



University of  
Zurich <sup>UZH</sup>

**ETH**

Eidgenössische Technische Hochschule Zürich  
Swiss Federal Institute of Technology Zurich



Translational Neuromodeling Unit

## Methods & Models for fMRI Analysis 2018

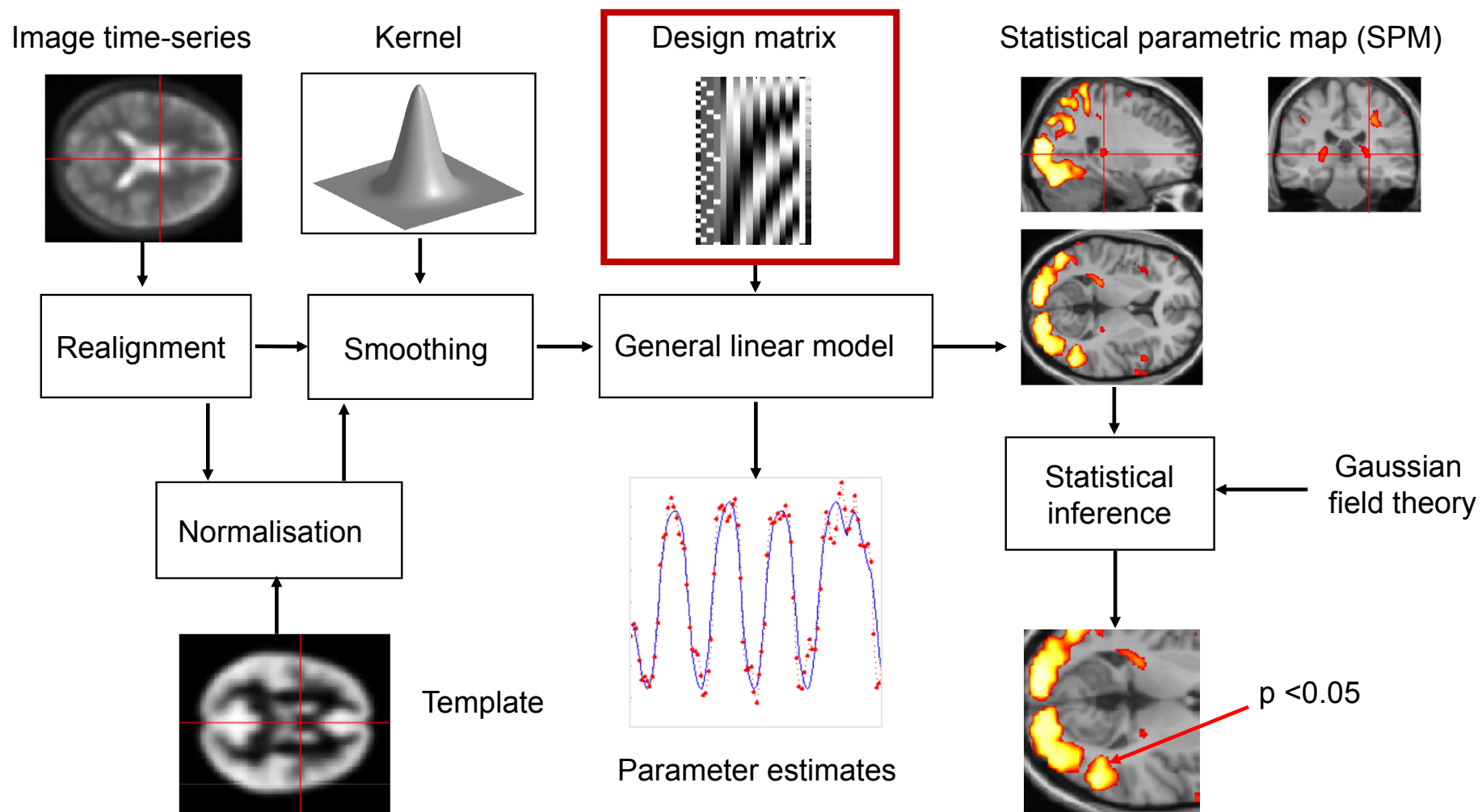
# Experimental design of fMRI studies

Jakob Heinzle, Sara Tomiello

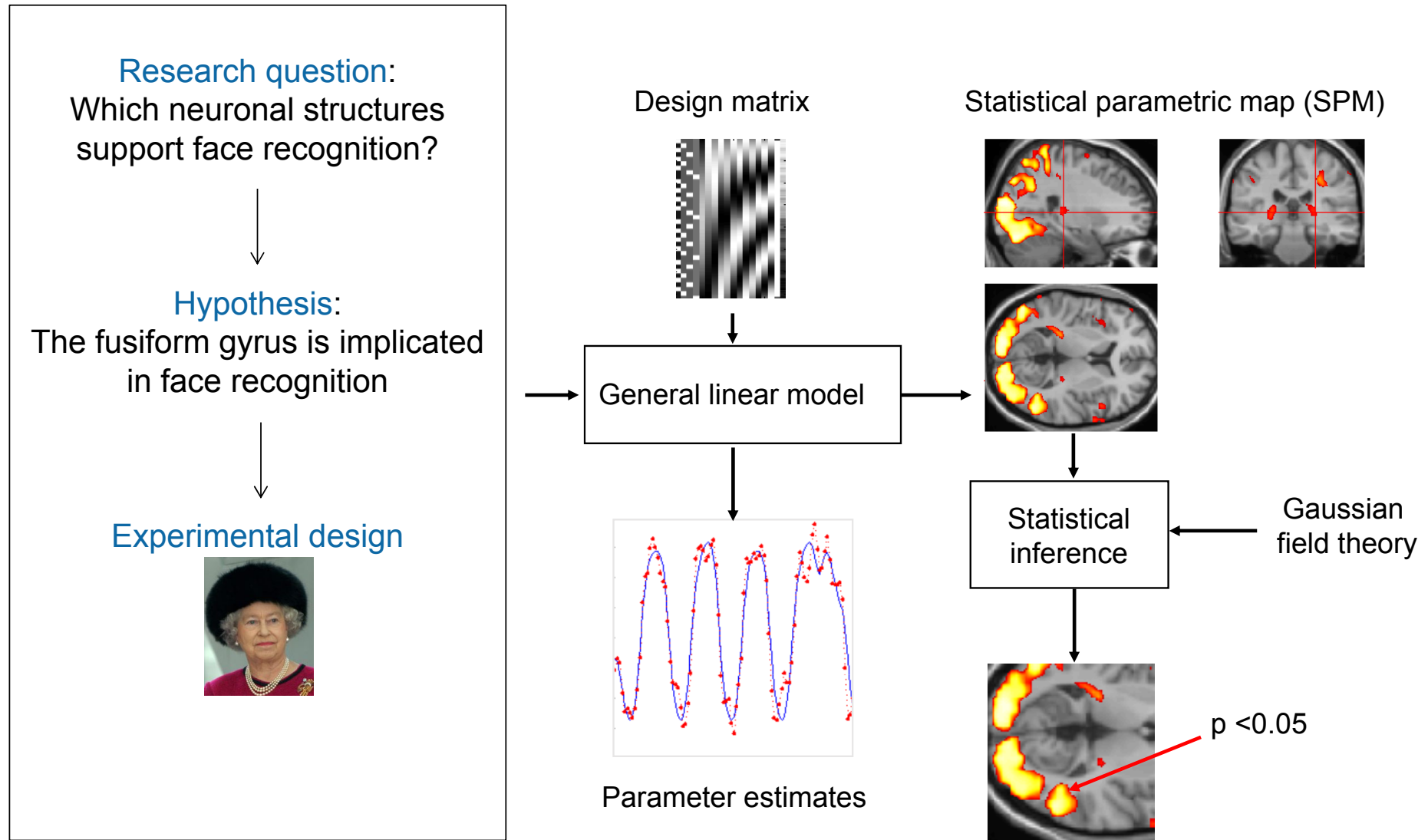
With many thanks for slides & images to:

Sara Tomiello,  
Sandra Iglesias,  
Klaas Enno Stephan,  
FIL Methods group,  
Christian Ruff

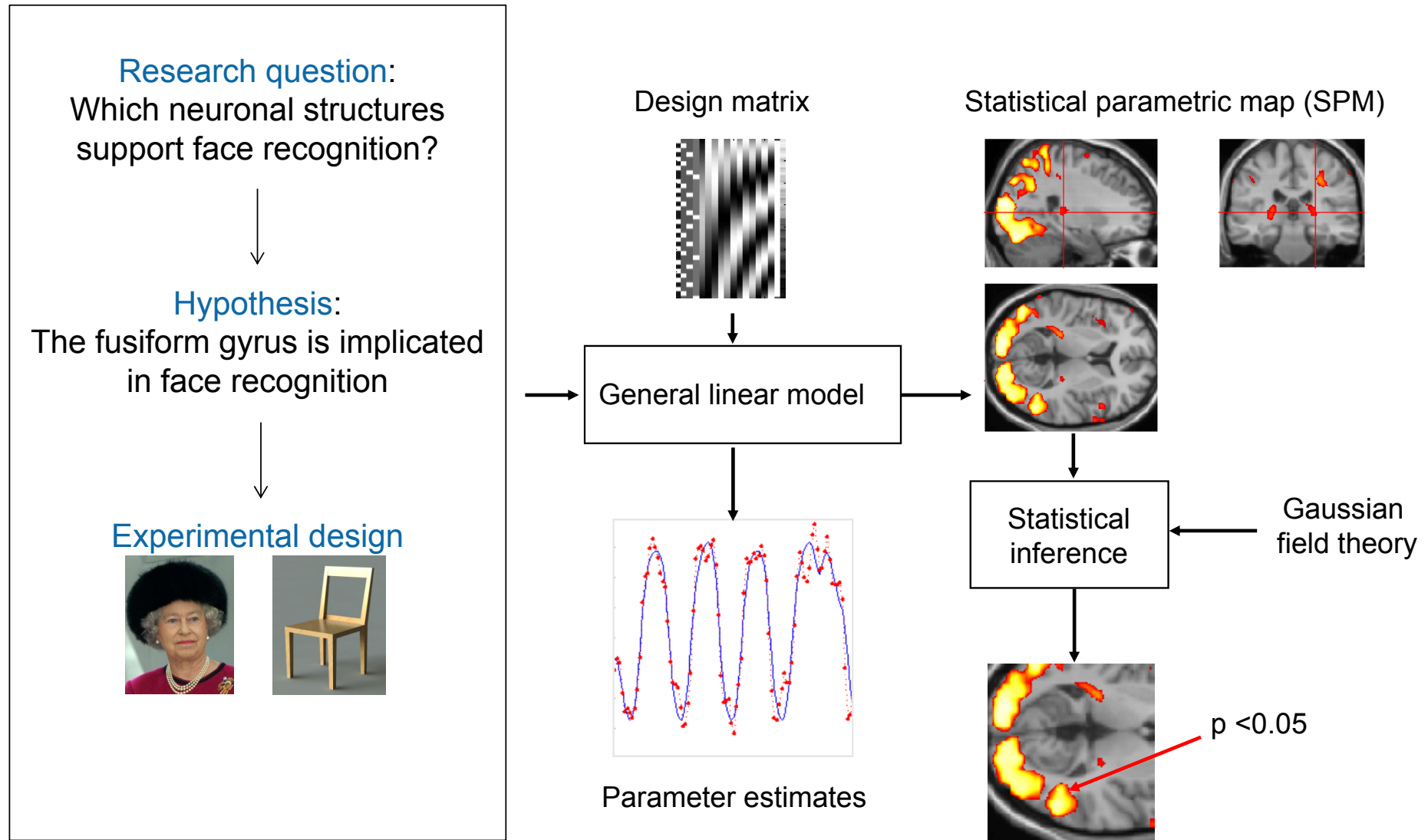
# Overview of SPM



# Overview of SPM



# Overview of SPM



# Overview Experimental Designs

- Categorical designs

- Subtraction - Pure insertion, evoked / differential responses
- Conjunction - Testing multiple hypotheses

