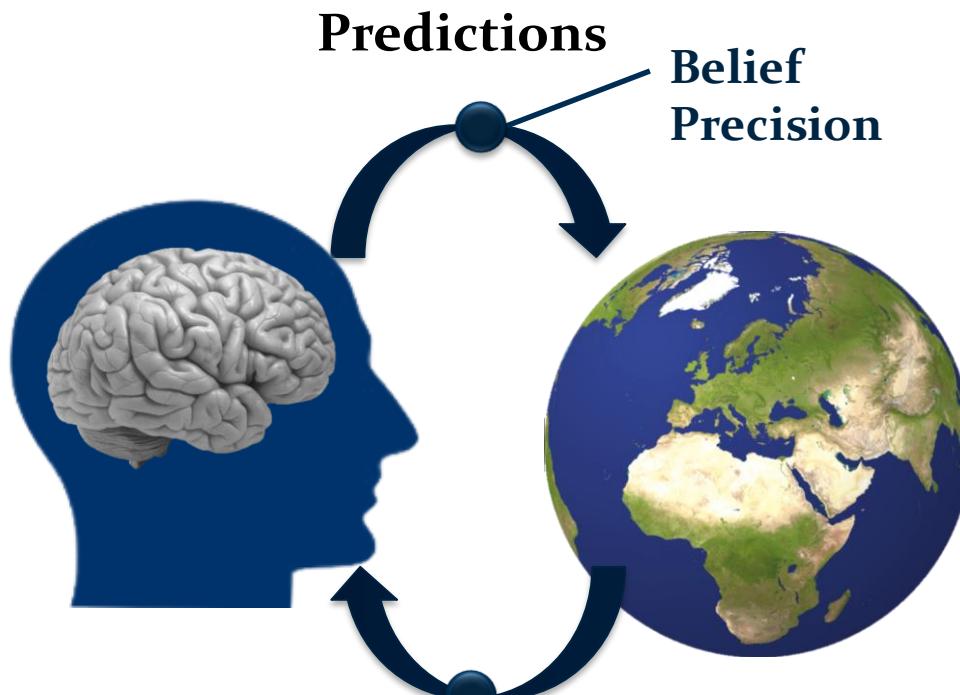
1. Computational

2.
Algorithmic

3.
Implementational
4. Application to Psychiatry



Hierarchical Gaussian Filter



Sensory
Precision

Prediction
Errors

$\Delta\mu_i^{(k)}$
Belief
Update

Belief
Precision