- Parametric designs

- Linear - Adaptation, cognitive dimensions
- Nonlinear - Polynomial expansions, neurometric functions

- Factorial designs

- Categorical - Interactions and pure insertion
- Parametric - Linear and nonlinear interactions
- Psychophysiological interactions

# Categorical Designs

## Subtraction

- Aim: Find neuronal structures underlying a *single* process  $P$
- Procedure: Under the critical assumption of „pure insertion“

$$[\text{task with } P] - [\text{control task without } P] = P$$

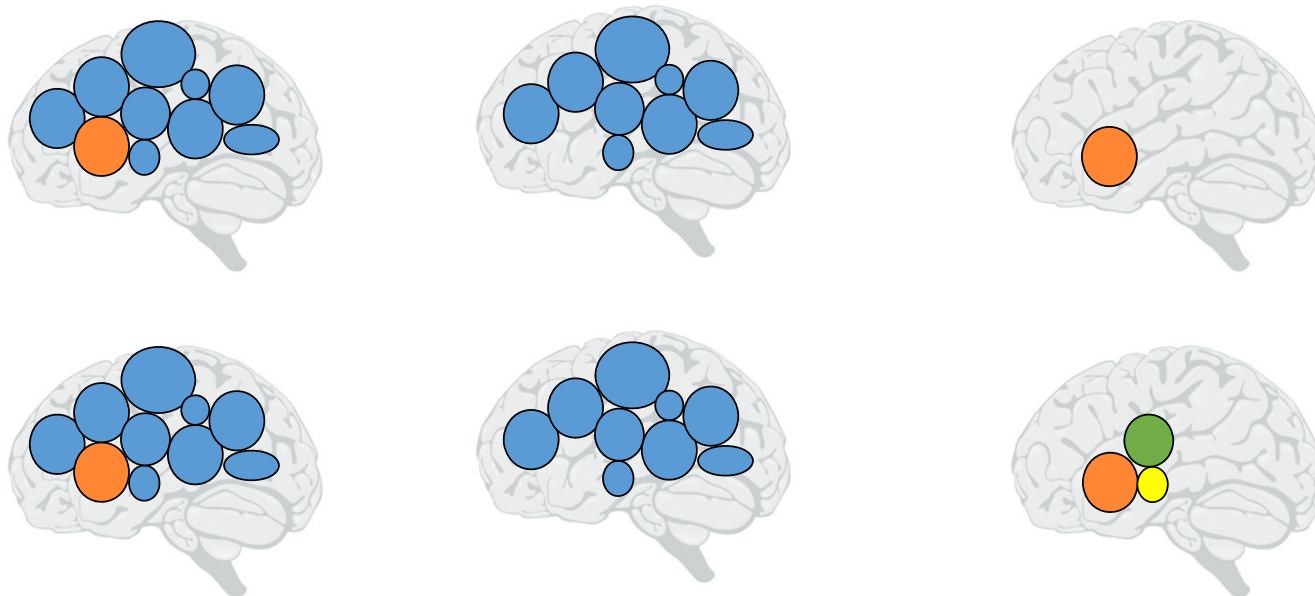


# Categorical Designs

## Subtraction

- Aim: Find neuronal structures underlying a *single* process  $P$
- Procedure: Under the critical assumption of „pure insertion“

$$[\text{task with } P] - [\text{control task without } P] = P$$



# Categorical Designs

## Subtraction, Example

Cognitive subtraction originated with reaction time experiments (F. C. Donders).

Measure the time for a process to occur by comparing two reaction times, one which has the same components as the other + the process of interest.

Example:

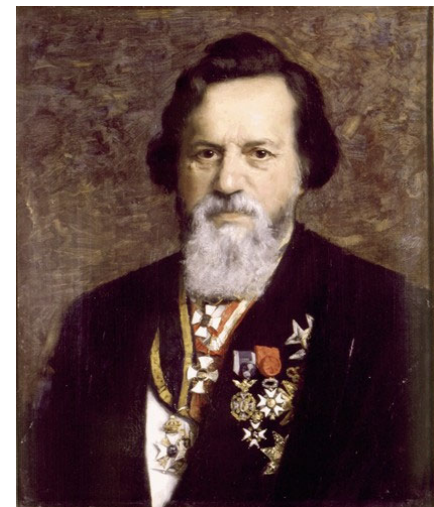
T1: Hit a button when you see a light

T2: Hit a button when the light is green but not red

T3: Hit the left button when the light is green and the right button when the light is red

$T2 - T1$  = time to make discrimination between light color

$T3 - T2$  = time to make a decision



*F.C. Donders 1868*

**Assumption of pure insertion:**

You can insert a component process into a task without disrupting the other components.



# Categorical Designs

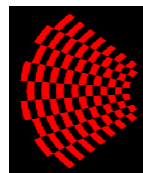
## Subtraction: Baseline problem

Which neuronal structures support face recognition ?

- „Distant“ stimuli



-



→ Several components differ

- „Related“ stimuli



-



„Queen!“

„Aunt Jenny?“

→ Additional processes in control condition (?)

- Same stimuli, different task



-



Name Person!

Name Gender!

→ Interaction of task and stimuli (specificity for naming)  
(i.e. do task differences depend on stimuli chosen (??))

# Categorical Designs

## Subtraction, Example

### Experimental design

Face viewing: F

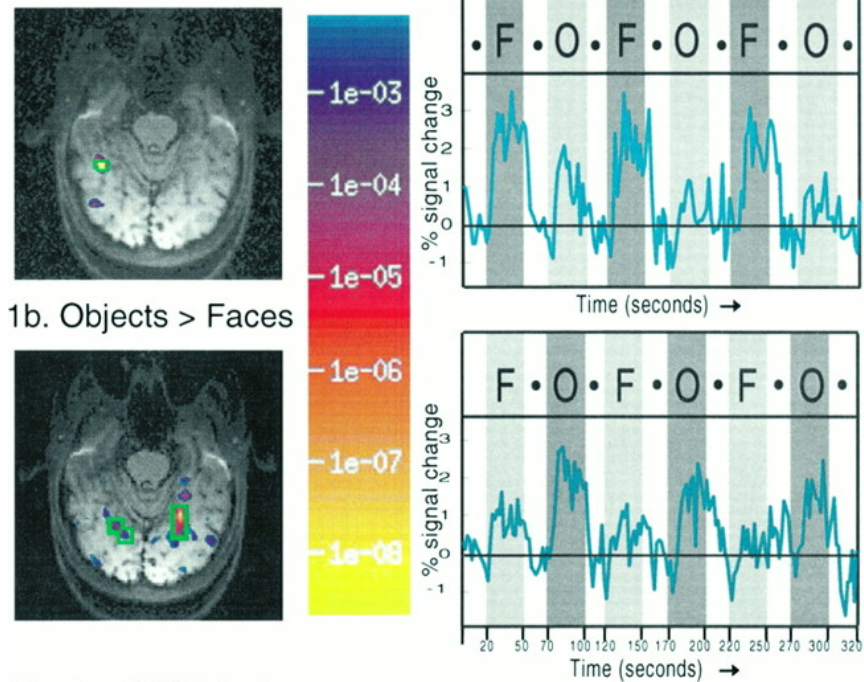
Object viewing: O

F - O = Face recognition

O - F = Object recognition

...under assumption of pure insertion

1a. Faces > Objects



# Categorical Designs

Subtraction, Example SPM

The SPM contrast manager dialog box is titled "define contrast...". It contains the following fields and controls:

- name:** A1-A2
- type:** ☒ t-contrast, ☐ F-contrast
- contrast:** A text area containing the vector `1 -1 1 1 -1 1 -1 -1`. Below it is a "...subset" button.
- Design matrix:** A large matrix visualization. Above it is a "contrast(s)" bar with a checkerboard pattern. Below it is a "parameter estimability" bar with 10 white boxes.
- Buttons:** Reset, Cancel, and OK.
- Status bar:** name defined, contrast defined

Annotations on the right side of the image point to specific parts of the Design matrix:

- Task 1:** Points to the first row of the Design matrix.
- Task 2:** Points to the second row of the Design matrix.
- Session:** Points to the third row of the Design matrix.

# Overview Experimental Designs

- Categorical designs

Subtraction      - Pure insertion, evoked / differential responses

**Conjunction      - Testing multiple hypotheses**

- Parametric designs

Linear              - Adaptation, cognitive dimensions

Nonlinear          - Polynomial expansions, neurometric functions

- Factorial designs

Categorical        - Interactions and pure insertion

Parametric        - Linear and nonlinear interactions

- Psychophysiological interactions

# Categorical Designs

## Conjunction

- One way to minimize the baseline/pure insertion problem is to isolate the same process by **two or more separate comparisons**, and inspect the resulting simple effects for commonalities
- A test for such activation common to several independent contrasts is called “conjunction”
- Conjunctions can be conducted across a whole variety of different contexts:
  - tasks
  - stimuli
  - senses (vision, audition)
  - etc.
- Note: the contrasts entering a conjunction must be **orthogonal**

# Categorical Designs

## Conjunction, Example

Which neural structures support object recognition, independent of task (naming vs. viewing)?

		Task (1/2)	
		Viewing	Naming
Stimuli (A/B)	Colours	A1	A2
	Objects	B1	B2

Visual Processing:  
Object Recognition:  
Phonological Retrieval:

V  
R  
P

# Categorical Designs

## Conjunction, Example

Which neural structures support object recognition, independent of task (naming vs. viewing)?

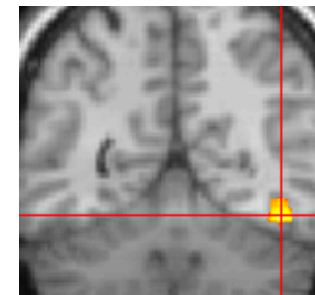
		Task (1/2)	
		Viewing	Naming
Stimuli (A/B)	Colours	<b>A1</b> Visual Processing V	<b>A2</b> Visual Processing Phonological Retrieval V P
	Objects	<b>B1</b> Visual Processing Object Recognition V R	<b>B2</b> Visual Processing Phonological Retrieval Object Recognition V P R

(Object - Colour viewing) [B1 - A1]

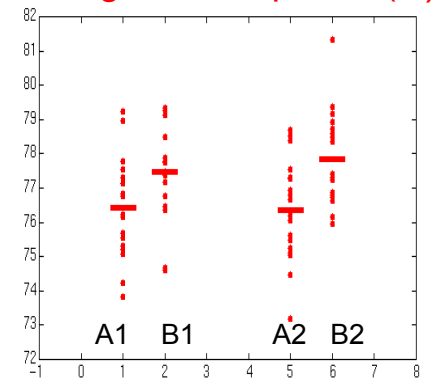
&

(Object - Colour naming) [B2 - A2]

[ V,R - V ] & [ P,V,R - P,V ] = R & R = **R**



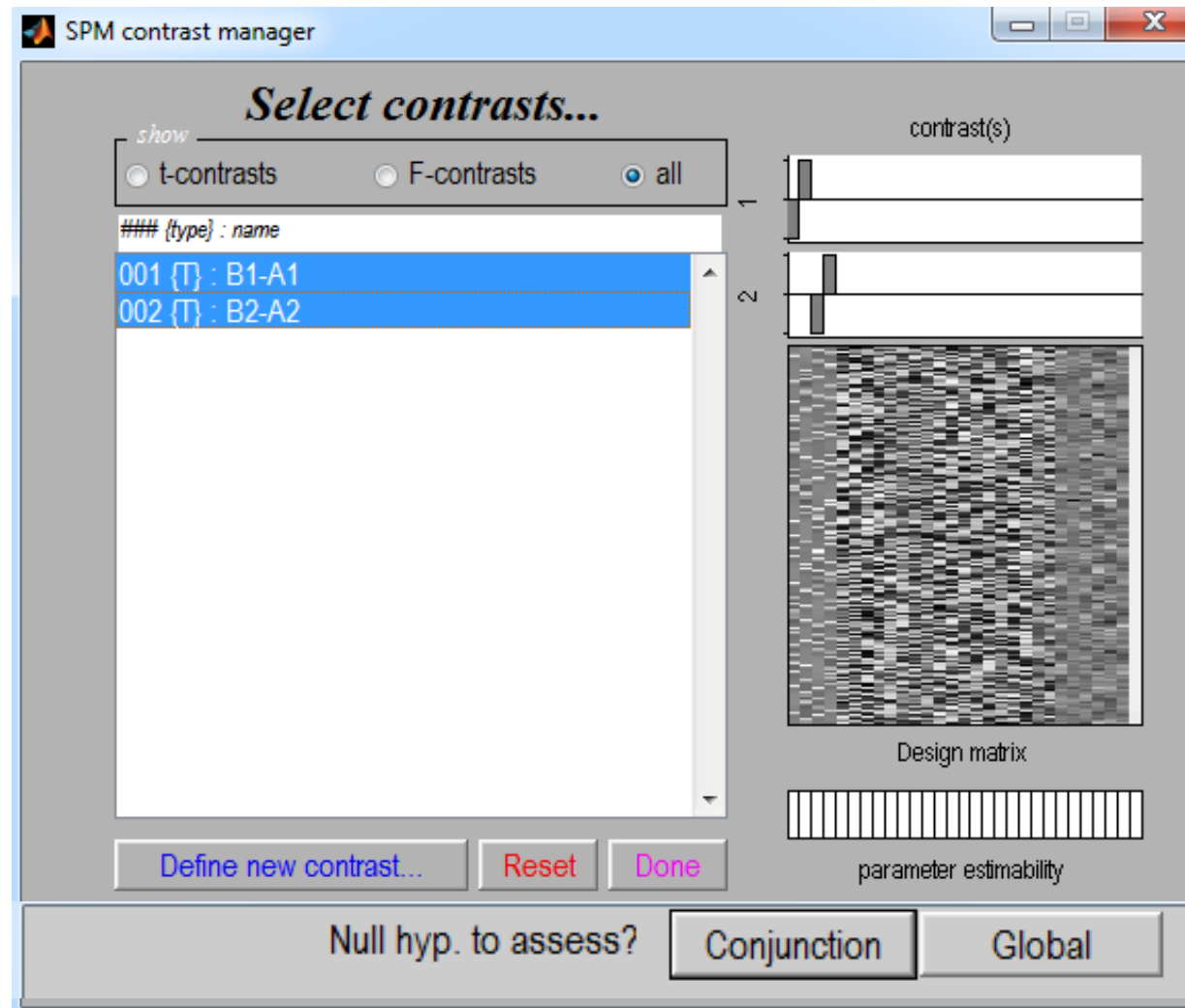
Common object  
recognition response (R)



Price et al. 1997, NeuroImage

# Categorical Designs

Conjunction, Example SPM

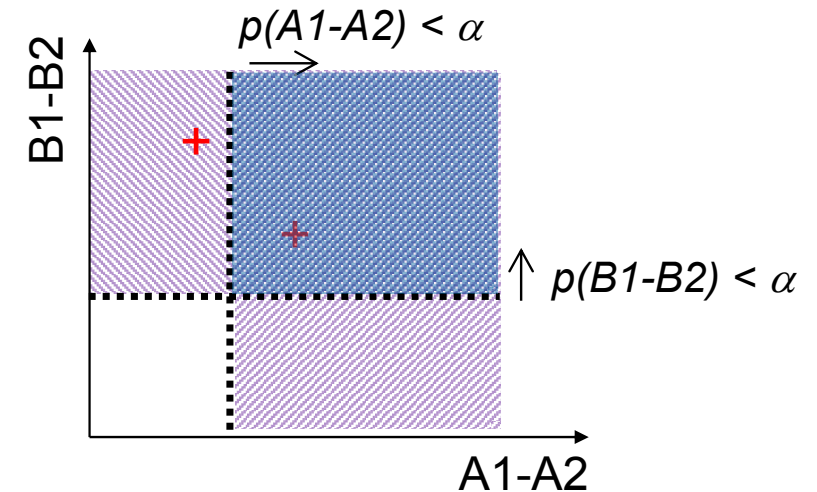




# Categorical Designs

## Types of Conjunctions

- Test of **global null hypothesis**:  
Significant set of consistent effect
  - “Which voxels show effects of similar direction (but not necessarily individual significance) across contrasts?”
  - $H_1: k > 0$
  - $H_0$ : No contrast is significant:  $k = 0$
  - Does **not** correspond to a logical AND !
- Test of **conjunction null hypothesis**:  
Set of consistently significant effects
  - “Which voxels show, for each specified contrast, significant effects?”
  - $H_1: k = n$
  - $H_0$ : Not all contrasts are significant:  $k < n$
  - Corresponds to a logical AND



$k$  = effects  
 $n$  = contrasts

Friston et al., 2005, NeuroImage  
 Nichols et al., 2005, NeuroImage

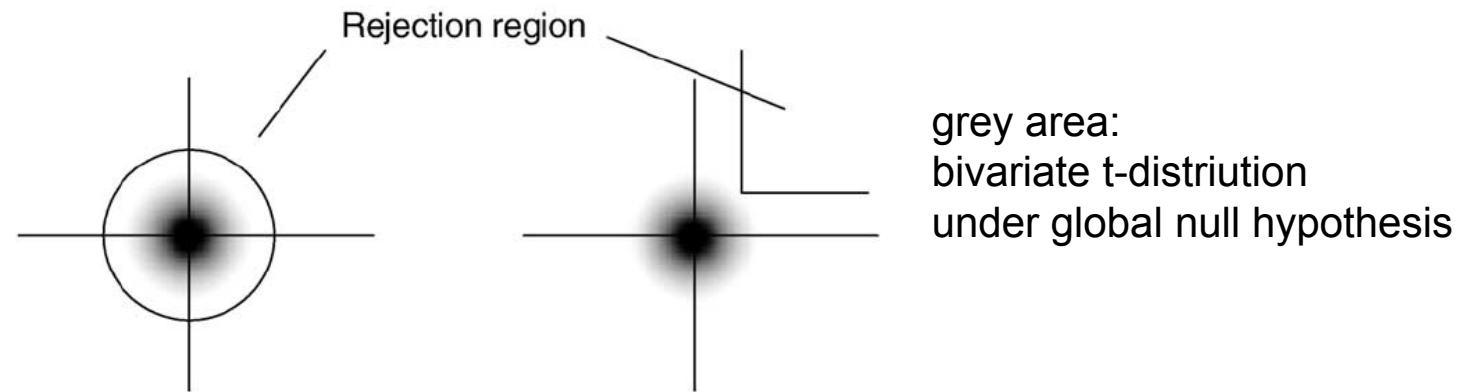
# Categorical Designs

## Conjunction, Global Null Hypothesis

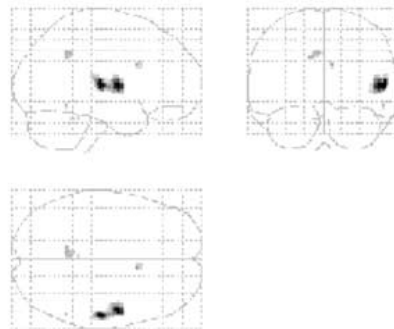
- Based on the "minimum t statistic":
  - imagine a voxel where contrast A gives  $t=1$  and contrast B gives  $t=1.4$
  - neither t-value is significant alone, but the fact that both values are **larger than zero** suggests that there may be a real effect
- Test: compare the observed minimum t value to the null distribution of minimal t-values for a given set of contrasts
  - assuming independence between the tests, one can find **uncorrected and corrected thresholds** for a minimum of two or more t-values (Worsley & Friston, Stat. Probab. Lett., 2000, 47 (2), 135–140)
  - this means the contrasts have to be orthogonal!