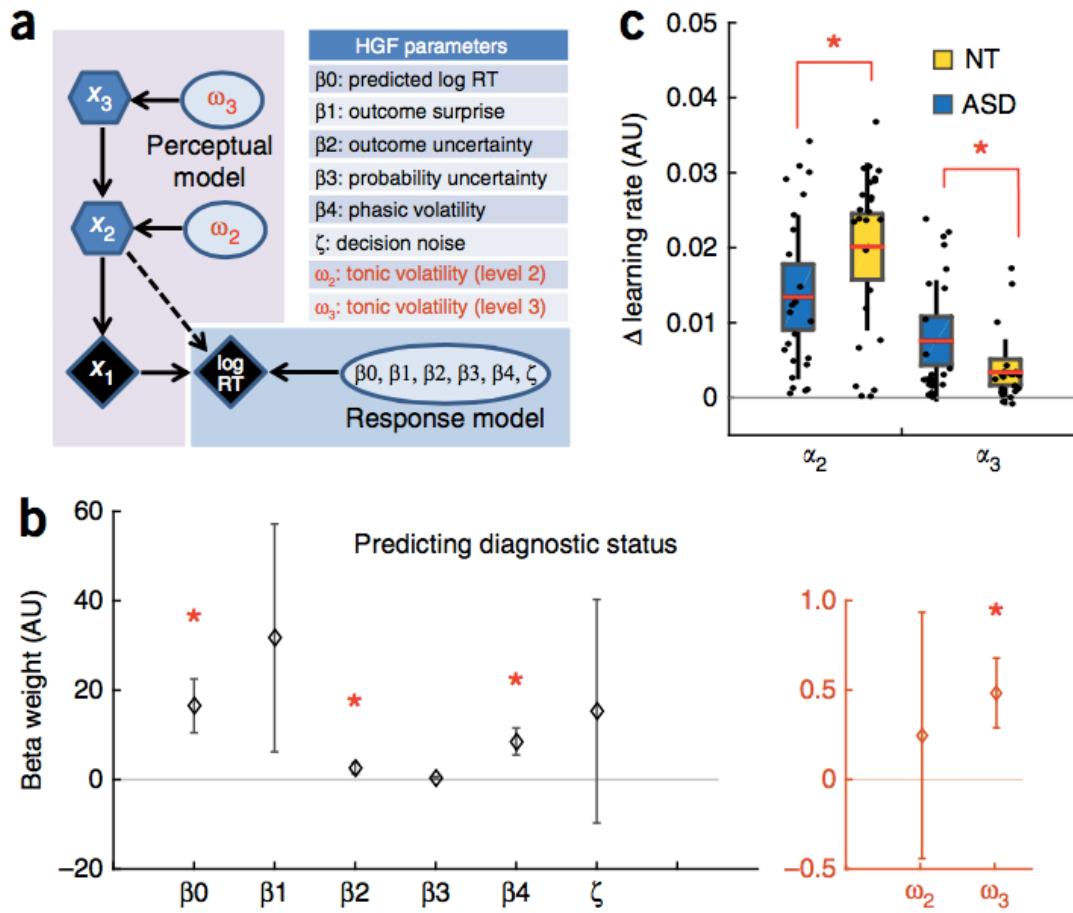
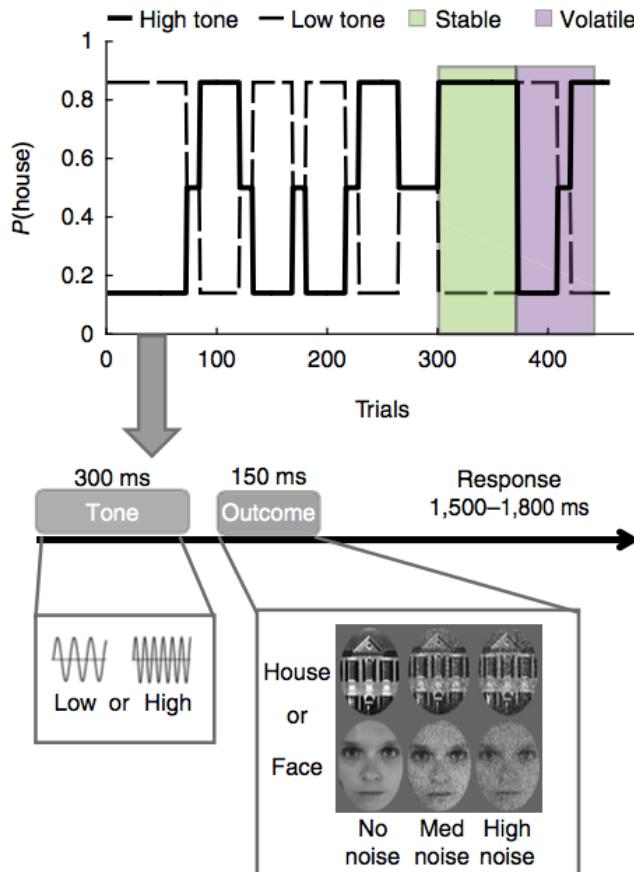
Sensory
Precision

$$\hat{\pi}_{i-1}^{(k)} \quad \text{Sensory Precision}$$
$$\pi_i^{(k)} \quad \text{Belief Precision}$$

$$\propto \frac{\hat{\pi}_{i-1}^{(k)}}{\pi_i^{(k)}} \delta_{i-1}^{(k)} \text{PE}$$

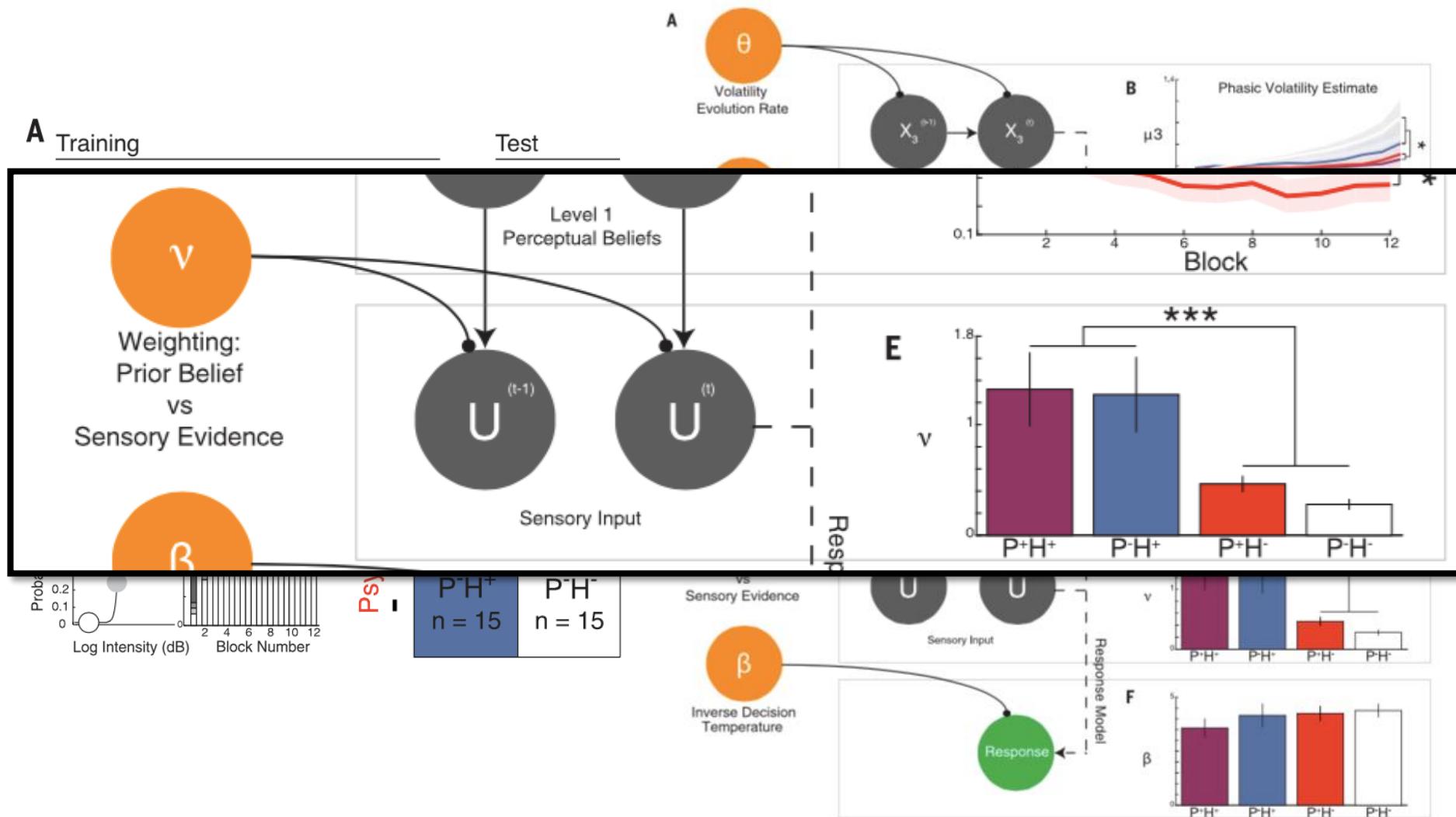
Mathys et al., *Frontiers Human Neurosci* 2011
Mathys et al., *Frontiers Human Neurosci* 2014