# Categorical Designs

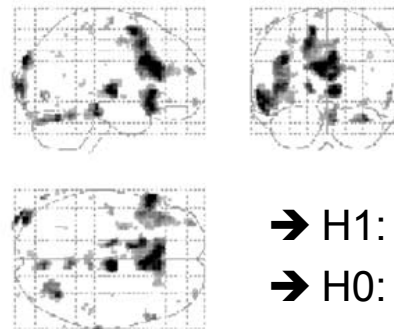
F-test vs. Conjunction based on global null



F-test



Conjunction



→  $H_1: k > 0$

→  $H_0$ : No contrast is significant:  $k = 0$

# Overview Experimental Designs

- Categorical designs

- Subtraction - Pure insertion, evoked / differential responses
- Conjunction - Testing multiple hypotheses

- **Parametric designs**

- Linear - Adaptation, cognitive dimensions
- Nonlinear - Polynomial expansions, neurometric functions

- Factorial designs

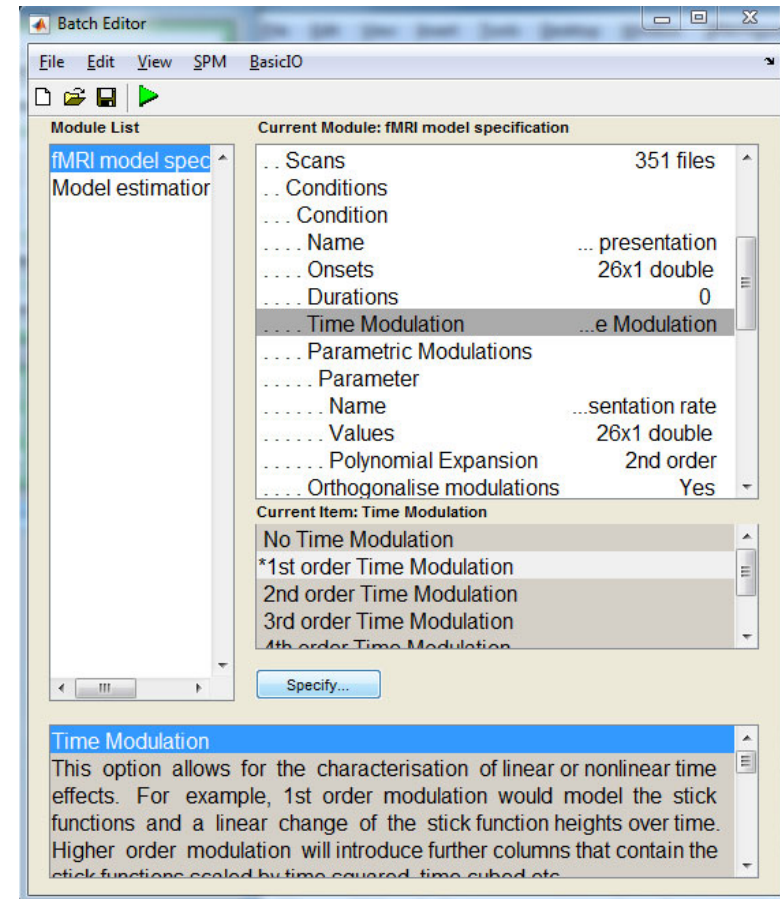
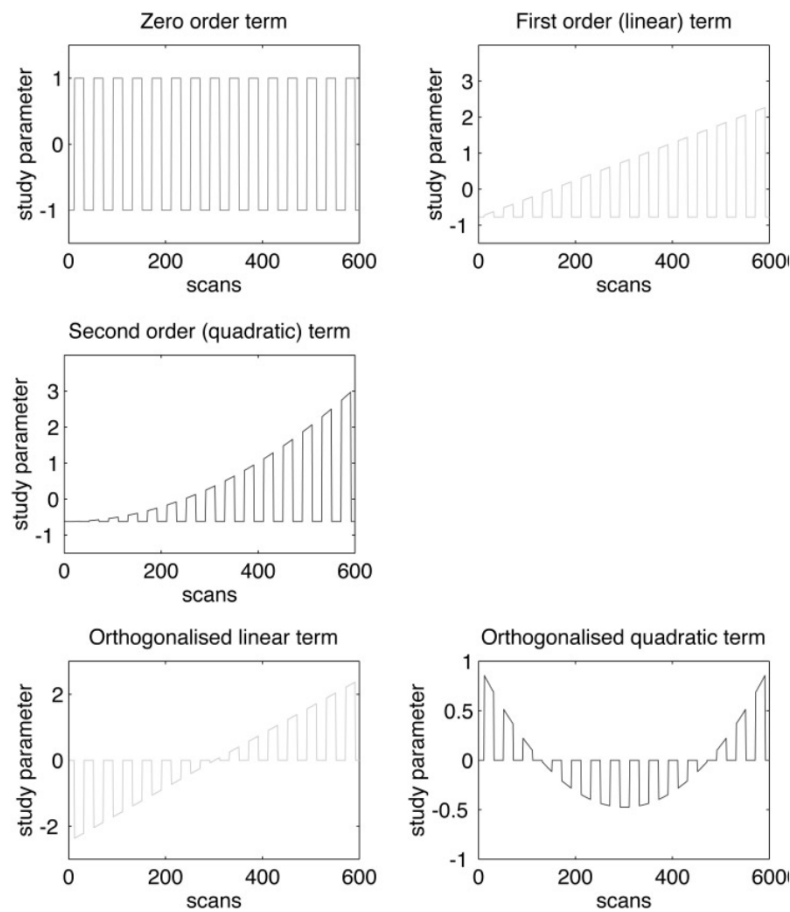
- Categorical - Interactions and pure insertion
- Parametric - Linear and nonlinear interactions
- Psychophysiological interactions

# Parametric Designs

- Parametric designs approach the baseline problem by:
  - varying the stimulus-parameter of interest on a **continuum, in multiple ( $n > 2$ ) steps...**
  - ... and relating measured BOLD signal to this parameter
- Possible tests for such relations are manifold:
  - Linear
  - Nonlinear: Quadratic/cubic/etc. (polynomial expansion)
  - Model-based (e.g. predictions from learning models)

# Parametric Designs

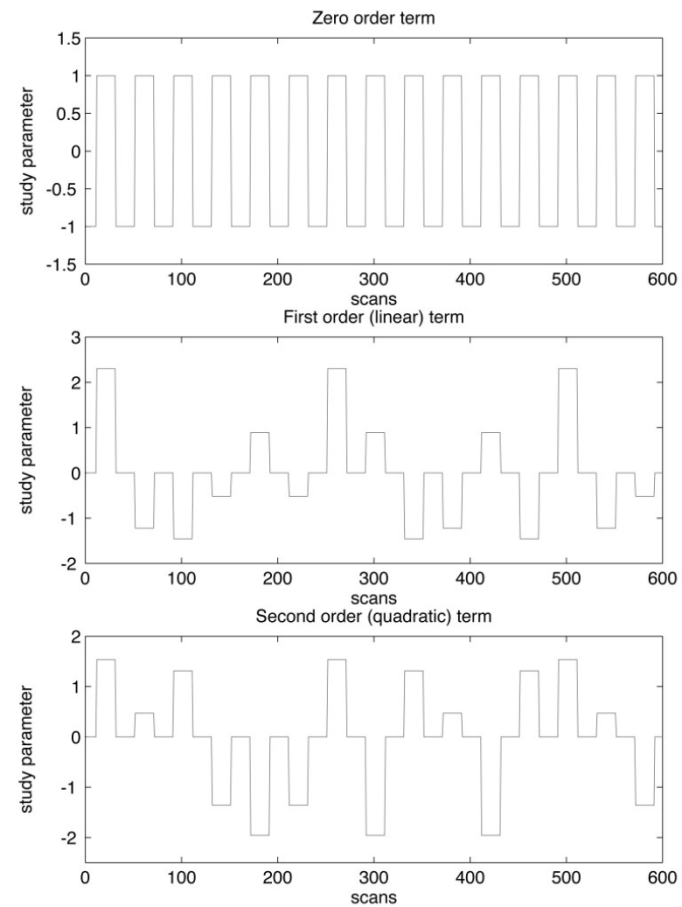
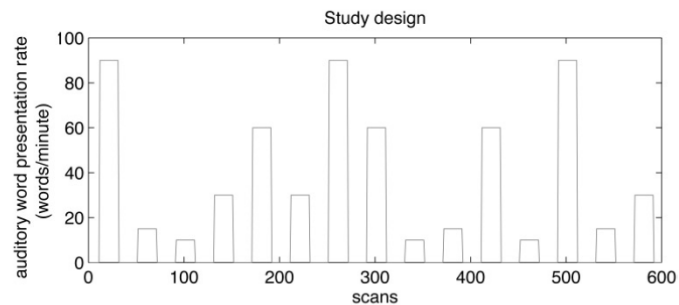
## Parametric modulation of regressors by time



# Parametric Designs

## Parametric modulation of regressors

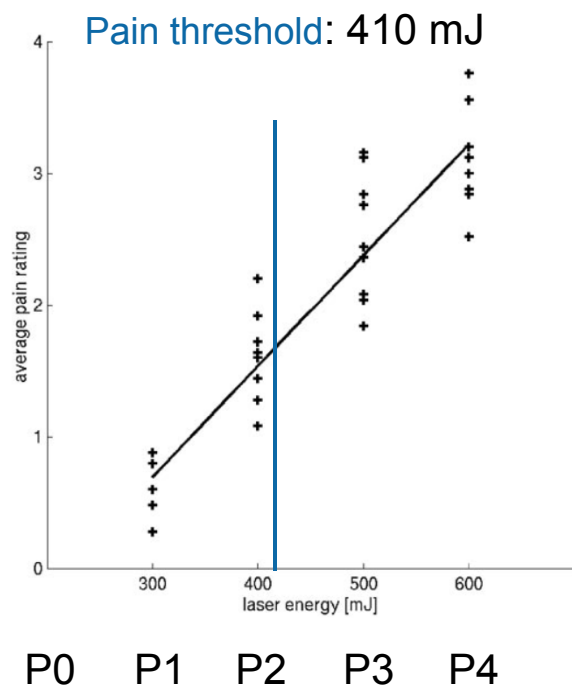
Polynomial expansion  
&  
orthogonalisation



Büchel et al., 1998, NeuroImage

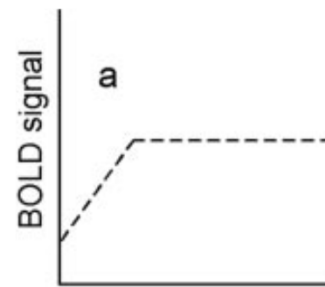
# Parametric Designs

Investigating neurometric functions

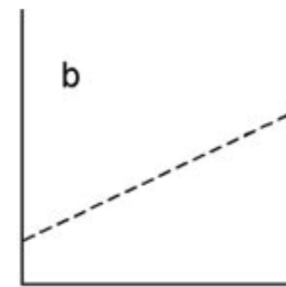


P0-P4: Variation of intensity of a laser stimulus applied to the right hand (0, 300, 400, 500, and 600 mJ)