Autism



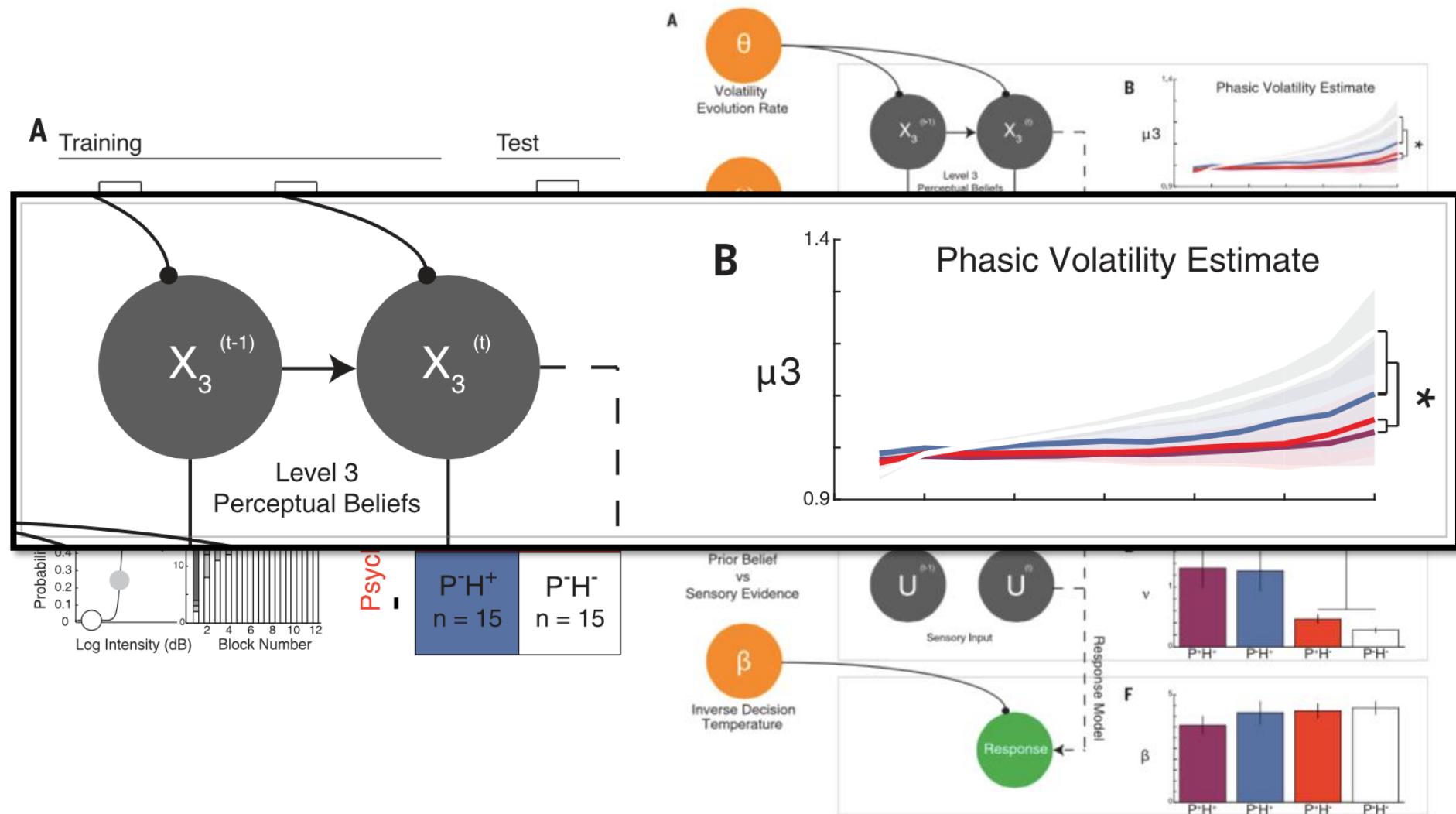
Lawson et al., *Nature Neuroscience*, 2017

Psychosis & Hallucinations



Powers et al., *Science*, 2017

Psychosis & Hallucinations



Powers et al., *Science*, 2017

Conclusion

Autism

$$\Delta\mu_i^{(k)} \propto \frac{\hat{\pi}_{i-1}^{(k)}}{\pi_i^{(k)}} \delta_{i-1}^{(k) \text{PE}}$$

Sensory Precision
Belief Update

3rd level of the hierarchy

Psychosis

$$\Delta\mu_i^{(k)} \propto \frac{\hat{\pi}_{i-1}^{(k)}}{\boldsymbol{\pi}_i^{(k)}} \delta_{i-1}^{(k) \text{PE}}$$

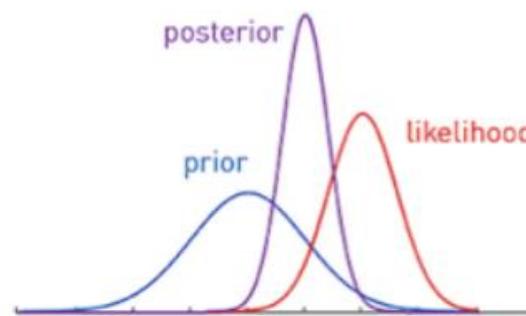
Sensory Precision
Belief Precision

2nd level of the hierarchy

Take-Home Message

Bayes' Theorem

$$p(x|y,m) = \frac{p(y|x,m)p(x|m)}{p(y|m)}$$

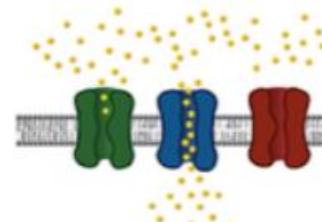


Generative models as computational assays



$$\xleftarrow[p(x|y,m)]{p(y|x,m)p(x|m)}$$

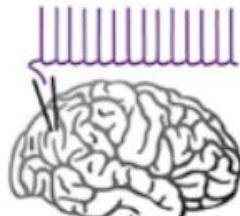
forward model
inference



measurement y

hidden system state x

Perception as the inversion of a generative model



$$\xleftarrow[p(x|y,m)]{p(y|x,m)p(x|m)}$$

forward model
perception



neuronal activity y

environmental state x

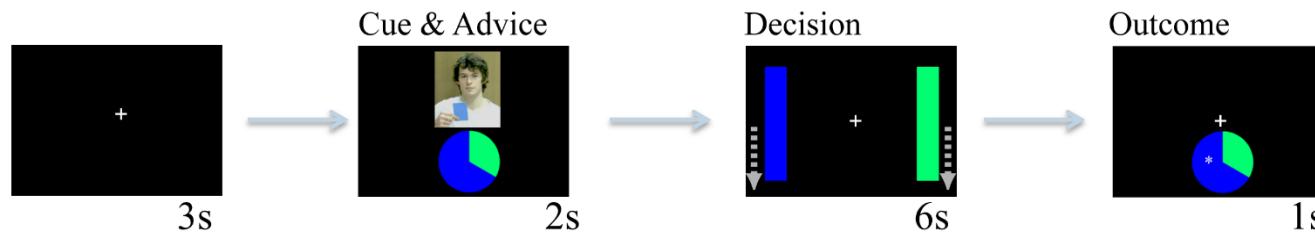
Stephan et al., *Frontiers Human Neurosci* 2016

References

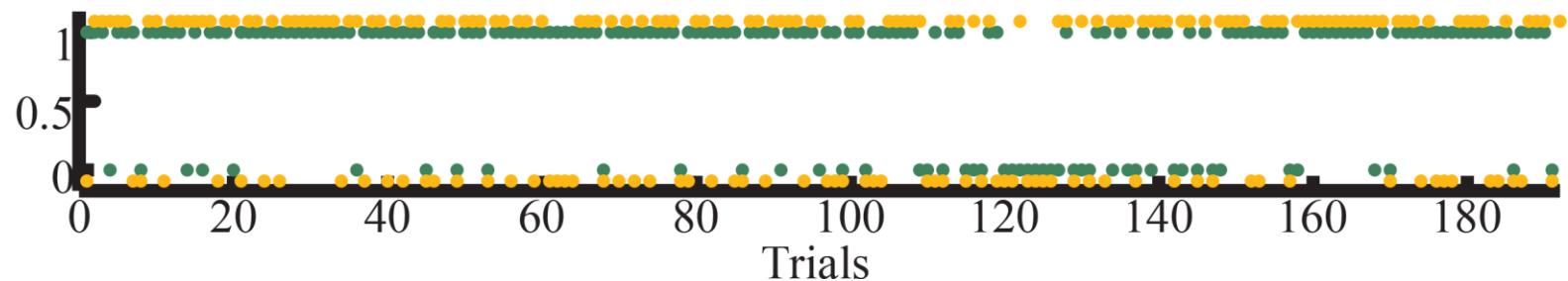
1. Daunizeau, J., den Ouden, H.E.M., Pessiglione, M., Kiebel, S.J., Stephan, K.E., and Friston, K.J. (2010). Observing the Observer (I): Meta-Bayesian Models of Learning and Decision-Making. *PLoS One* 5.
2. Diaconescu, A.O., Mathys, C., Weber, L.A.E., Kasper, L., Mauer, J., and Stephan, K.E. (2017). Hierarchical prediction errors in midbrain and septum during social learning. *Soc. Cogn. Affect. Neurosci.* 12, 618–634.
3. Iglesias, S., Mathys, C., Brodersen, K.H., Kasper, L., Piccirelli, M., den Ouden, H.E.M., and Stephan, K.E. (2013). Hierarchical Prediction Errors in Midbrain and Basal Forebrain during Sensory Learning. *Neuron* 80, 519–530.
4. Iglesias, S., Tomiello, S., Schneebeli, M., and Stephan, K.E. (2016). Models of neuromodulation for computational psychiatry. *Wiley Interdiscip. Rev. Cogn. Sci.*
5. Lawson, R.P., Mathys, C., and Rees, G. (2017). Adults with autism overestimate the volatility of the sensory environment. *Nat. Neurosci. advance online publication*.
6. Mathys, C., Daunizeau, J., Friston, K.J., and Stephan, K.E. (2011). A Bayesian foundation for individual learning under uncertainty. *Front Hum Neurosci* 5.
7. Mathys, C.D., Lomakina, E.I., Daunizeau, J., Iglesias, S., Brodersen, K.H., Friston, K.J., and Stephan, K.E. (2014). Uncertainty in perception and the Hierarchical Gaussian Filter. *Front. Hum. Neurosci.* 8.
8. Powers, A.R., Mathys, C., and Corlett, P.R. (2017). Pavlovian conditioning-induced hallucinations result from overweighting of perceptual priors. *Science* 357, 596–600.
9. Stephan, K.E., Manjaly, Z.M., Mathys, C.D., Weber, L.A.E., Paliwal, S., Gard, T., Tittgemeyer, M., Fleming, S.M., Haker, H., Seth, A.K., et al. (2016). Allostatic Self-efficacy: A Metacognitive Theory of Dyshomeostasis-Induced Fatigue and Depression. *Front. Hum. Neurosci.* 10.