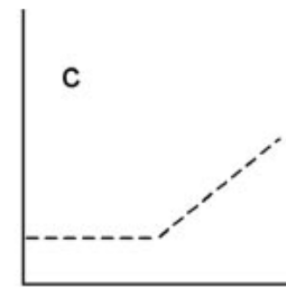
Stimulus awareness



Stimulus intensity



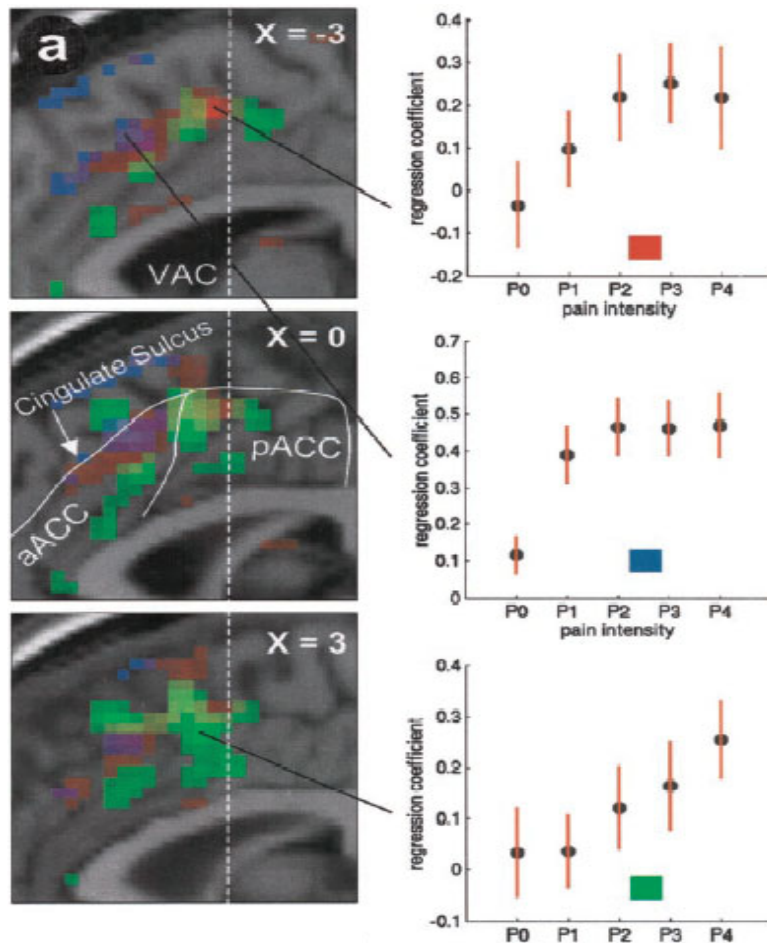
Pain intensity





# Parametric Designs

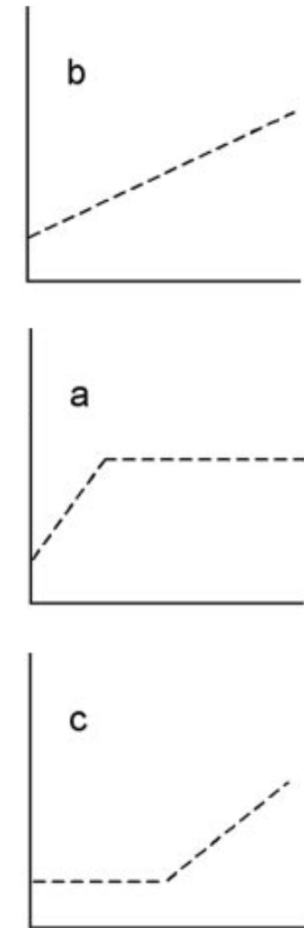
Investigating neurometric functions



→ Stimulus intensity  
dorsal pACC

→ Stimulus awareness  
cingulate sulcus aACC

→ Pain intensity  
ventral pACC



Büchel et al., 2002, J Neurosci

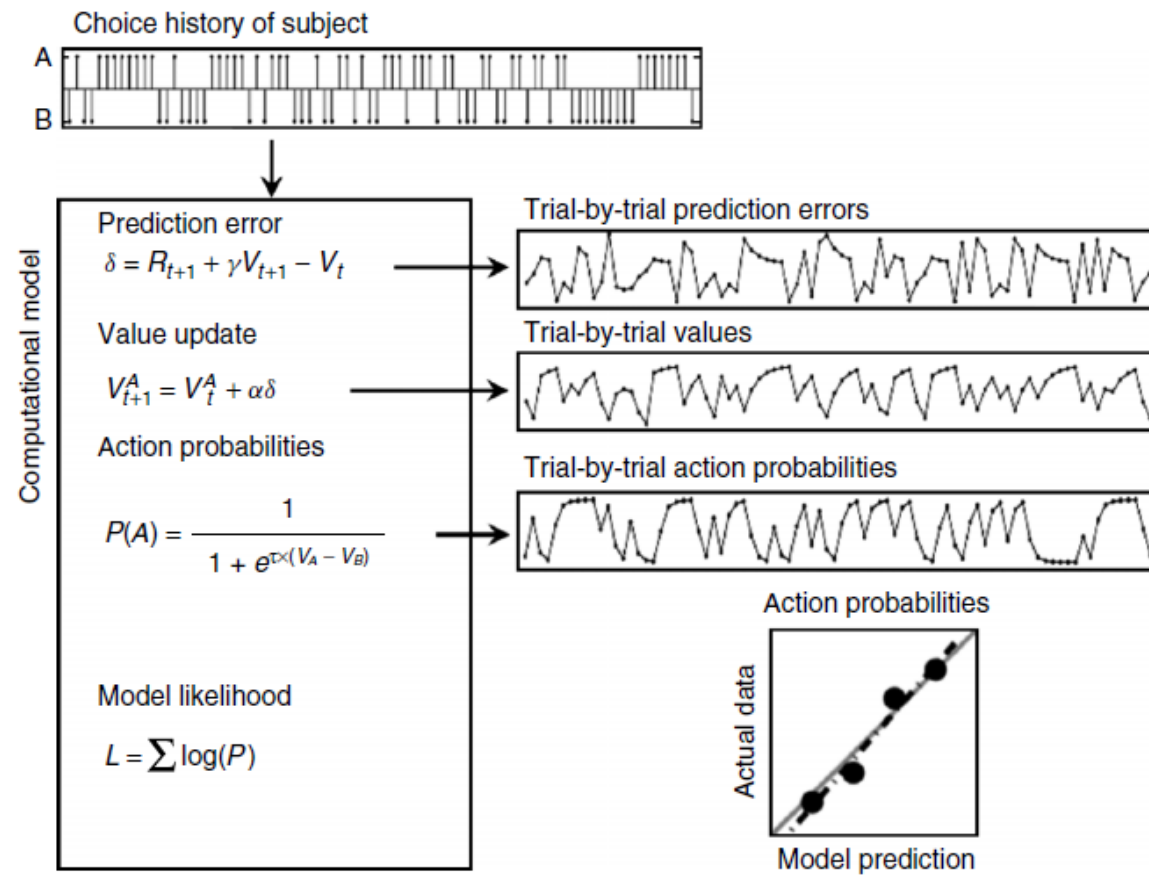
# Parametric Designs

## Model-based regressors

- General idea:  
generate predictions from a **computational model**, e.g. of learning or decision-making
- Commonly used models:
  - Rescorla-Wagner learning model
  - Temporal difference (TD) learning model
  - Bayesian models
- **Predictions used to define regressors**
- Inclusion of these regressors in a GLM and testing for significant correlations with voxel-wise BOLD responses