How do we construct regressors that correspond to cognitive processes and use them in SPM?

1. Pass individual subject trial history into SPM:



Response y (orange=1 advice was taken), input u (green=1 advice was accurate)



How do we construct regressors that correspond to cognitive processes and use them in SPM?

2. Estimated subject-by-subject model parameters:

- Model Inversion:

```
running model/param combination 4 of 546
Irregular trials: none
Ignored trials: none
Irregular trials: none

Optimizing...

Calculating the negative free energy...

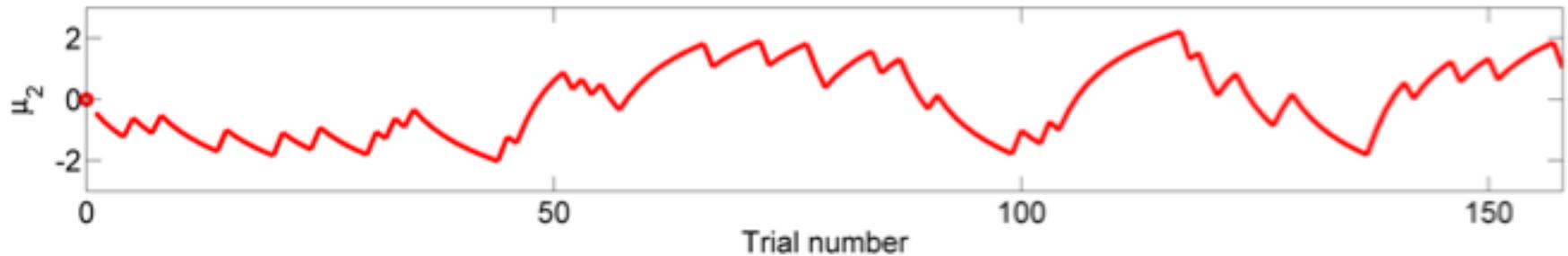
Results:
    mu2_0: 1.0665
    sa2_0: 1.4966
    mu3_0: 1
    sa3_0: 1
    ka: 0
    om: -10
    th: 1.0000e-18
    p: [1.0665 1.4966 1 1 0 -10 1.0000e-18]
ptrans: [1.0665 0.4032 1 0 -22.3327 -10 -34.5388]

    ze1: 0.8816
    ze2: 48.0000
    p: [0.8816 48.0000]
ptrans: [2.0073 3.8712]

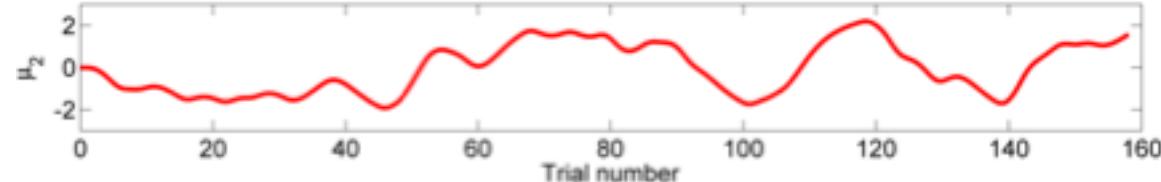
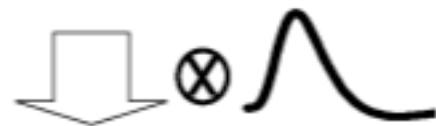
Negative free energy F: -82.9603
```

How do we construct regressors that correspond to cognitive processes and use them in SPM?

3. Generate model-based time-series:



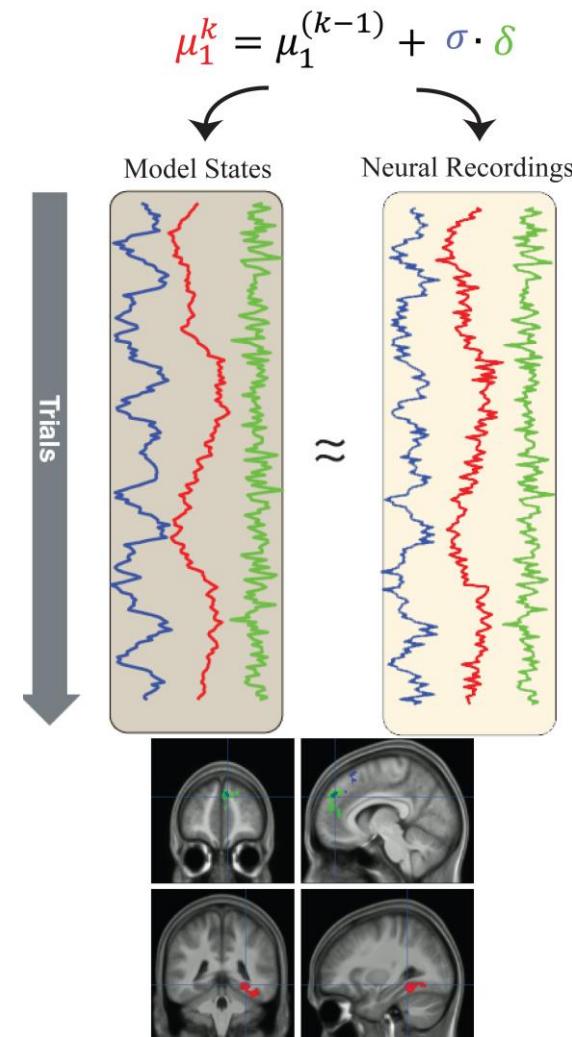
3. Convolve them with HRF:



Adapted from O'Doherty et al., 2007

How do we construct regressors that correspond to cognitive processes and use them in SPM?

5. Construct your GLM:



Adapted from Behrens et al., 2010

Estimate: single subject

6. First-level analysis:

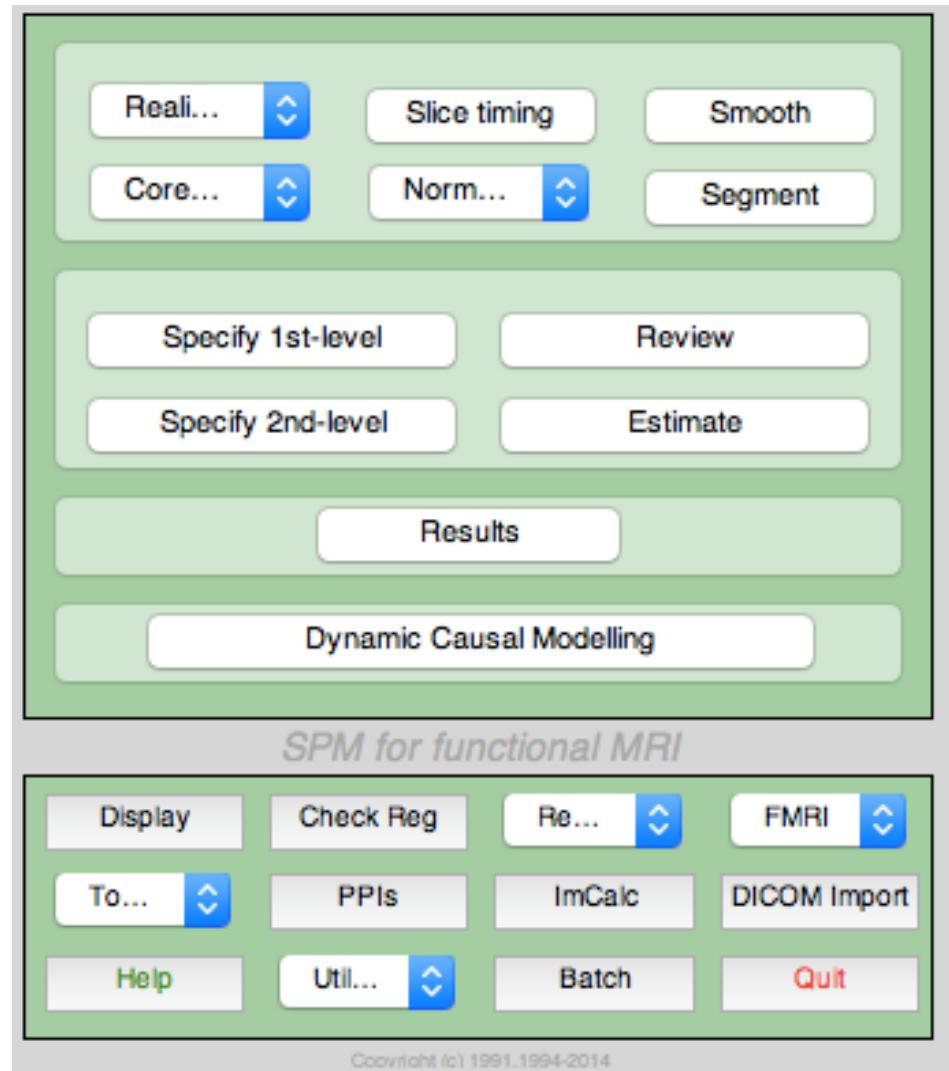
- Load your regressors:

```
reg1 =  
[1x189 double]  
[1x189 double]  
[1x189 double]  
  
mu1hat <1x189 double>  
positive_PE <1x189 double>
```