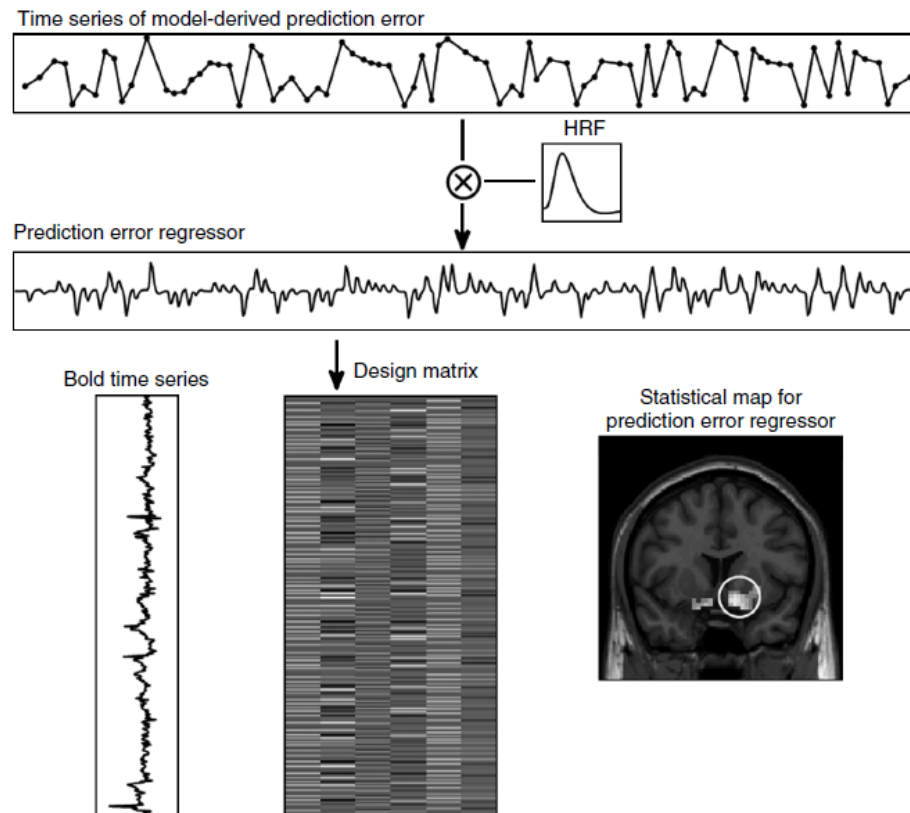
# Parametric Designs

## Model-based fMRI analysis, Example



# Parametric Designs

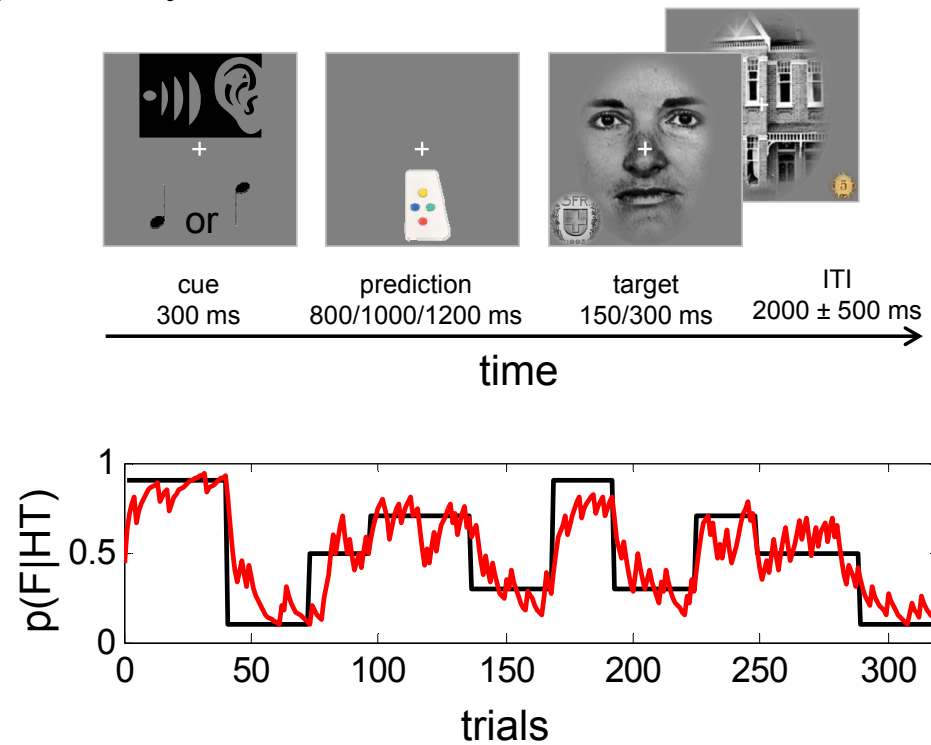
## Model-based fMRI analysis, Example



# Parametric Designs

## Model-based fMRI analysis, Example

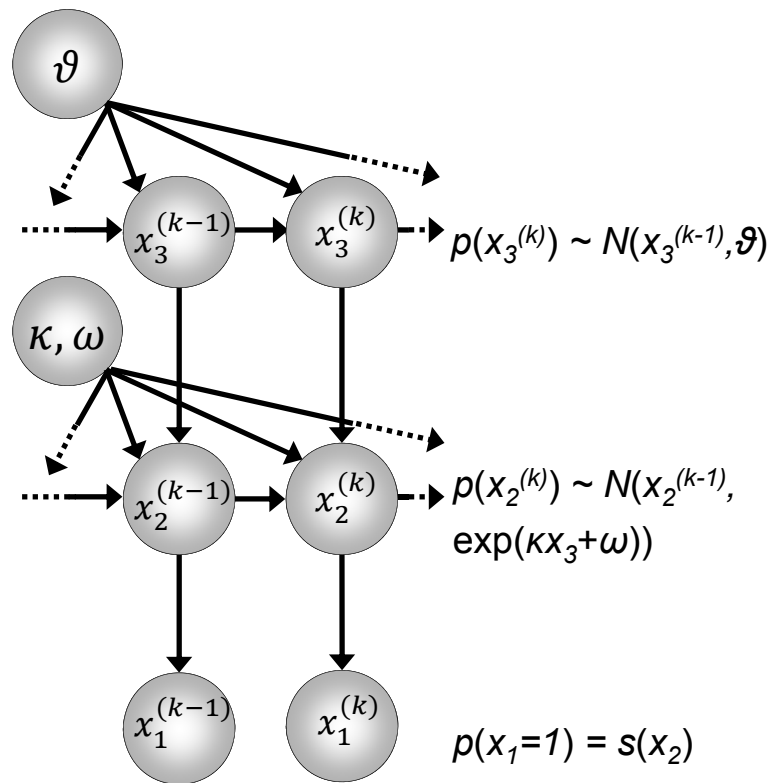
Hierarchical prediction errors  
about sensory outcome and its probability



# Parametric Designs

## Model-based fMRI analysis, Example

### The Hierarchical Gaussian Filter (HGF)



$$\Delta\mu_i \propto \frac{\hat{\pi}_{i-1}}{\pi_i} PE_{i-1}$$

$$\varepsilon_3 \propto \sigma_3^{(k)} \delta_2^{(k)}$$

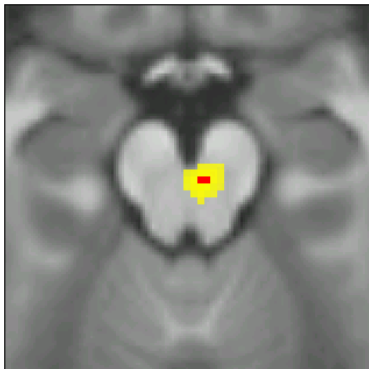
$$\varepsilon_2 = \sigma_2^{(k)} \delta_1^{(k)}$$

# Parametric Designs

## Model-based fMRI analysis, Example

Hierarchical prediction errors  
about sensory outcome and its probability

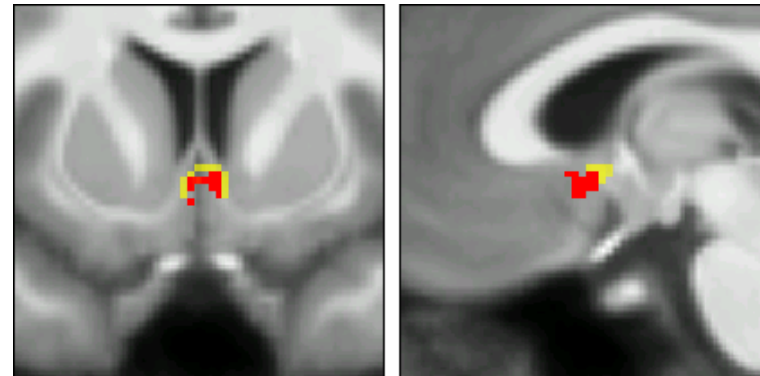
$\varepsilon_2$  in midbrain (N=45)



$$\varepsilon_2 = \sigma_2^{(k)} \delta_1^{(k)}$$

p<0.05, whole brain FWE corrected  
p<0.05, SVC FWE corrected

$\varepsilon_3$  in basal forebrain (N=45)



$$\varepsilon_3 \propto \sigma_3^{(k)} \delta_2^{(k)}$$

p<0.05, SVC FWE corrected  
p<0.001, uncorrected

# Overview Experimental Designs

- **Categorical designs**

- Subtraction - Pure insertion, evoked / differential responses
- Conjunction - Testing multiple hypotheses

- **Parametric designs**

- Linear - Adaptation, cognitive dimensions
- Nonlinear - Polynomial expansions, neurometric functions

- **Factorial designs**

- Categorical - Interactions and pure insertion
- Parametric
  - Linear and nonlinear interactions
  - Psychophysiological interactions



# Factorial Designs

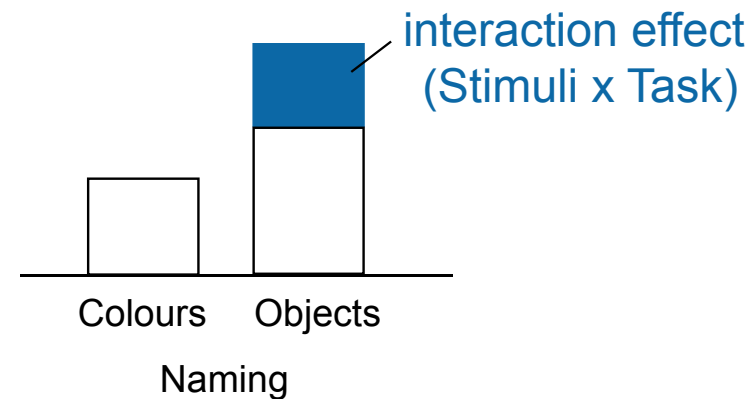
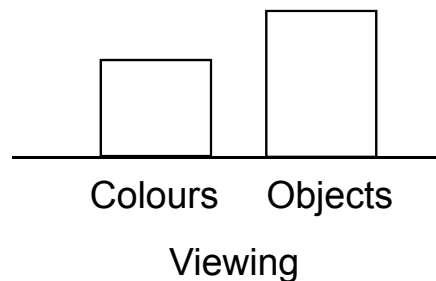
## Main effects and Interactions

		Task (1/2)	
		Viewing	Naming
Stimuli (A/B)	Colours	A1	A2
	Objects	B1	B2

- **Main effect of task:**  $(A1 + B1) - (A2 + B2)$
- **Main effect of stimuli:**  $(A1 + A2) - (B1 + B2)$
- **Interaction of task and stimuli:**  
Can show a failure of pure insertion

$$(A1 - B1) - (A2 - B2)$$

Is the inferotemporal region implicated in phonological retrieval during object naming?