Estimate: single subject

6. First-level analysis:

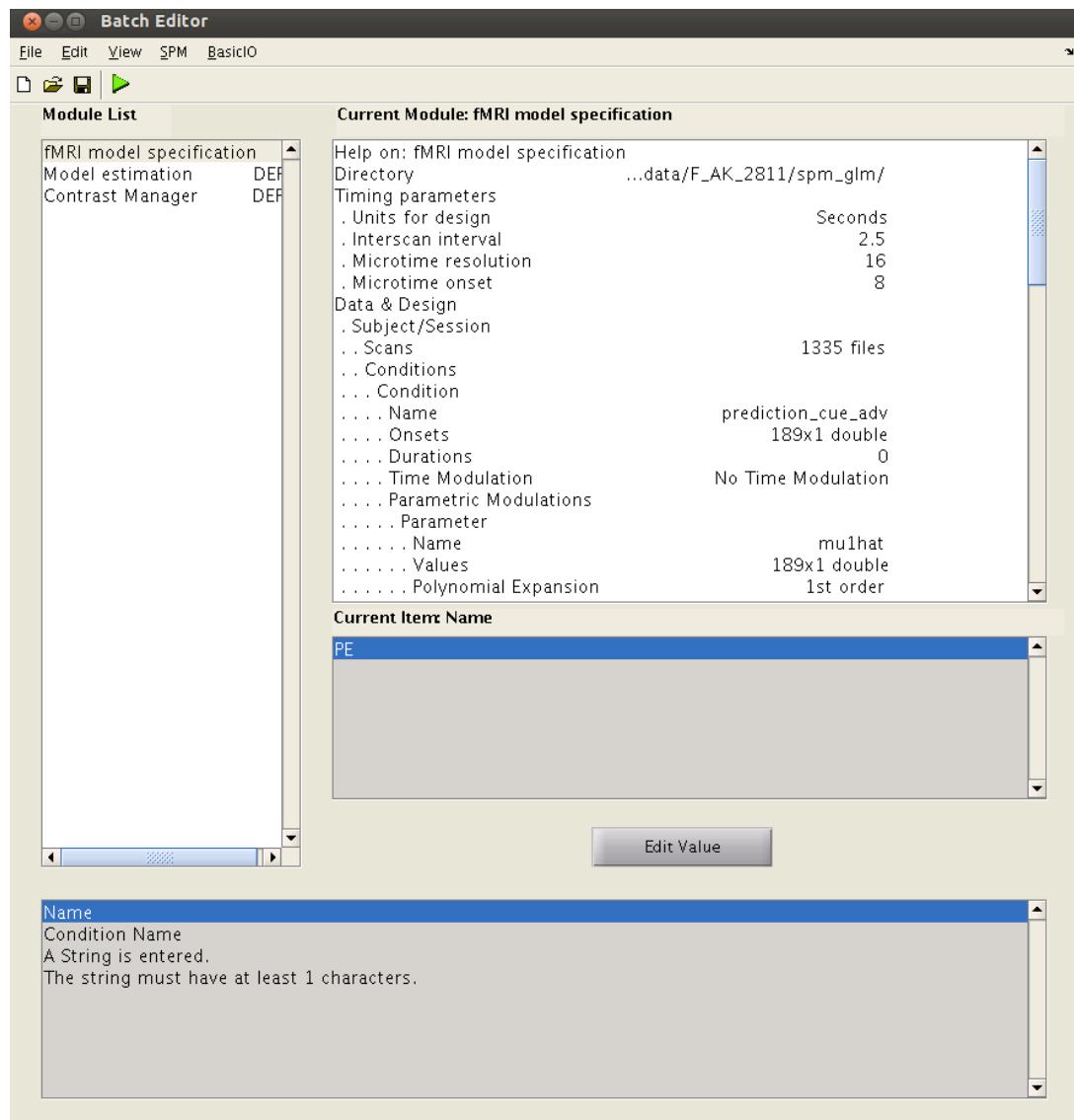
- Open SPM: Specify first level analysis



Estimate: single subject

6. First-level analysis:

- Load Design matrix into Batch editor



Estimate: single subject

6. First-level analysis:

- Examine results:
 - PE