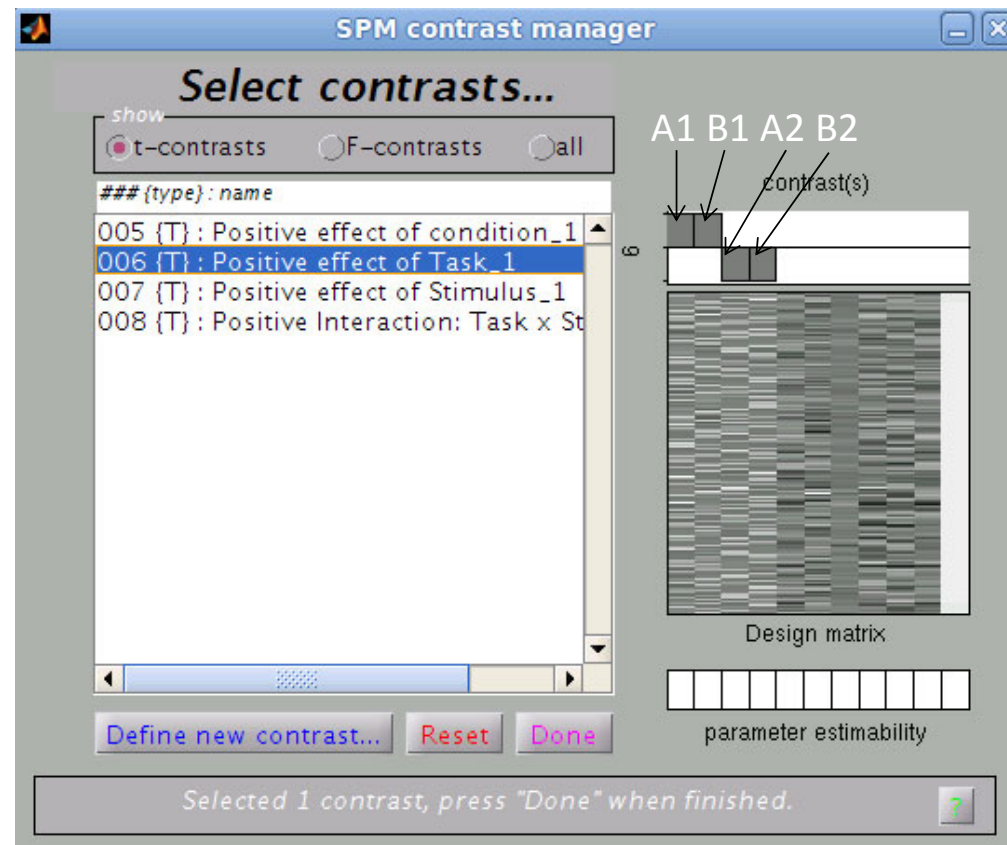
# Factorial Designs

Main effect, Example SPM

Task (1/2)	
Viewing	Naming
A1	A2
B1	B2

Stimuli (A/B)  
Objects Colours

Main effect of task:  
 $(A1 + B1) - (A2 + B2)$



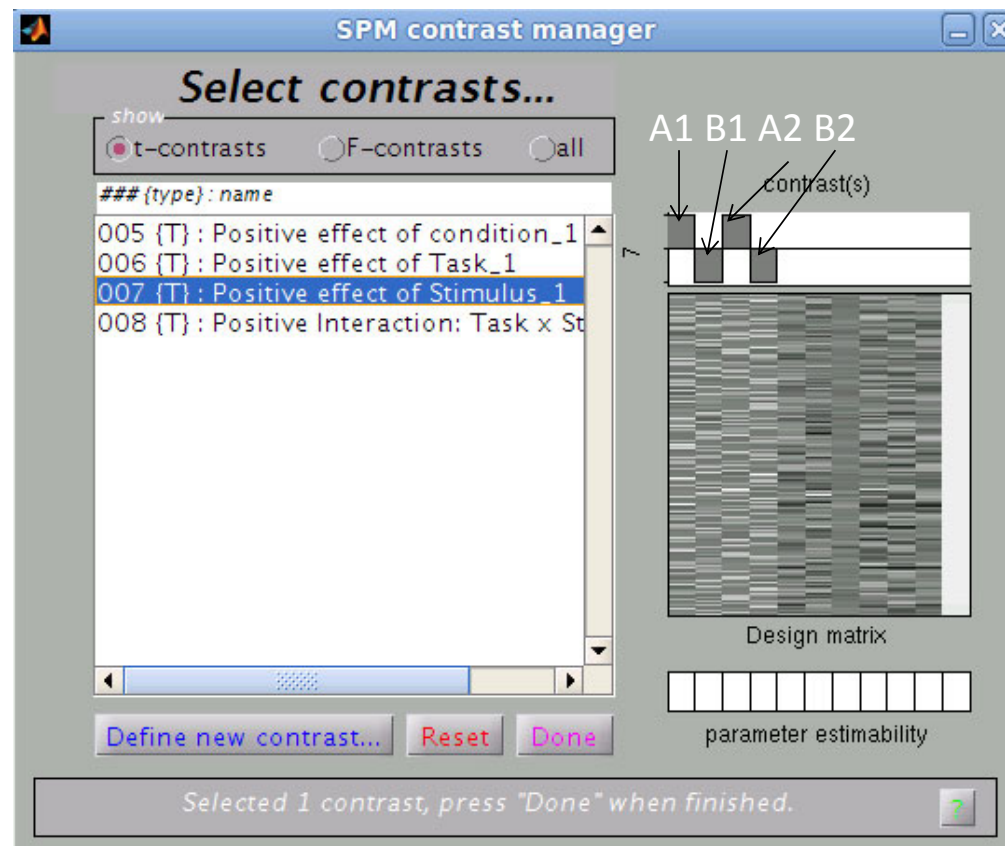
# Factorial Designs

Main effect, Example SPM

Task (1/2)	
Viewing	Naming
A1	A2
B1	B2

Stimuli (A/B)  
Objects Colours

Main effect of stimuli:  
 $(A1 + A2) - (B1 + B2)$



# Factorial Designs

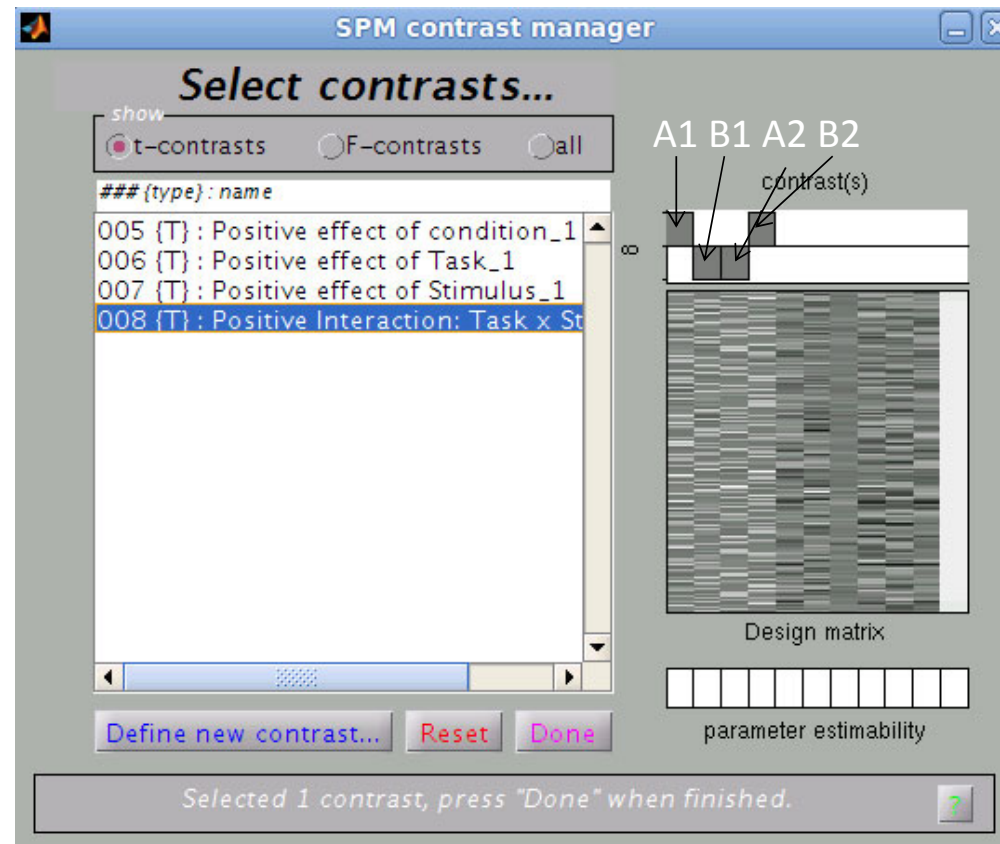
Interaction, Example SPM

Task (1/2)	
Viewing	Naming
A1	A2
B1	B2

Stimuli (A/B)

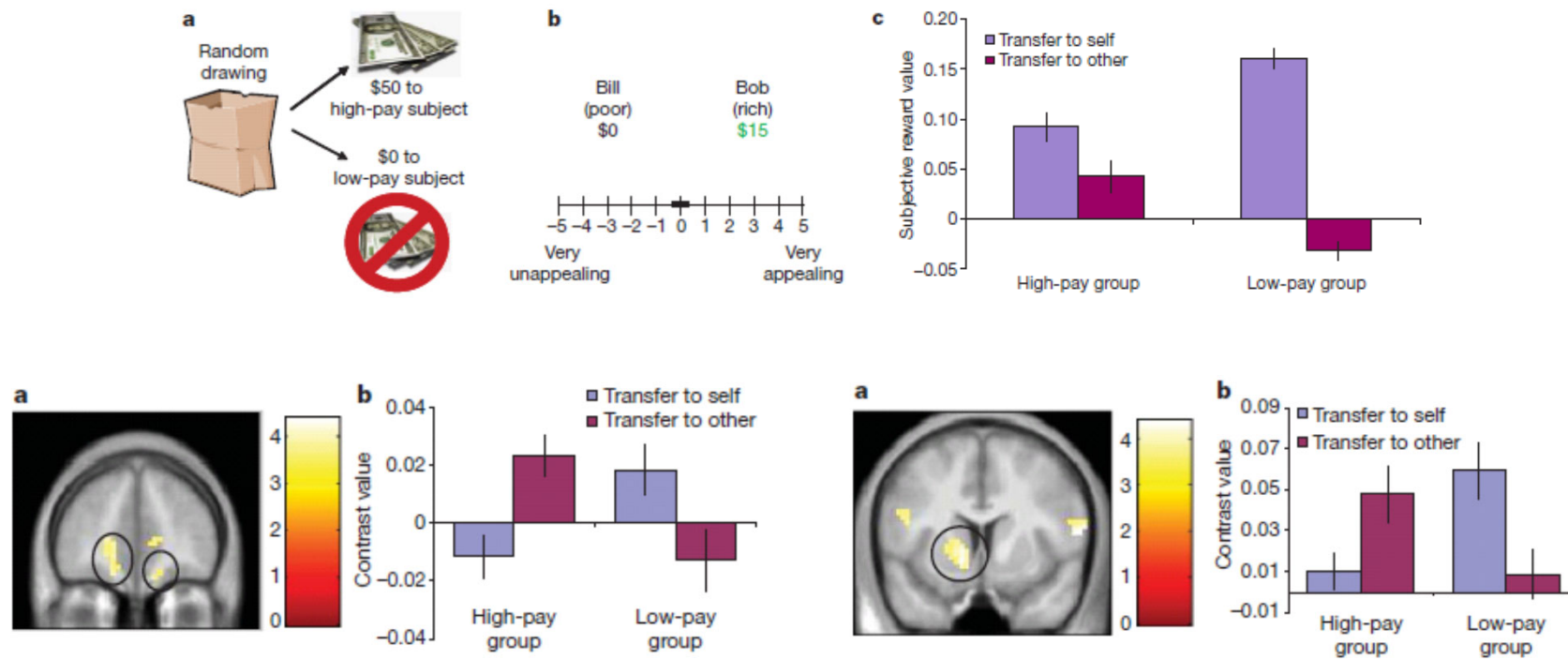
Objects Colours

Interaction of task and stimuli:  
 $(A1 - B1) - (A2 - B2)$



# Factorial Designs

## Example



# Factorial Designs

## Psycho-Physiological Interactions (PPIs)

		Task factor	
		Task A	Task B
Stimulus factor	Stim 1	$T_A/S_1$	$T_B/S_1$
	Stim 2	$T_A/S_2$	$T_B/S_2$

GLM of a 2x2 factorial design:

$$y = (T_A - T_B) \beta_1 + (S_1 - S_2) \beta_2 + (T_A - T_B)(S_1 - S_2) \beta_3 + e$$

$\leftarrow$  main effect of task  
 $\leftarrow$  main effect of stim. type  
 interaction

We can replace one main effect in the GLM by the time series of an area that shows this main effect.

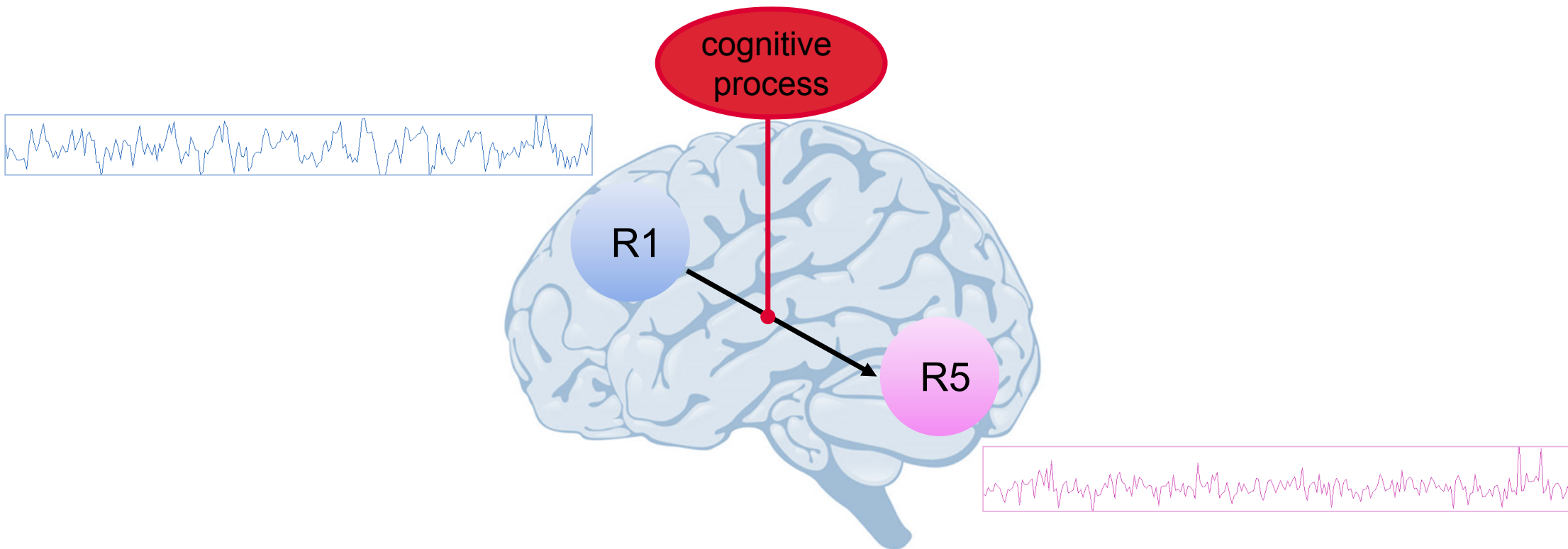
E.g. let's replace the main effect of stimulus type by the time series of area V1.

$$y = (T_A - T_B) \beta_1 + V1 \beta_2 + (T_A - T_B) V1 \beta_3 + e$$

$\leftarrow$  main effect of task  
 $\leftarrow$  V1 time series  $\approx$  main effect of stim. type  
 PPI

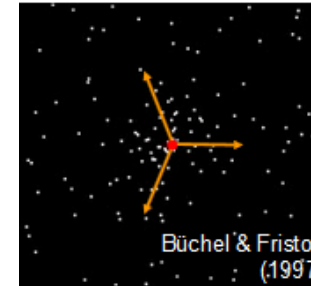
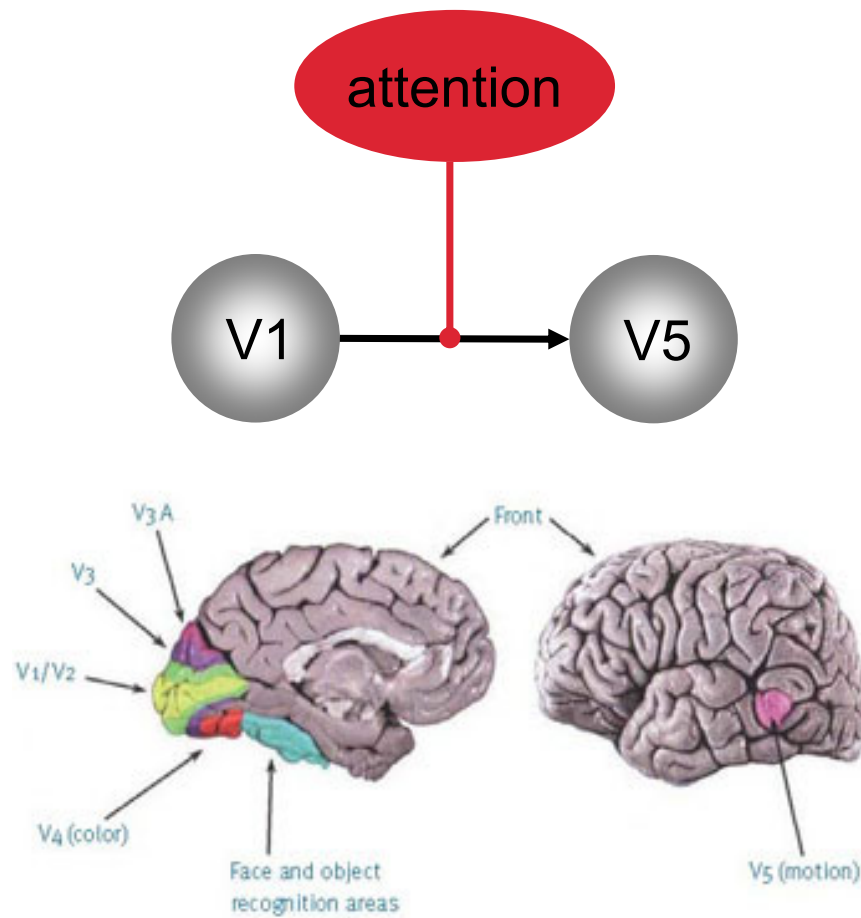
# Factorial Designs

## Psycho-Physiological Interactions (PPIs)



# Factorial Designs

PPI, Example



Radially moving dots

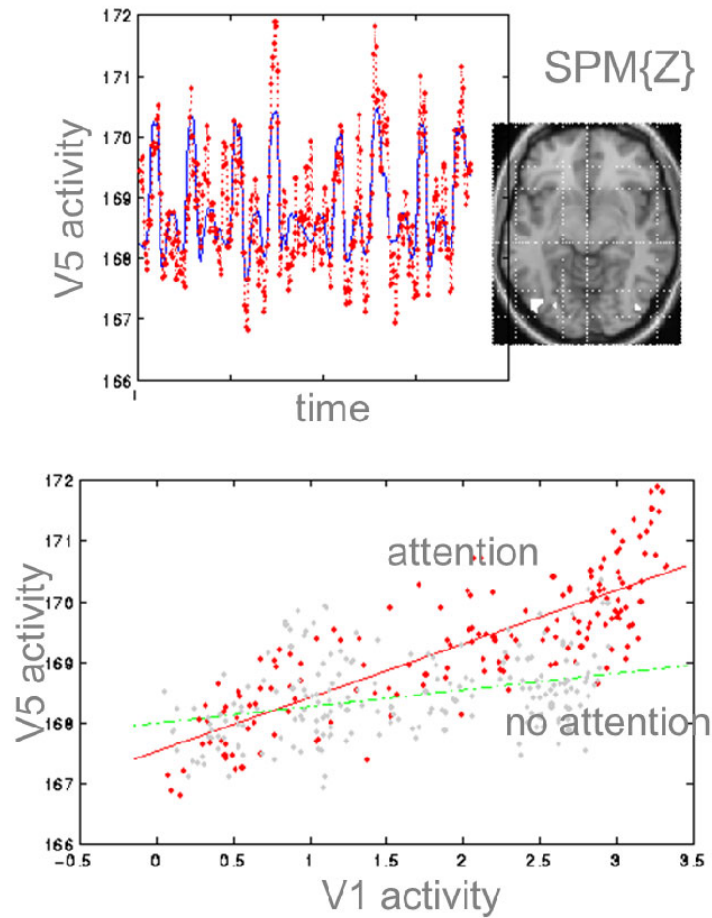
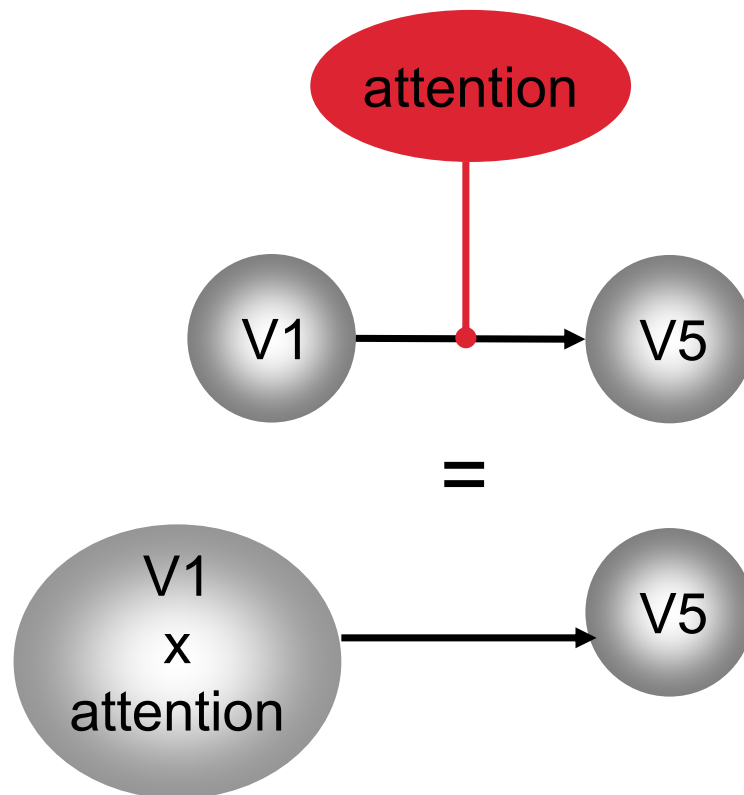
Conditions:

- Stationary
- Motion and attention ("detect changes")
- Motion without attention



# Factorial Designs

## PPI, Example



Friston et al. 1997, NeuroImage

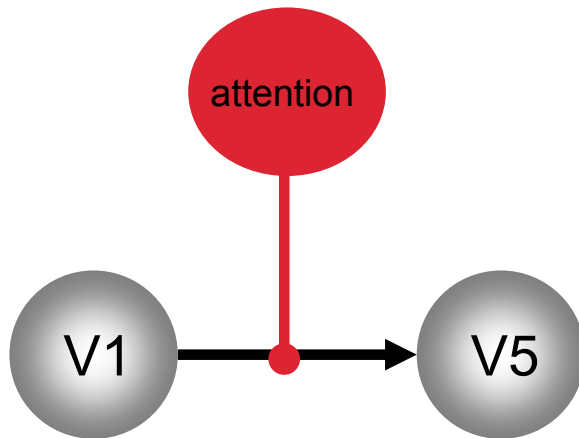
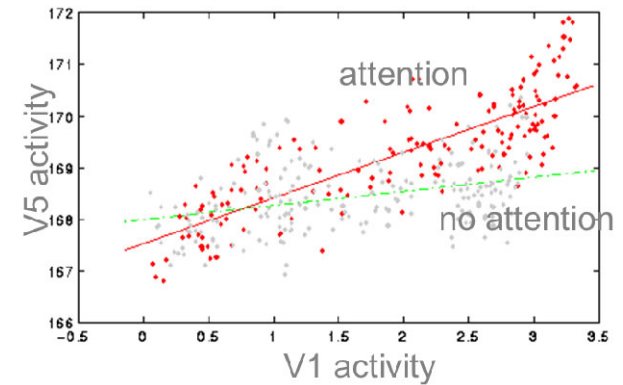
Büchel & Friston, 1997, Cereb. Cortex

# Factorial Designs

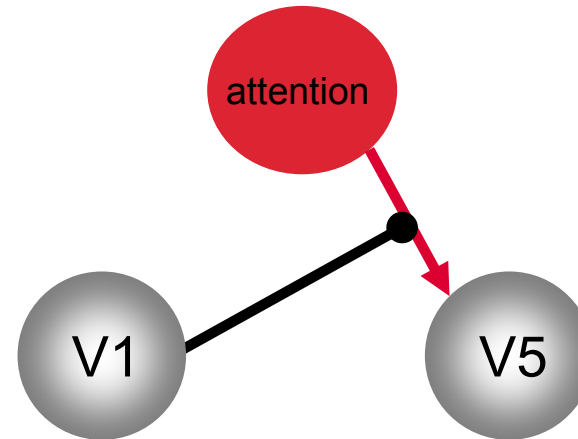
## PPI, Example

$$y = (T_A - T_B) \beta_1 + V1 \beta_2 + (T_A - T_B) V1 \beta_3 + e$$

Two possible interpretations of the PPI term



Modulation of V1 → V5 by attention



Modulation of attention → V5 by V1

# Questions?

- Categorical designs

- |             |   |
|-------------|---|
| Subtraction | - Pure insertion, evoked / differential responses |
| Conjunction | - Testing multiple hypotheses                     |

- Parametric designs

- |           |  |
|-----------|--|
| Linear    | - Adaptation, cognitive dimensions             |
| Nonlinear | - Polynomial expansions, neurometric functions |

- Factorial designs

- |             |                                     |
|-------------|-------------------------------------|
| Categorical | - Interactions and pure insertion   |
| Parametric  | - Linear and nonlinear interactions |
|             | - Psychophysiological interactions  |